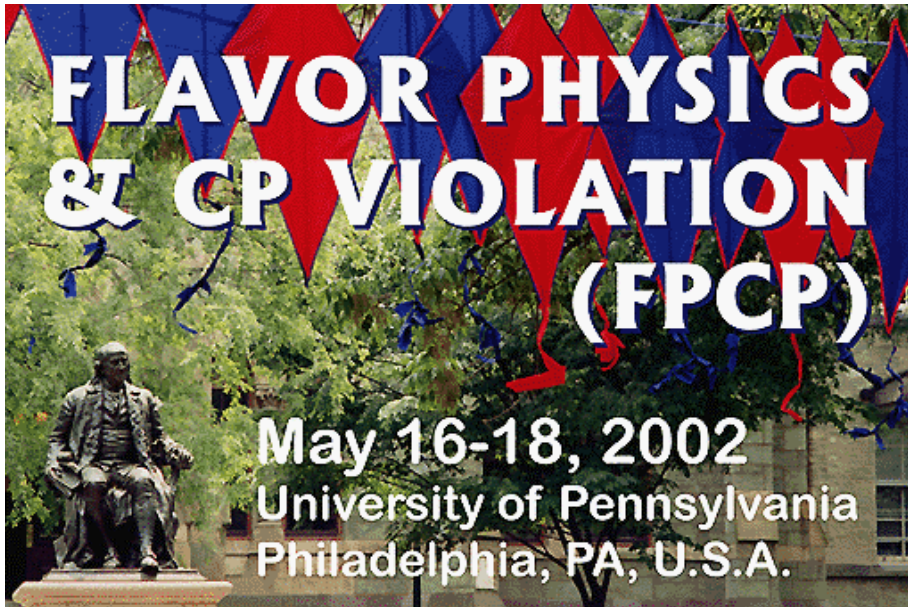


$\text{Sin}2\phi_2(=\alpha)$ from Belle

Eunil Won (Korea Univ) for
the Belle Collaboration



Outline

$\text{sin}2\phi_2$ and $B \rightarrow \pi\pi$ decay
Event Selection
CP fit results
Summary

Measuring CKM Angles with B decays

From time dependent decay asymmetry,

$$\frac{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) - \Gamma(B_{phys}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{phys}^0(t) \rightarrow f_{CP}) + \Gamma(B_{phys}^0(t) \rightarrow f_{CP})} = S_{f_{CP}} \sin(\Delta m_d \Delta t) + A_{f_{CP}} \cos(\Delta m \Delta t)$$

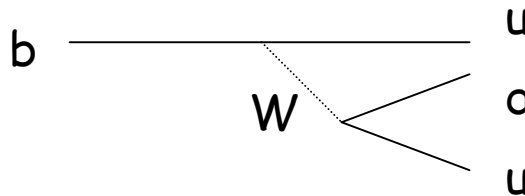
where $A_{f_{CP}} = \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1}$ and $S_{f_{CP}} = \frac{2 \text{Im } \lambda}{|\lambda|^2 + 1}$ $\lambda = q / p \bar{A} / A$
 $|B_L\rangle = p |B^0\rangle + q |\bar{B}^0\rangle$

Mode	$A_{f_{CP}}$	$S_{f_{CP}}$
$B \rightarrow J/\psi K_s$	0	$\sin 2\phi_1$
$B \rightarrow \pi^+ \pi^-$	nonzero	$\sim \sin 2(\phi_2 + \theta)$

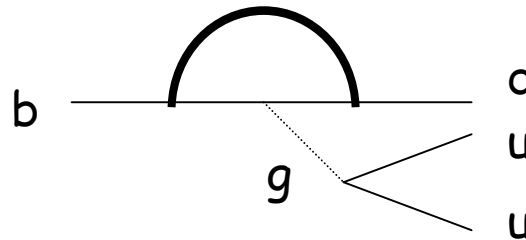
$S_{f_{CP}}$ is identical to $\sin 2\phi_2$ if there is no penguin amplitudes
 (θ : relative phase btw penguin contributions in $\bar{A}_{\pi\pi}$ and $A_{\pi\pi}$)

CP violation in $B \rightarrow \pi^+\pi^-$ decay

Tree Amplitude (T)



Penguin Amplitude (P)



Possibility of significant contributions from gluonic $b \rightarrow d$ penguin amplitudes

$$\rightarrow S_{\pi\pi} \neq \sin 2\phi_2$$

$$A_{\pi\pi} \neq 0 \text{ (indicating direct CP violation)}$$

$$\Gamma(K\pi) \sim 3\Gamma(\pi\pi) \rightarrow \text{penguins} \sim V_{ub} \text{ trees}$$

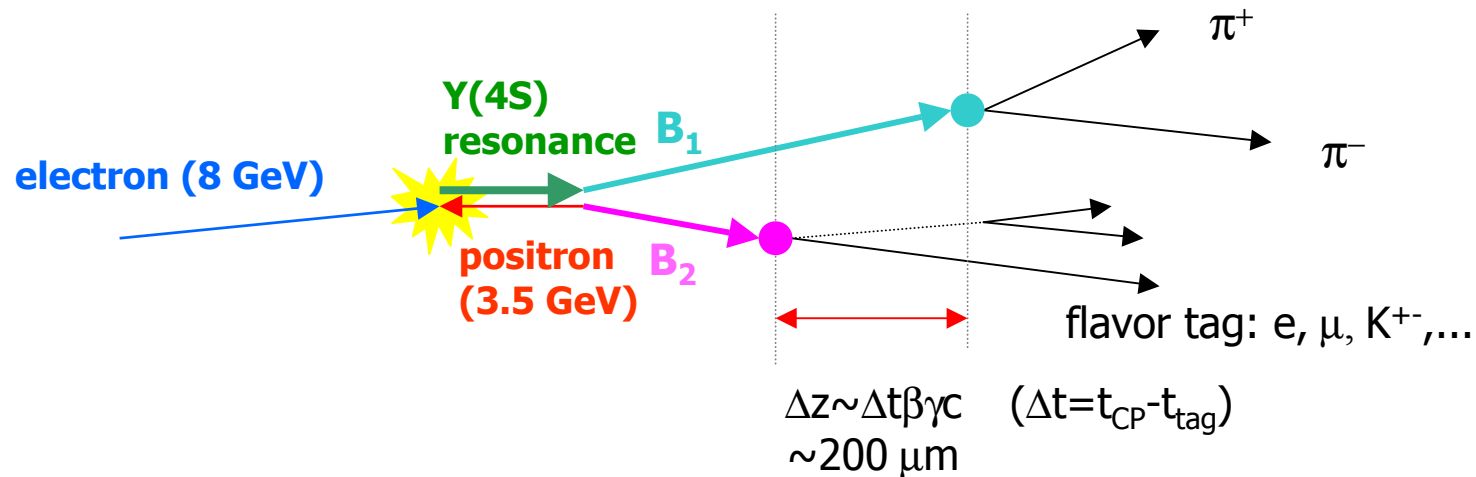
Isospin analysis is required for a clean determination of the angle ϕ_2

→ For this, one needs to know $\text{Br}(\bar{B}^0 \rightarrow \pi^0\pi^0)$ and $\text{Br}(B^0 \rightarrow \pi^0\pi^0)$ separately
(experimentally difficult...)

Hep-ph/ 0105308, Gronau et al:

$S_{\pi\pi} \sim \sin 2(\phi_2 + \theta)$ and put an upper bound on $|2\theta|$ ("Gronau bound") with knowing $B^{00} = \frac{1}{2}(|A^{00}|^2 + |\bar{A}^{00}|^2)$ only

Measurement of CPV asymmetries in $B \rightarrow \pi^+ \pi^-$



The method is very similar to that of $\sin 2\phi_1$

One needs to introduce **direct CP violation term** ($A_{\pi\pi}$) in the CP fitting procedure

$$q = \begin{cases} +1 & B \text{ tag} \\ -1 & \bar{B} \text{ tag} \end{cases}$$

The decay rate distribution $R_q(\Delta t)$ is given by

$$R_q(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} \left[1 + q \left\{ A_{\pi\pi} \cos(\Delta m \Delta t) + S_{\pi\pi} \sin(\Delta m \Delta t) \right\} \right]$$

Event Selection (42 fb⁻¹)

Oppositely charged pairs of well measured track

remove electron candidates and assume all are π or K
require π identification (likelihood ratio using ACC and dE/dx)

$$(\epsilon_{\pi} = 0.900 \pm 0.005, f_{\pi \rightarrow K} = 0.064 \pm 0.002)$$

B candidate selection

Energy difference ($-300 < \Delta E < 500$ MeV)

Beam energy constrained mass ($m_{bc} > 5.2$ GeV)

(includes side band at this stage)

$$\Delta E \equiv E_{\pi} + E_{\pi} - E_{CM} / 2$$

$$m_{bc} = \sqrt{(E_{CM} / 2)^2 - (\vec{p}_{\pi} + \vec{p}_{\pi})^2}$$

Continuum background suppression

Likelihood ratio using event shape variables

(Modified Fox-Wolfram variables and B flight direction)

