

# CP violation and cosmology

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- CP and the origin of baryon asymmetry

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- models of baryogenesis and the sources of CP violation

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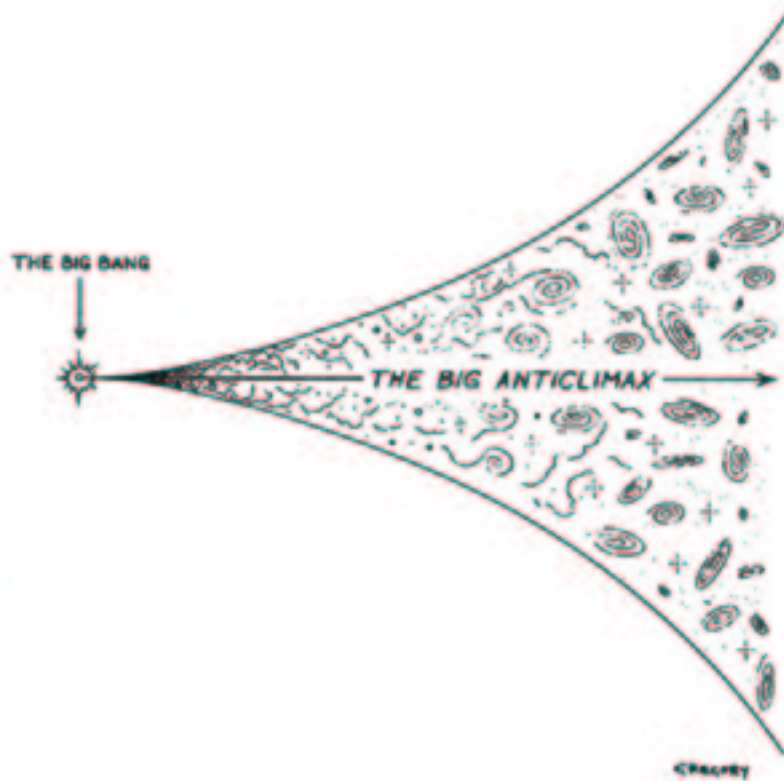
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COSMOLOGY MARCHES ON



# CP violation and baryogenesis





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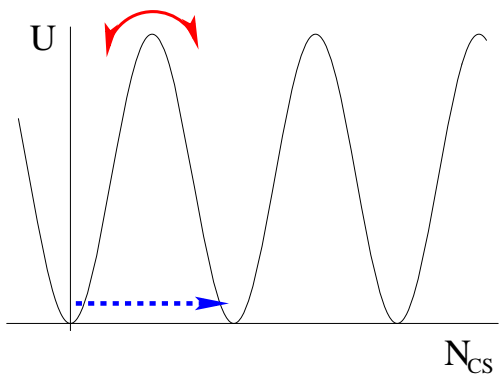
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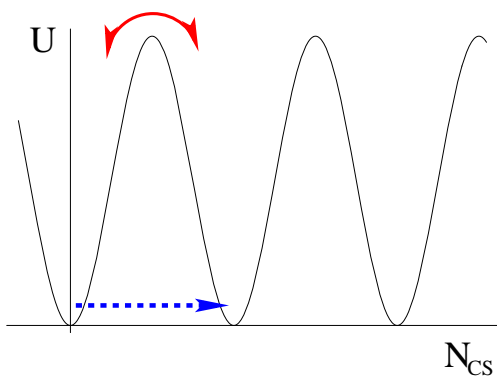
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All three conditions are satisfied in the Standard Model (to some extent)

- **B violation**



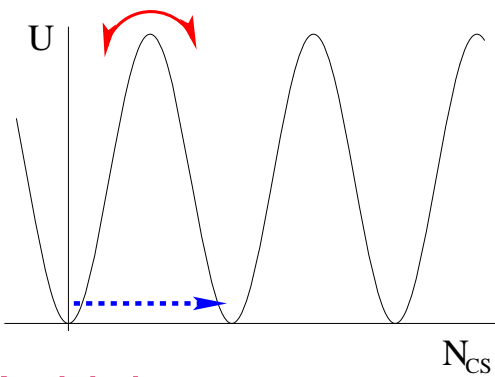
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Instantons violate  $B$  with  
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At high temperature transitions occur via **sphalerons**, over the barrier.  
 No suppression!