Rare B decay backgrounds

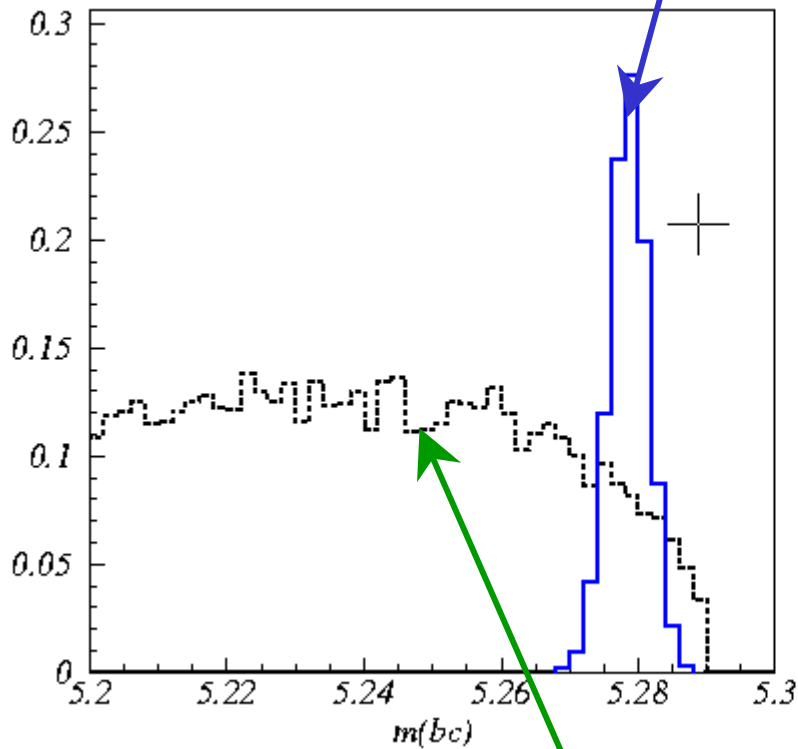
shifted in ΔE distribution

→ subtraction considered in the yield extraction

B meson Reconstruction

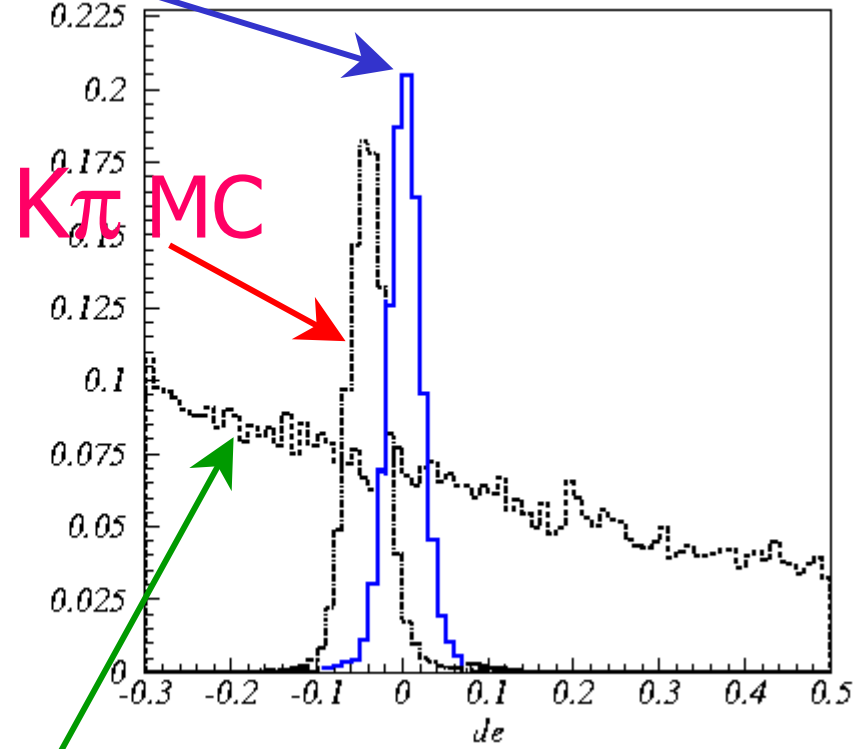
$K\pi$ is indistinguishable in m_{bc}
but shifted by -45 MeV in ΔE

$\pi^+\pi^-$ MC



m_{bc}

Off resonance Data

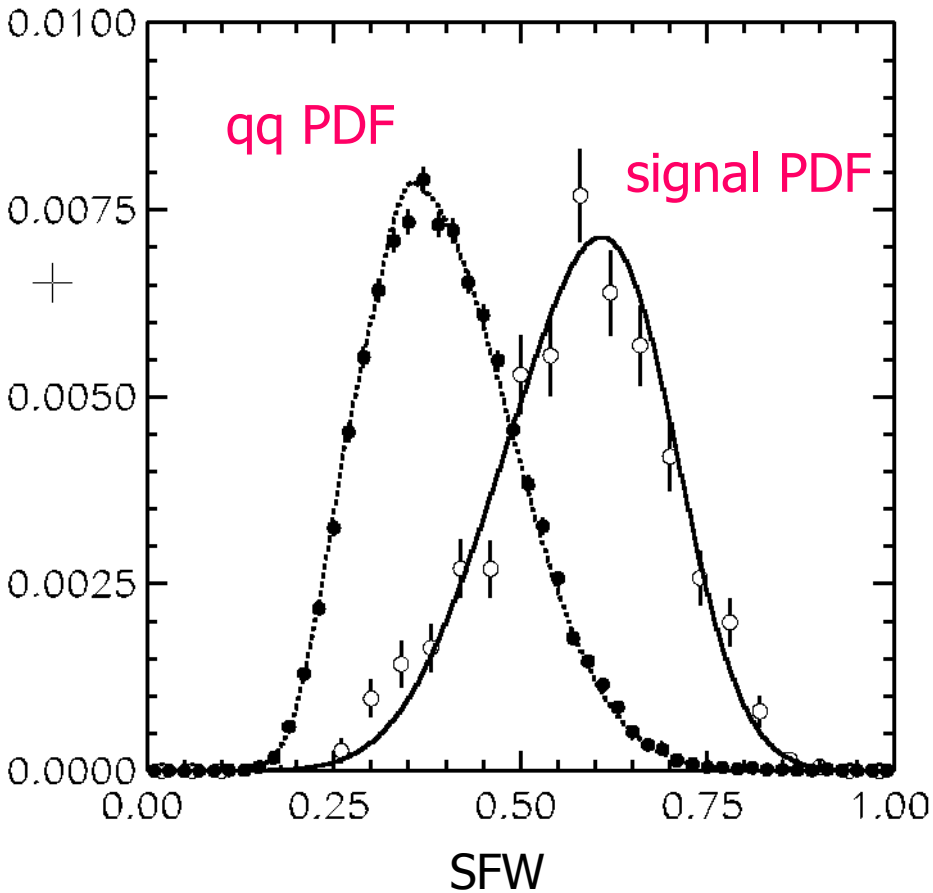


$K\pi$ MC

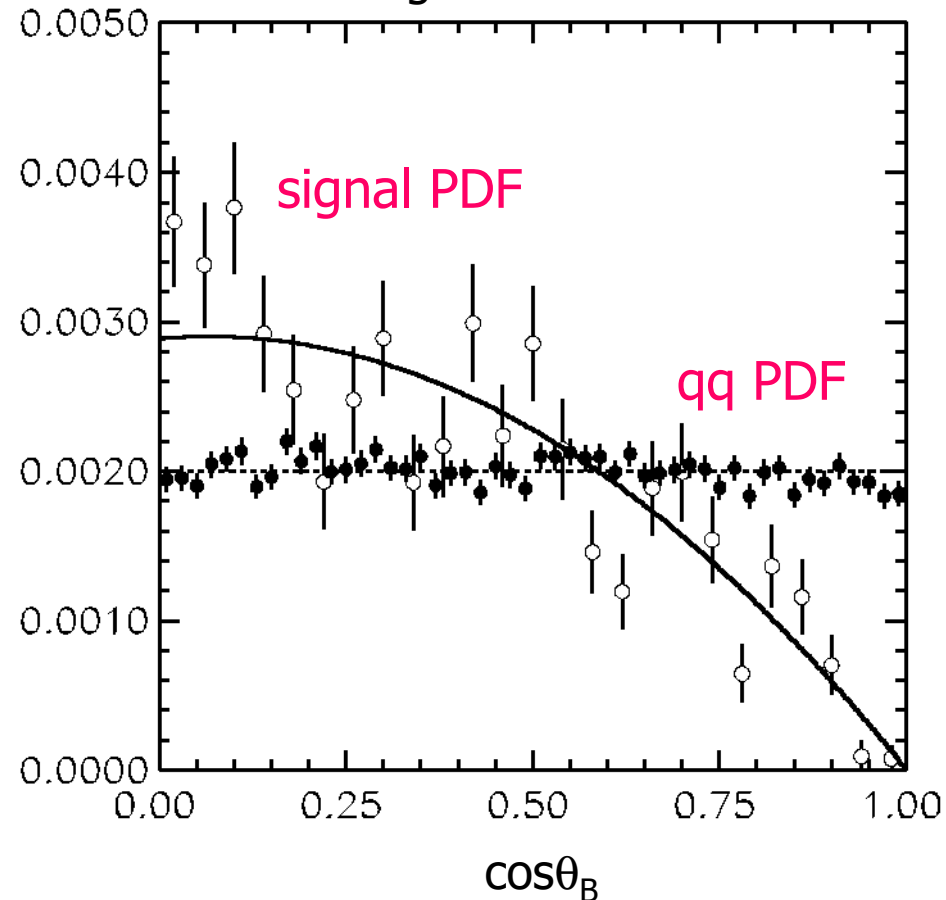
ΔE

Continuum Suppression

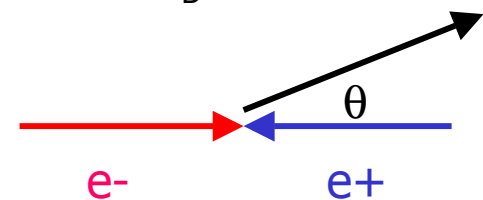
event shape variable based Fisher Disc



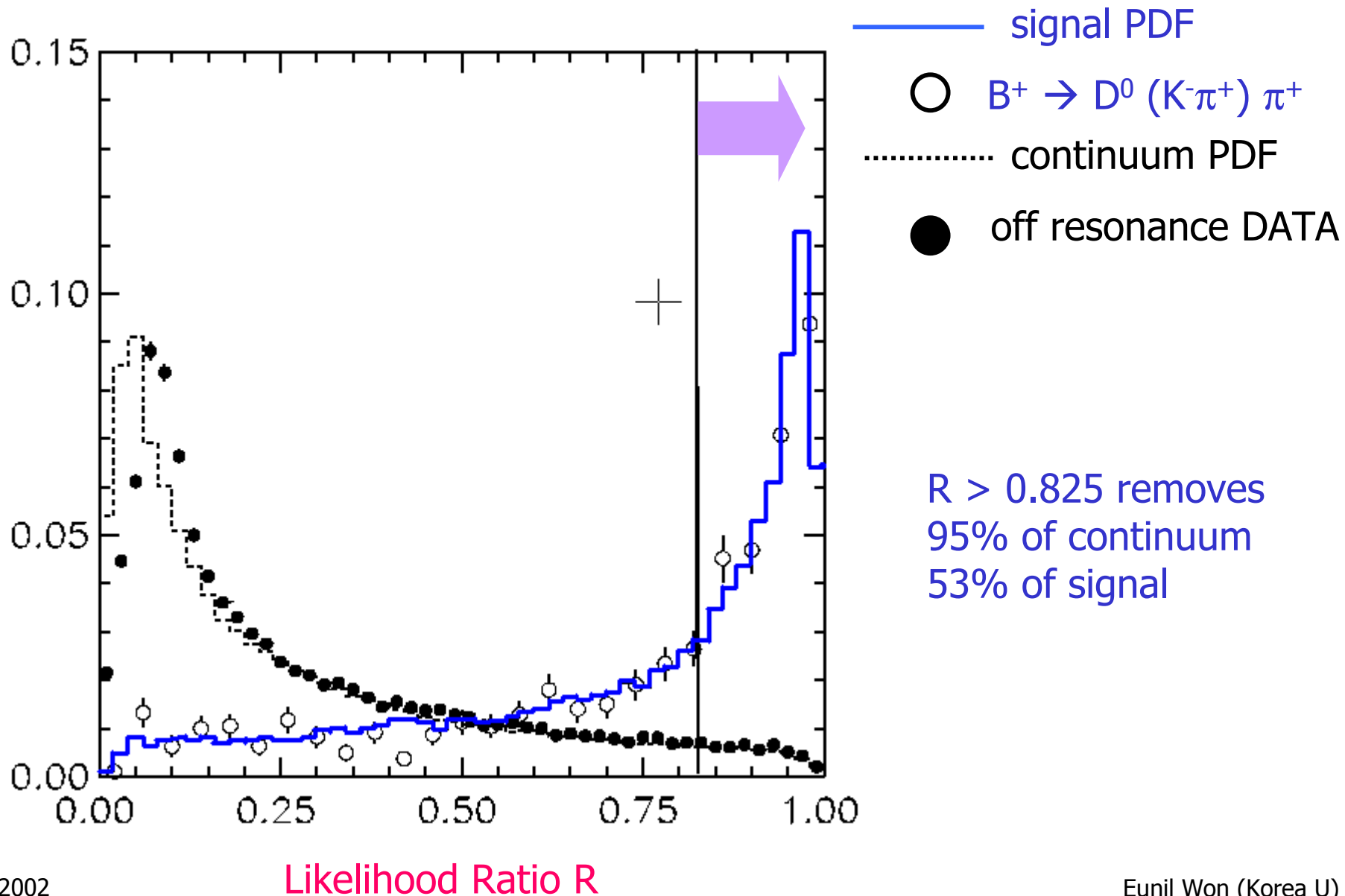
B flight direction



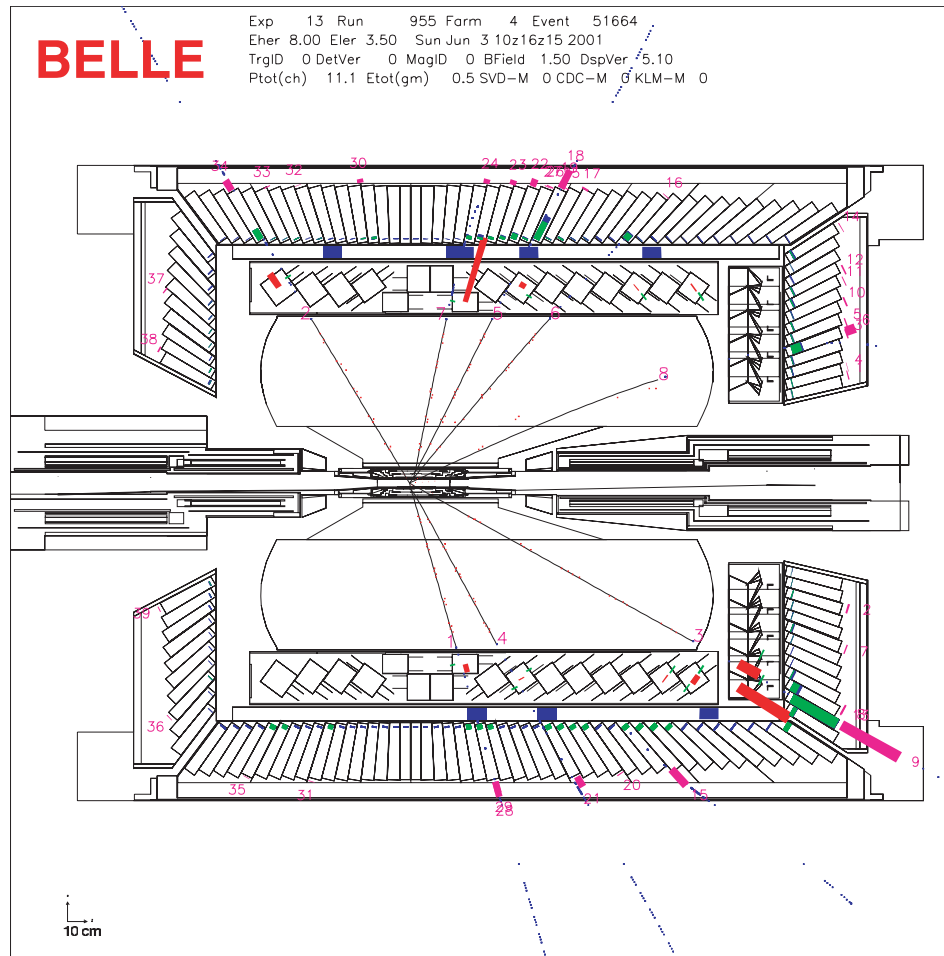
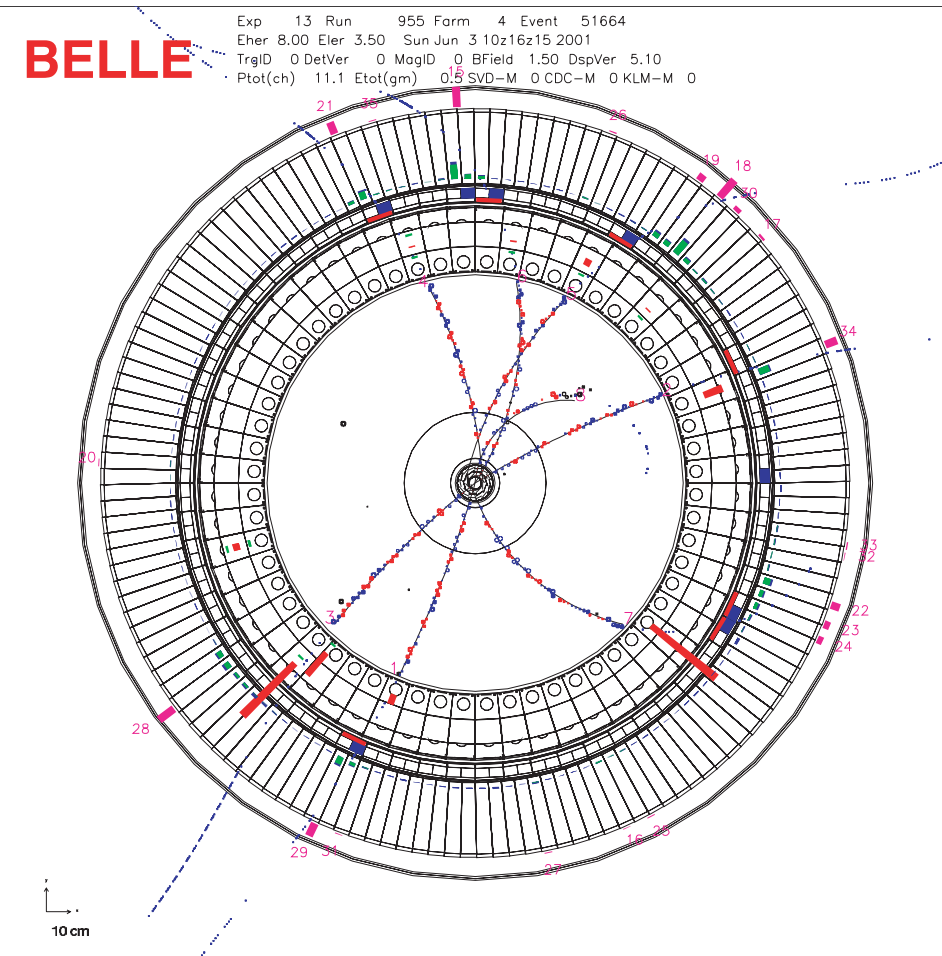
$$SFW = \sum_{2,4} \alpha_i \frac{h_{os}^i}{h_{os}^0} + \sum_{1-4} \beta_i \frac{h_{oo}^i}{h_{oo}^0}$$