## In the Standard Model

- B violation
- B, C, CP not conserved
- universe out of equilibrium at EW phase transition

## ELECTROWEAK BARYOGENESIS!

[Kuzmin, Rubakov, Shaposhnikov '85]

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Can SUSY help? (More scalar fields, more parameters...)

# Thermal electroweak baryogenesis in the MSSM

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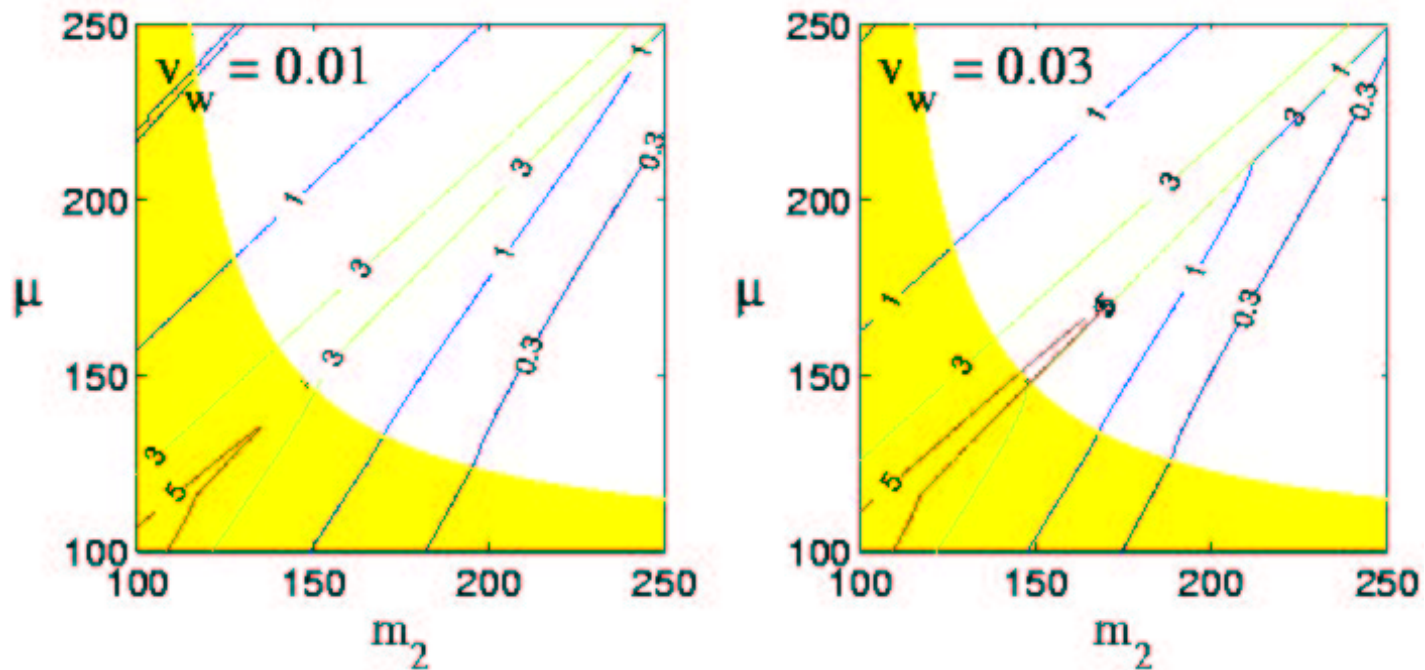
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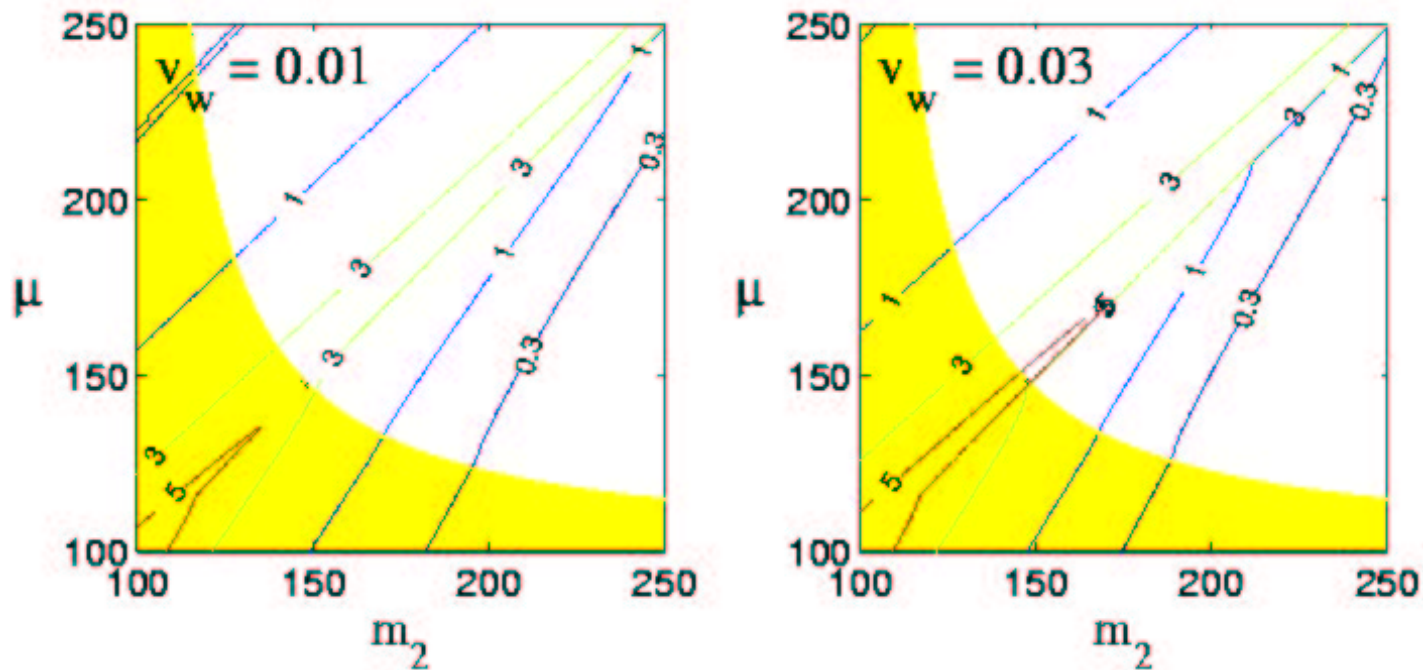
$$\bar{\psi}_R M_\chi \psi_L = (\bar{\tilde{w}}^+, \bar{\tilde{h}}_2^+)_R \begin{pmatrix} m_2 & gH_2(x) \\ gH_1(x) & \mu \end{pmatrix} \begin{pmatrix} \tilde{w}^+ \\ \tilde{h}_1^+ \end{pmatrix}_L + \text{h.c.}$$