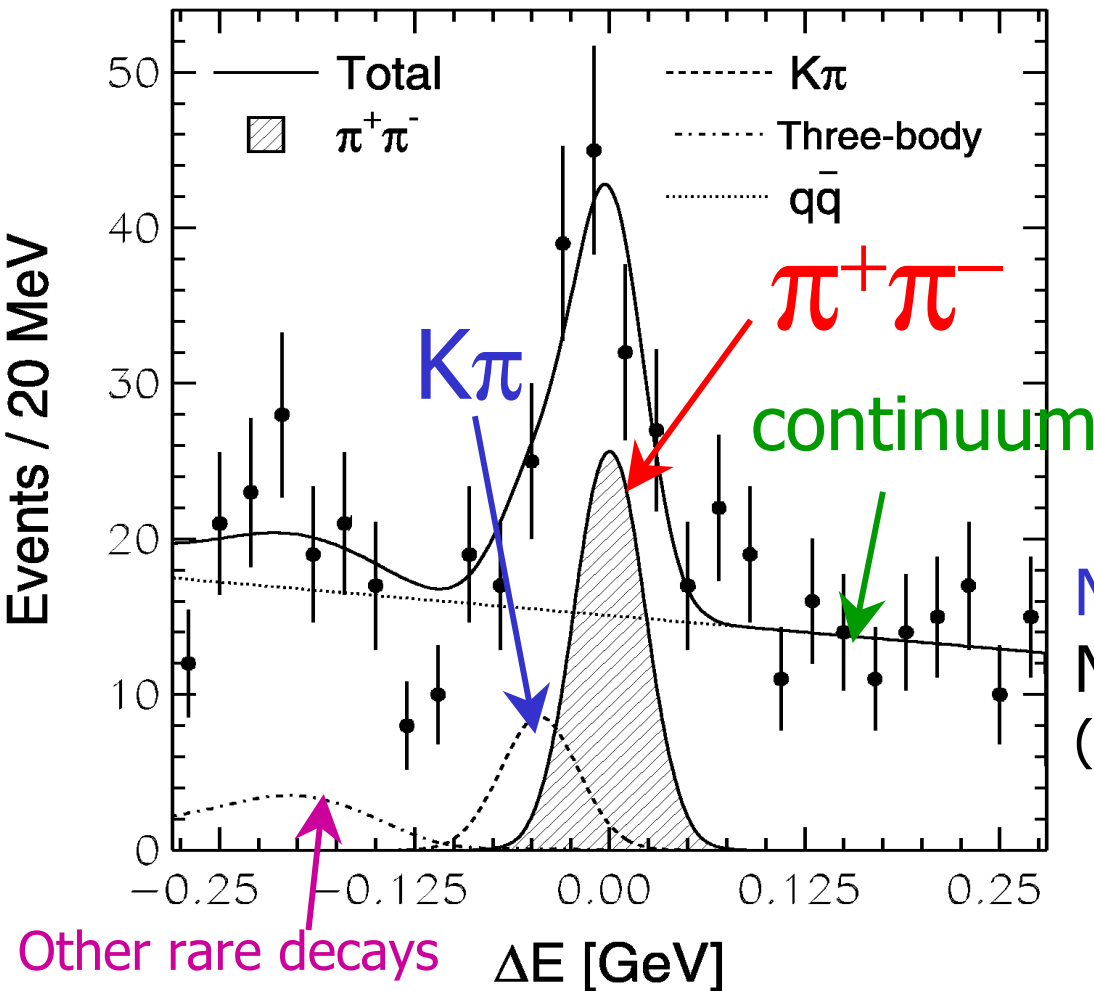
Continuum Suppression



$B^0 \rightarrow \pi^+\pi^-$ example



Signal Yield for $B \rightarrow \pi^+ \pi^-$



$$5.271 < m_{bc} < 5.287 \text{ GeV}$$

Fits in ΔE distribution w/

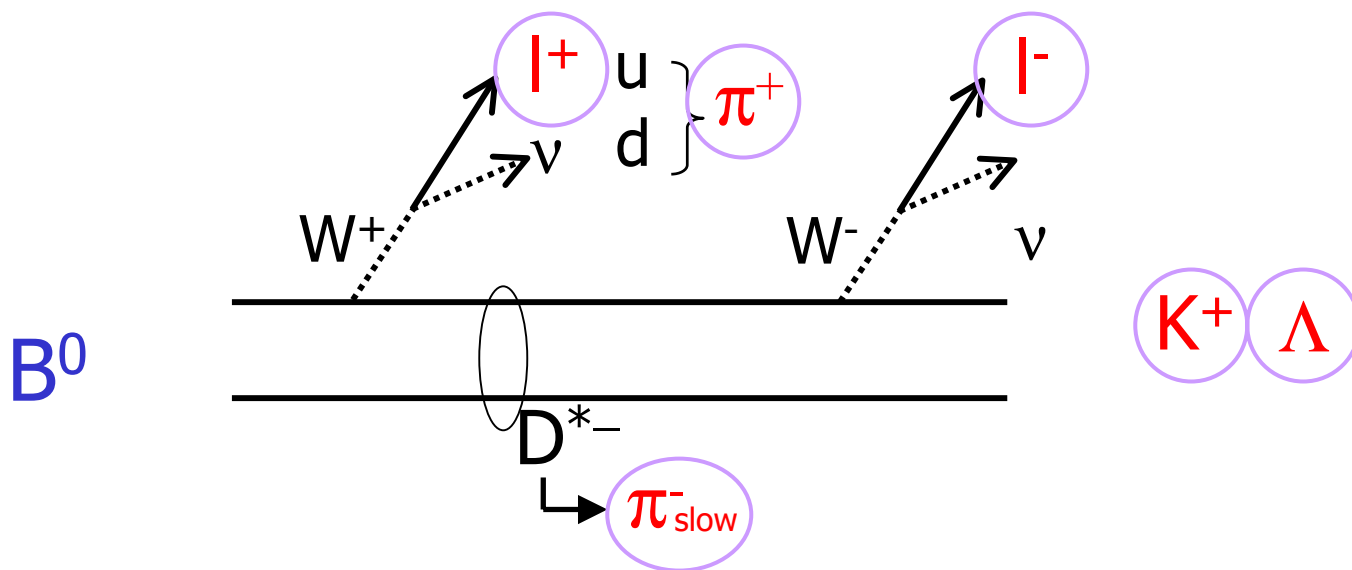
Signal
 Continuum
 $K\pi$ feed across
 Rare decays

$$N(\pi\pi) = 73.5 \pm 13.8 \text{ events}$$

$$N(K\pi) = 28.4 \pm 12.5 \text{ events}$$

(feed across)

Flavor Tagging



High-p (primary), low-p (secondary) leptons

Strangeness ($b \rightarrow c \rightarrow s$)

Fast π , slow π

Identical flavor tagging method as used in $\sin 2\phi_1$ measurement
 two stage (track and event level) multi dimensional likelihood
 Total effective tagging efficiency : 29.6%

Vertex Reconstruction

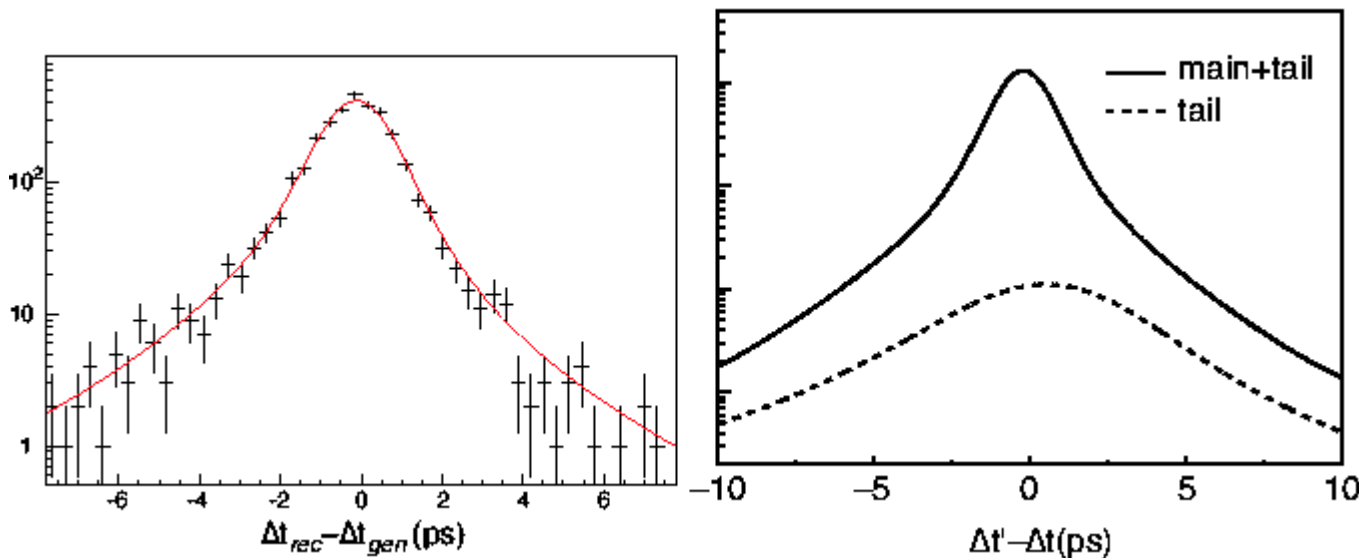
Vertex reconstruction and resolution functions are **same as that used for the $\sin 2\phi_1$ analysis of LP01**

MC study shows little difference btw $\pi\pi$ and J/ψ samples

Both signal and background resolution functions are in same functional form:

$$R(\Delta t_B - \Delta t') = (1 - f_{tail}) \frac{1}{\sqrt{2\pi}\sigma_{\Delta t}} e^{-\frac{(\Delta t_B - \Delta t' - \mu_{\Delta t})^2}{2\sigma^2}} + f_{tail} \frac{1}{\sqrt{2\pi}\sigma_{tail}^{\Delta t}} e^{-\frac{(\Delta t_B - \Delta t' - \mu_{tail}^{\Delta t})^2}{2(\sigma_{tail}^{\Delta t})^2}}$$

Sum of two Gaussians modeling main and tail part respectively



CP fit for $S_{\pi\pi}$ and $A_{\pi\pi}$

PDF for $\pi\pi$ signal events

$$P_{\pi\pi}(\Delta t, q, w_l) = \frac{e^{|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \{1 + q(1 - 2w_l) \times (A_{\pi\pi} \cos(\Delta m_d \Delta t) + S_{\pi\pi} \sin(\Delta m_d \Delta t))\}$$

for $K\pi$ events

$$P_{K\pi}(\Delta t, q, w_l) = \frac{e^{|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \{1 + q(1 - 2w_l) \times A_{K\pi} \cos(\Delta m_d \Delta t)\}$$

for continuum background

$$P_{q\bar{q}}(\Delta t) = \frac{1}{2} \left\{ f_\tau \frac{e^{|\Delta t|/\tau_{bkg}}}{2\tau_{bkg}} + (1 - f_\tau) \delta(\Delta t) \right\}$$

$$f_\tau = 0.011 \pm 0.004$$

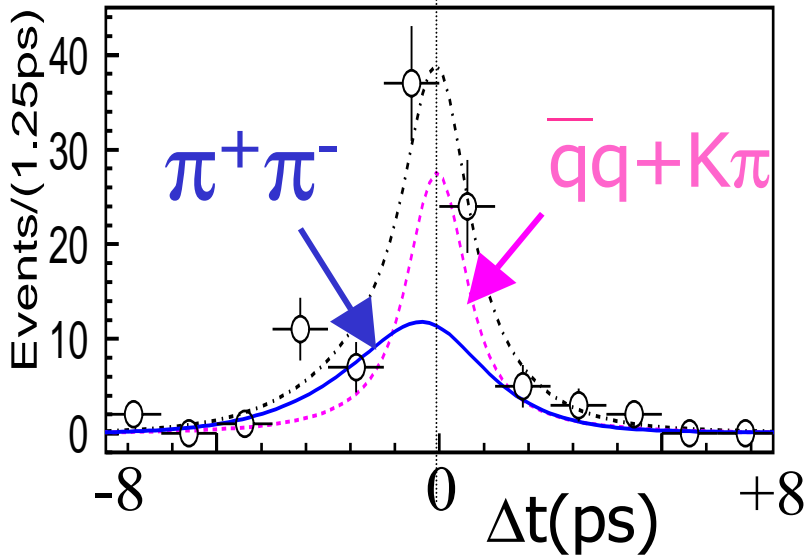
$$\tau_{bkg} = 2.68 + 0.95 - 0.72 \text{ ps}$$

Construct event by event (unbinned) likelihood as PDF \otimes Resolution function and maximize product of them

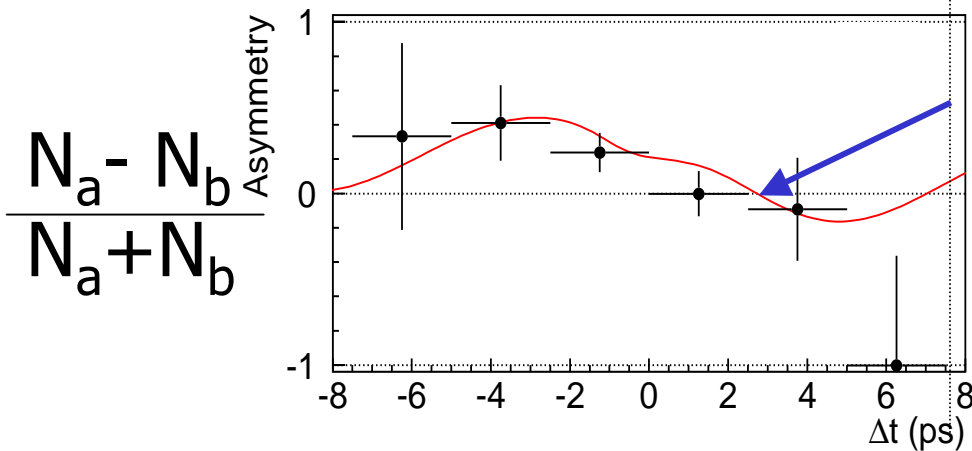
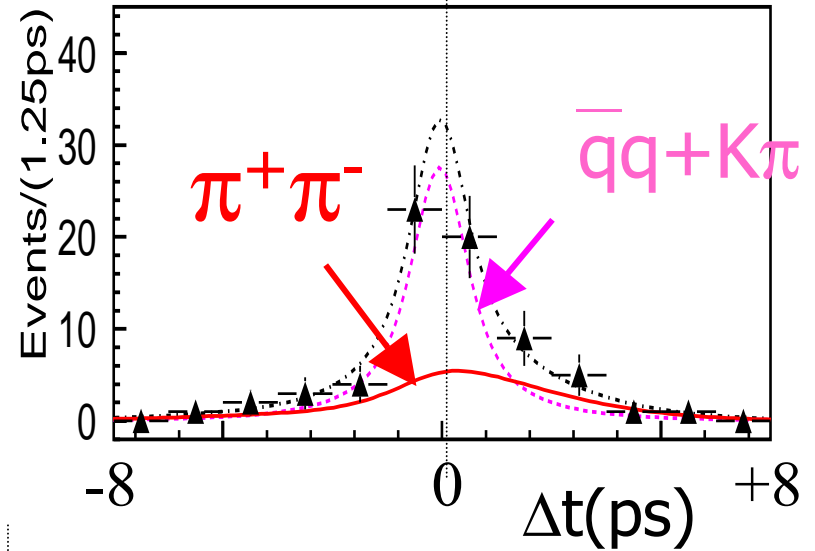
$$L_i = \int_{-\infty}^{\infty} d\Delta t' \{ (f_{\pi\pi} P_{\pi\pi}(\Delta t', q) + f_{K\pi} P_{K\pi}(\Delta t', q)) \cdot R_{sig}(\Delta t_i - \Delta t') \\ + f_{q\bar{q}} P_{q\bar{q}}(\Delta t') \cdot R_{q\bar{q}}(\Delta t_i - \Delta t') \}$$

Raw asymmetries

B^0 tagging



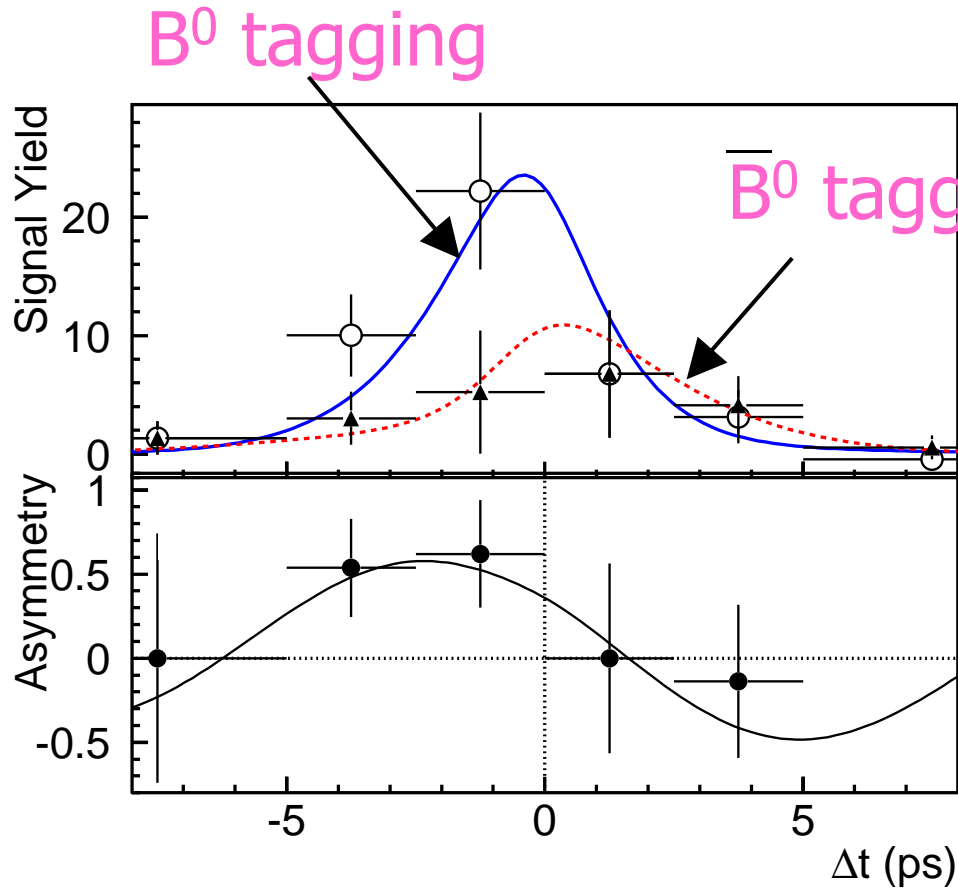
\bar{B}^0 tagging



$\pi^+\pi^- + \bar{q}q+K\pi$

More B^0 tags than \bar{B}^0 tags
 More B^0 tags with $\Delta t < 0$ than $\Delta t > 0$

CP fit results : $S_{\pi\pi}$ and $A_{\pi\pi}$



extracting $\pi^+\pi^-$
by subtracting $\bar{q}q+K\pi$

$$S_{\pi\pi} = -1.21 \quad \begin{matrix} +0.38 \\ -0.27 \end{matrix}$$

(stat.)

$$A_{\pi\pi} = +0.94 \quad \begin{matrix} +0.25 \\ -0.31 \end{matrix}$$

Each is 2.9σ from zero

Belle's ($S_{\pi\pi'}$, $A_{\pi\pi}$) is 1.2σ away from the physical boundary
Belle and Babar disagree by $> 2\sigma$

What (if any) can be wrong?

(The components of the present analysis are the same as those used to measure $\sin 2\phi_1$, τ_B , Δm_d , etc all in reasonable agreement with BaBar and PDG averages)

Possibilities

Are the backgrounds asymmetric?

- check with $K\pi$ and qq -sideband samples
- check with $D\pi$, $D\rho$ samples

Is vertexing wrong for $B \rightarrow h^+h^-$ decays?

- Measure Δm_d , τ_B for $B \rightarrow \pi\pi$ and $K\pi$ decays

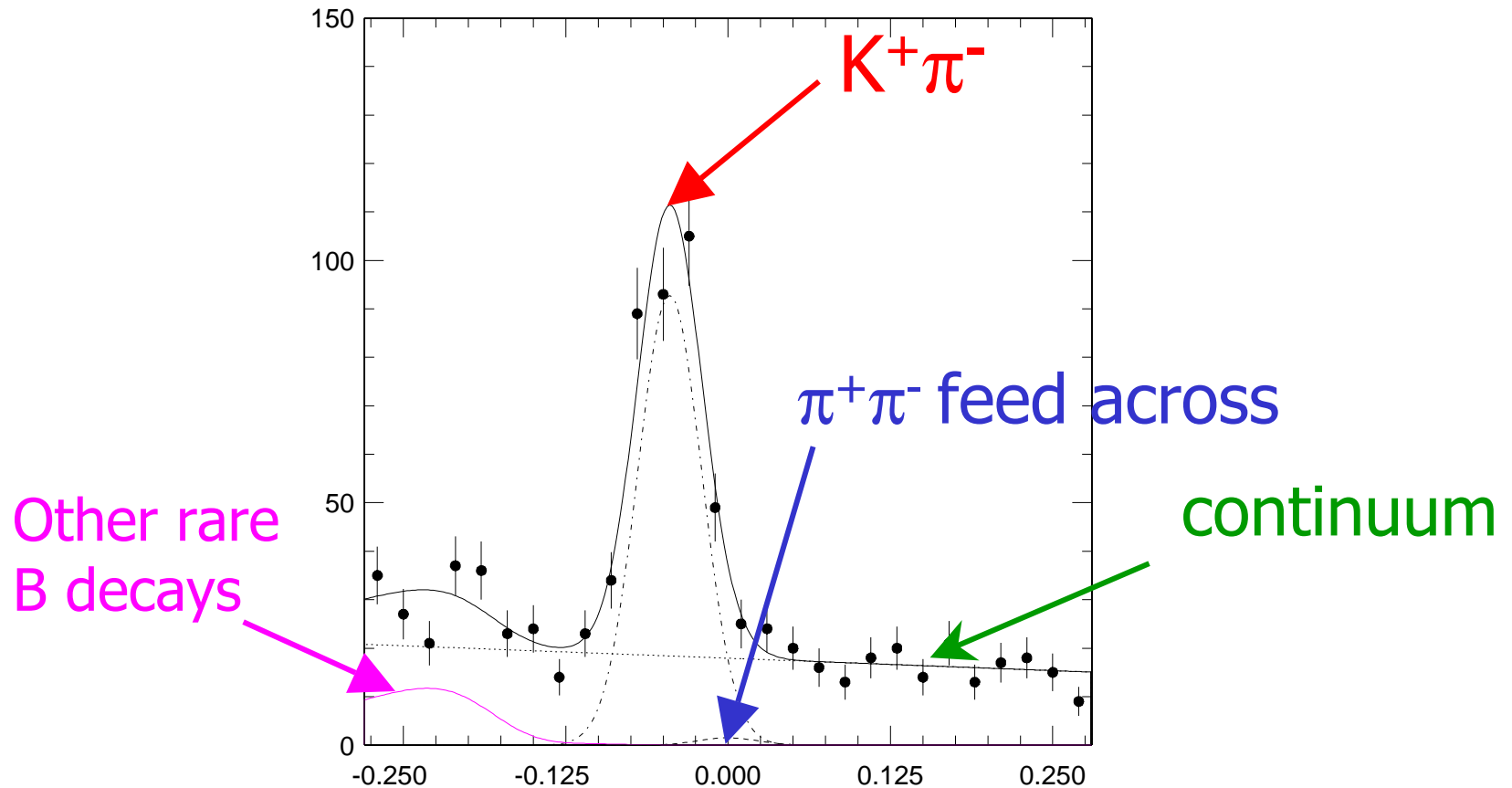
Do the likelihood values and errors make sense?

- Ensemble tests

Statistical fluctuations?

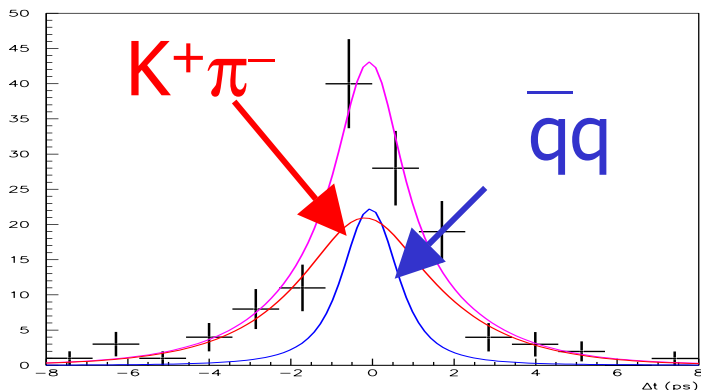
$K\pi$ samples

$$N(K^+\pi^-) = 289.5 \pm 21.5 \text{ events } (5.2 \pm 13.3 \pi^+\pi^- \text{ feed-across})$$



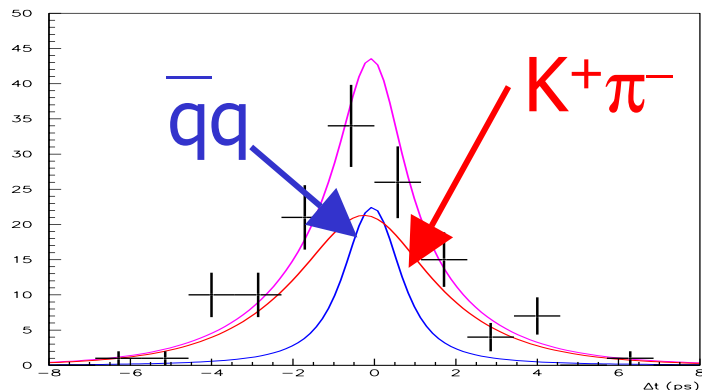
Asymmetry for $K^+\pi^-$

B^0 tagging

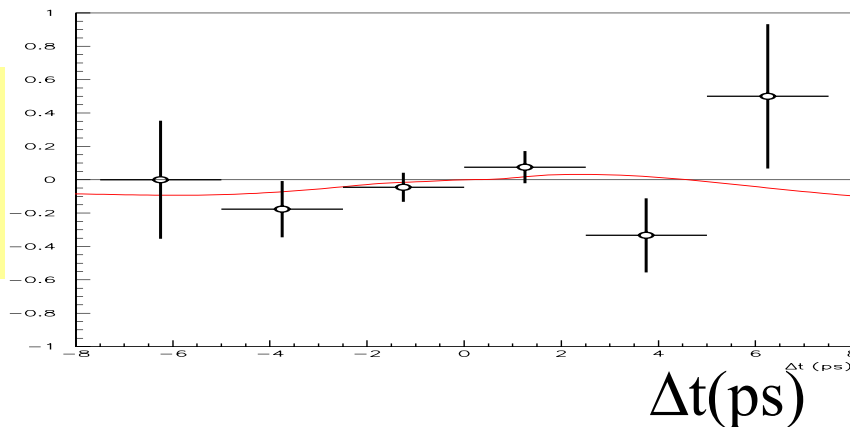


$\Delta t(\text{ps})$

\bar{B}^0 tagging



$\Delta t(\text{ps})$



Consistent
with null
asymmetry

$K^+\pi^-$	
$\tau_B(\text{ps})$	1.73 ± 0.15
S	0.15 ± 0.24
A	0.07 ± 0.17

PDG $\tau_B(\text{ps}) : 1.548 \pm 0.032 \text{ ps}$

Other control samples

Other **non-CP eigenstate** self-tagged modes

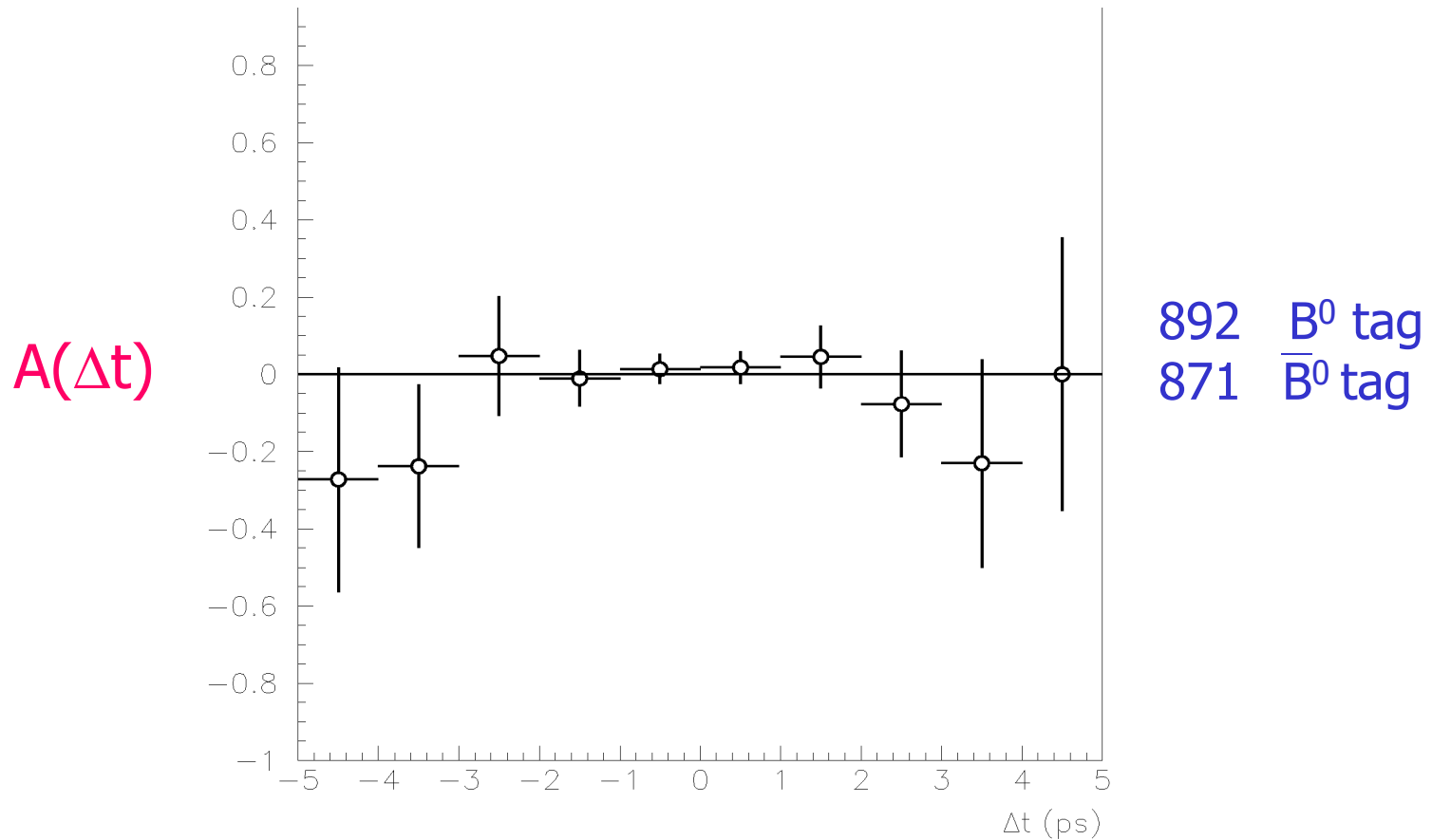
No asymmetry is expected.

⇒ **We find no asymmetries.**

PDG τ_B : 1.548 ± 0.032 ps

	$D^-\pi^+$	$D^{*-\pi^+}$	$D^{*-\rho^+}$
$\tau_B(\text{ps})$	1.64 ± 0.05	1.61 ± 0.05	1.68 ± 0.06
S	0.09 ± 0.09	0.13 ± 0.09	-0.04 ± 0.10
A	0.01 ± 0.06	-0.03 ± 0.06	-0.10 ± 0.07

Asymmetry for sideband data

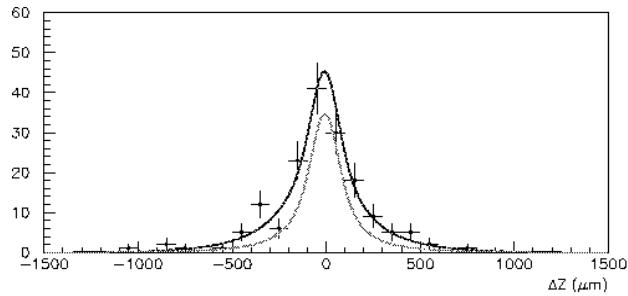


Consistent with no asymmetry

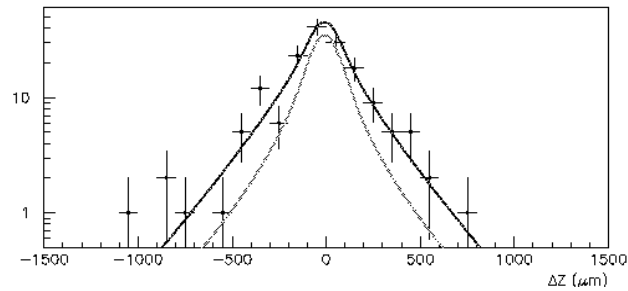
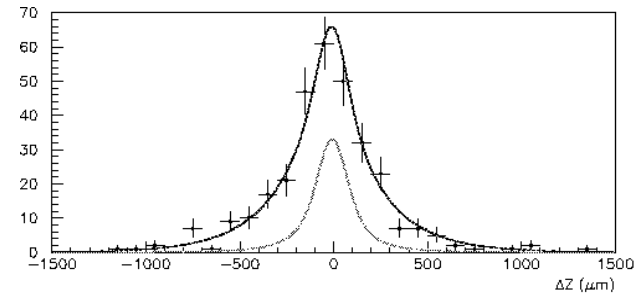
$B \rightarrow K\pi, \pi\pi$ lifetime validations

Lifetime measurements

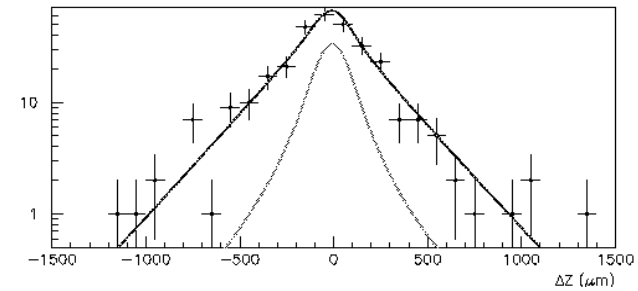
$B \rightarrow \pi\pi$



$B \rightarrow K\pi$



ΔZ

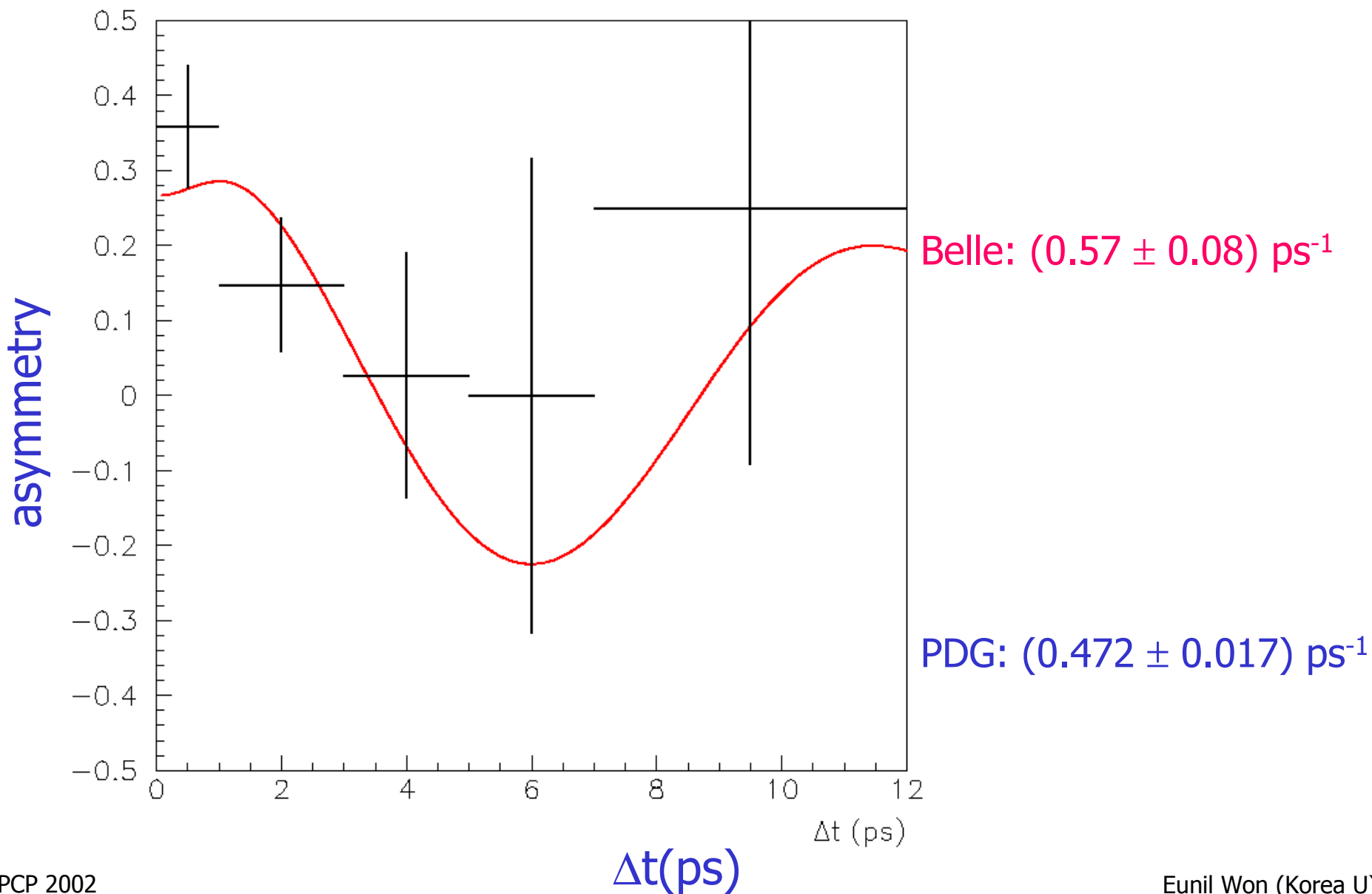


1.49 ± 0.21 ps

1.73 ± 0.15 ps

PDG: 1.548 ± 0.032 ps

Δm_d from $B \rightarrow K\pi$



Possibilities revisited

Are the backgrounds asymmetric?

- $K\pi$, qq-sideband and $D\pi/\rho$ samples show null asymmetries

Is vertexing wrong for $B \rightarrow h^+h^-$ decays?

- Lifetime for $B \rightarrow \pi\pi$ and $K\pi$ samples are OK
- Δm_d for $B \rightarrow K\pi$ is OK

Do the likelihood values and errors make sense?

- Ensemble tests show no anomaly

Statistical fluctuations?

- Most likely at this moment

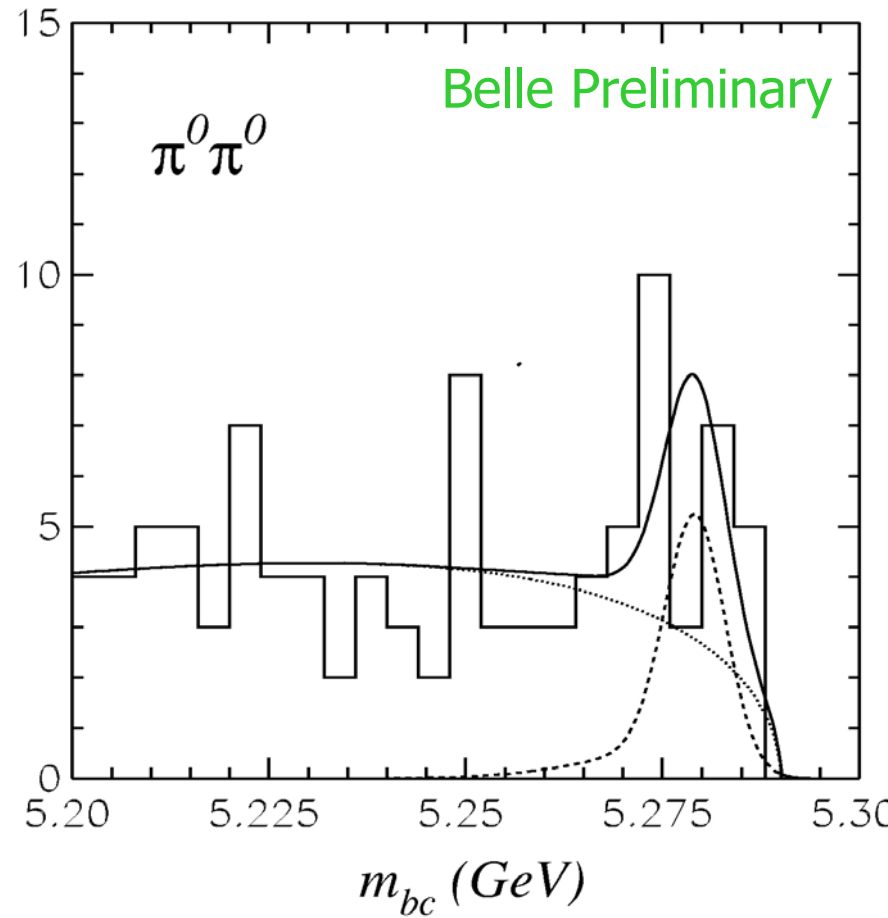
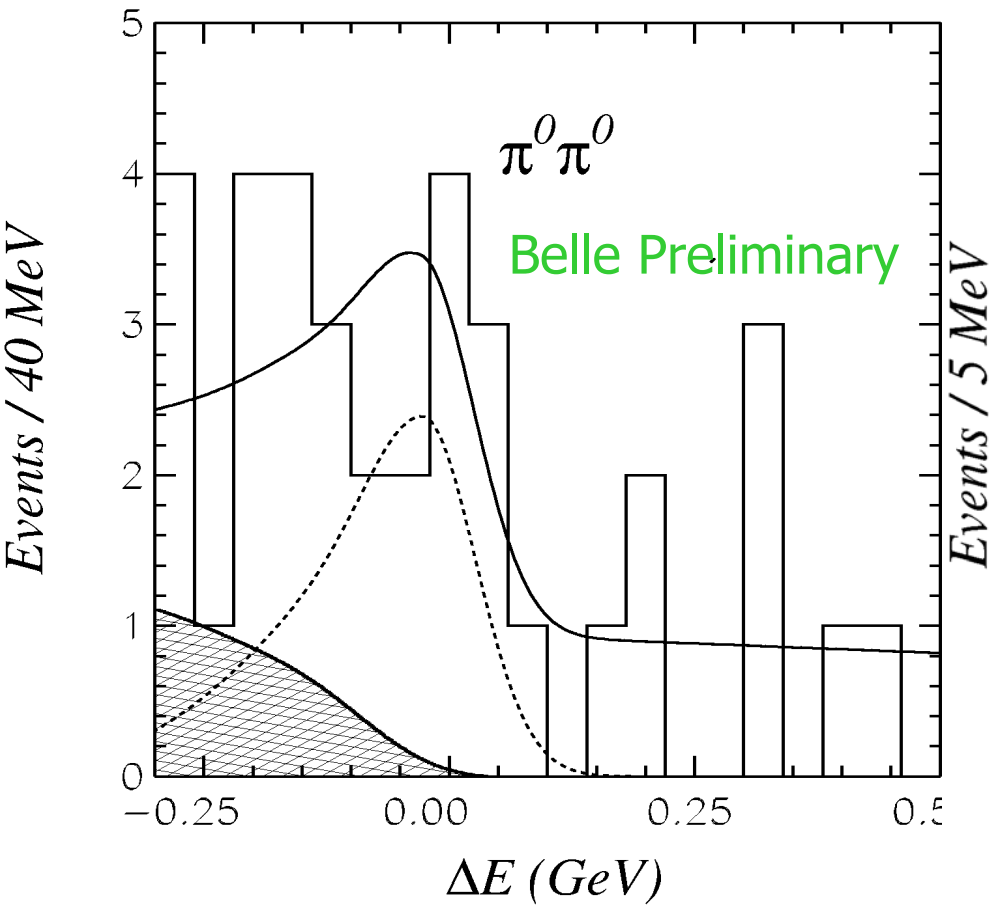
Systematic error estimation

Item	$\delta S(-)$	$\delta S(+)$	$\delta A(-)$	$\delta A(+)$
Background frac.	-0.088	+0.077	-0.040	+0.057
Wrong tag	-0.071	+0.047	-0.052	+0.058
vertexing	-0.049	+0.059	-0.030	+0.017
physics	-0.039	+0.040	-0.012	+0.017
Fit bias	-0.024	+0.110	-0.051	+0.030
Background shape	-0.015	+0.015	-0.003	+0.004
Resolution function	-0.012	+0.012	-0.008	+0.008
Total	-0.133	+0.160	-0.090	+0.090

At present, statistical error is 2~3 times larger than systematic

What's going on with $B \rightarrow \pi^0 \pi^0$?

Data sample: 29 fb⁻¹



2.2 σ effect at this moment

$\text{Br}(B \rightarrow \pi^0 \pi^0) < 0.56 \times 10^{-5}$ at 90% CL

Summary

CP violating asymmetry parameters were measured in $B \rightarrow \pi^+ \pi^-$ decay using 42 fb^{-1} of data

$$S_{\pi\pi} = -1.21 \begin{array}{l} +0.38 \\ -0.27 \end{array} \begin{array}{l} +0.16 \\ -0.13 \end{array}$$

(stat.) (syst.)

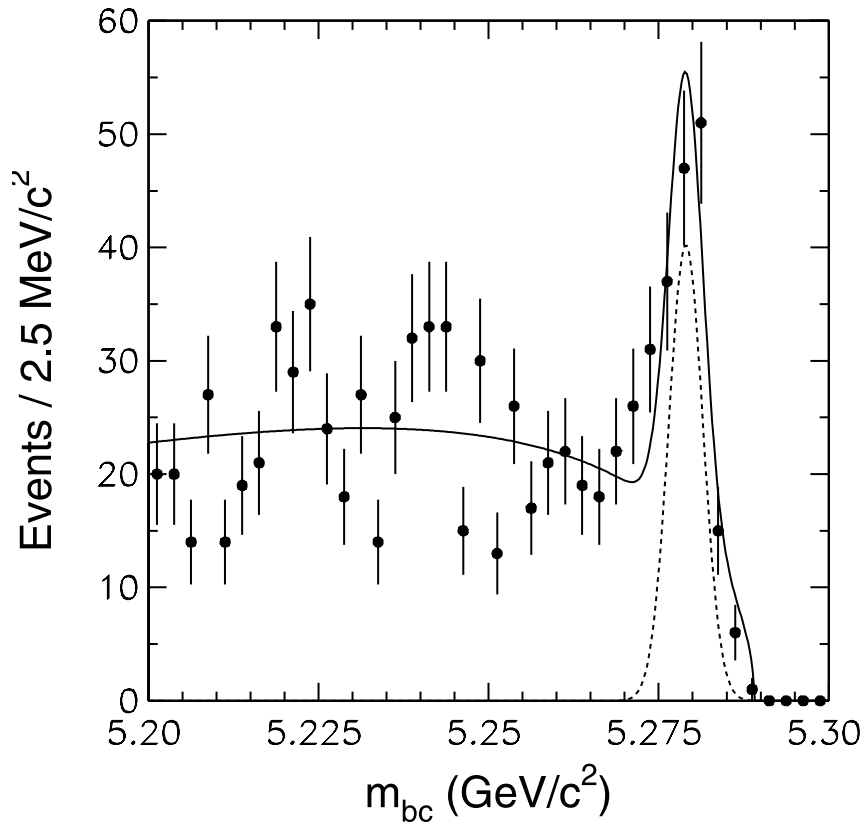
$$A_{\pi\pi} = +0.94 \begin{array}{l} +0.25 \\ -0.31 \end{array} \pm 0.09$$

Both are 2.9σ away from zero

$\text{Br}(B \rightarrow \pi^0 \pi^0)$ could be within reach in near future

Backup Slides for Questions

Signal Yield for $B \rightarrow \pi^+ \pi^-$



$$|\Delta E| < 0.067 \text{ GeV}$$

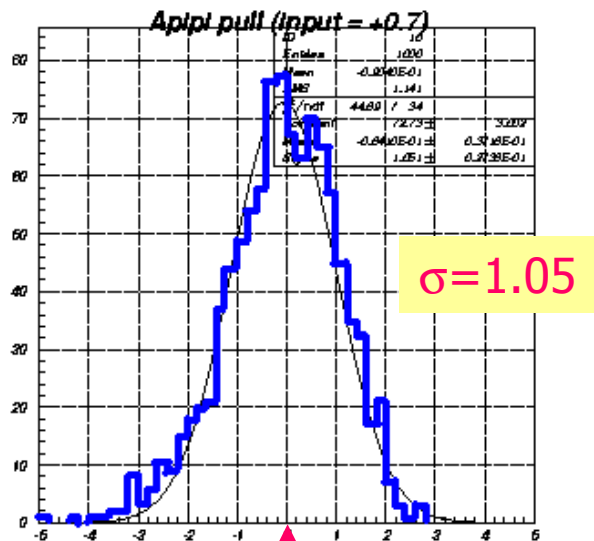
Peak in m_{bc} includes both $\pi\pi$ and $K\pi$ components

Fit result in m_{bc}
 101.6 ± 13.1
(consistent with ΔE fit
result: 101.9 ± 18.6)

Beam energy constrained mass

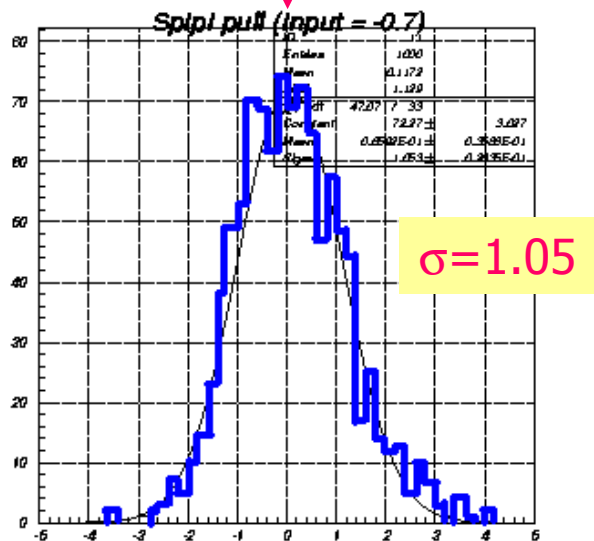
Ensemble tests: Pulls and Errors

$A_{\pi\pi}$

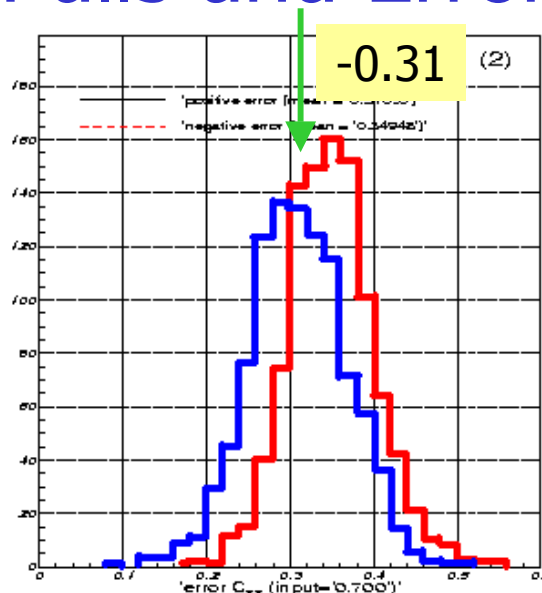


Pull = 0

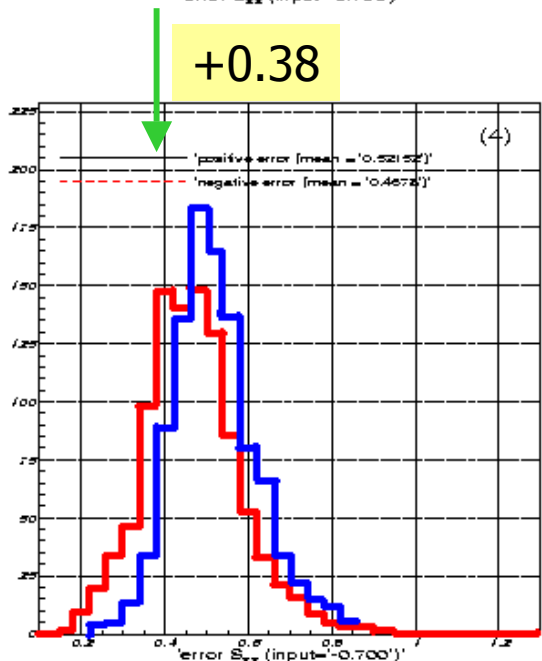
$S_{\pi\pi}$



Pulls



Input $A_{\pi\pi} = 0.7$
 $S_{\pi\pi} = -0.7$



5.4% of the time
MC expects smaller
+ errors

Errors