$m_2$  and  $\mu$  are complex  $\Rightarrow$  spatially varying complex phases in the wall

Contours of baryon asymmetry in units  $10^{-10}$  [Cline, Joyce, Kainulainen]. Shaded limits are excluded by LEP2 limits on chargino mass,  $m_{\chi^\pm} > 104$  GeV.



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Assumptions:  $\tan \beta \approx 3$ ; “optimal” wall velocity  $v_w \approx 0.02$ ; very thin wall,  $l_w \approx 6/T$ .

**EW baryogenesis in the MSSM** will be ruled out with (any!) improvement of bounds on the lightest Higgs mass, and also if the light stop is ruled out. Alternatively, MSSM may soon be discovered.

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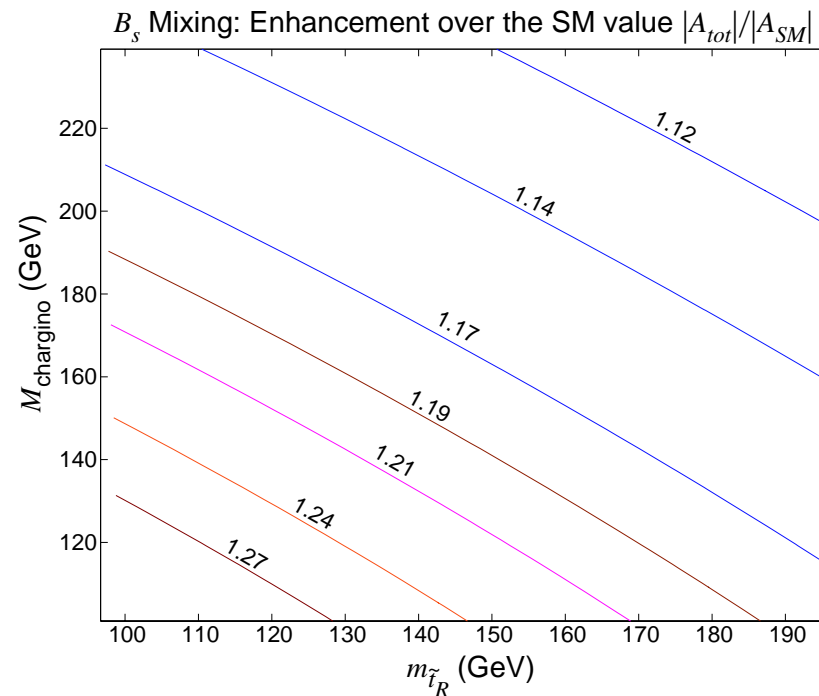
Enhancement of  $B_s$  mixing  
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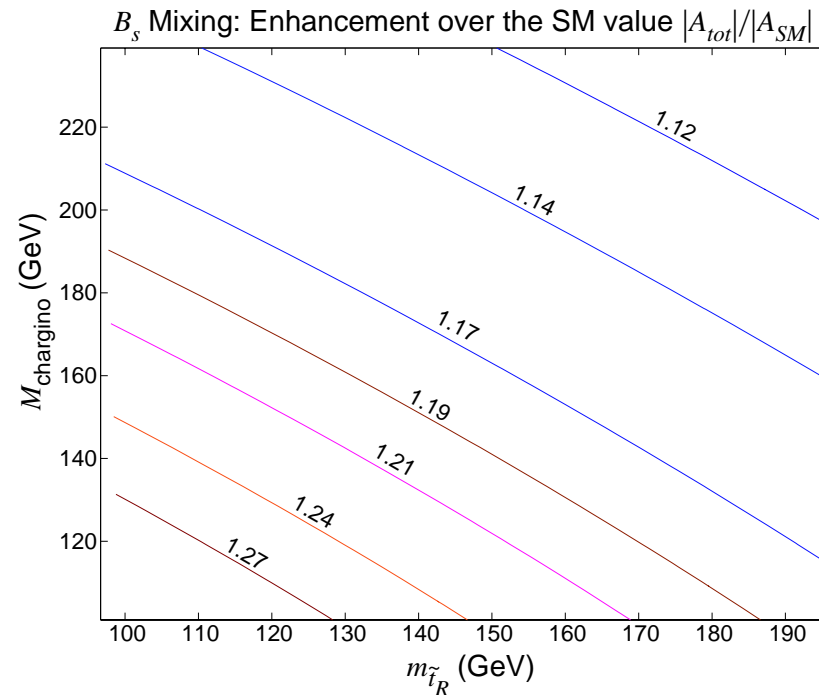


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But need to know  $V_{ub}$  to **5-10%**  
and  $\sin 2\beta$  to **a few %**



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**CP violation in the neutrino mass matrix?** [Kayser]

# Transient CP violation



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- electroweak baryogenesis at preheating

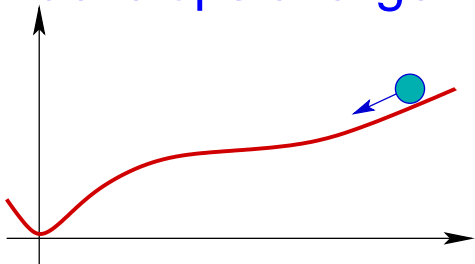
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at the end of inflation  
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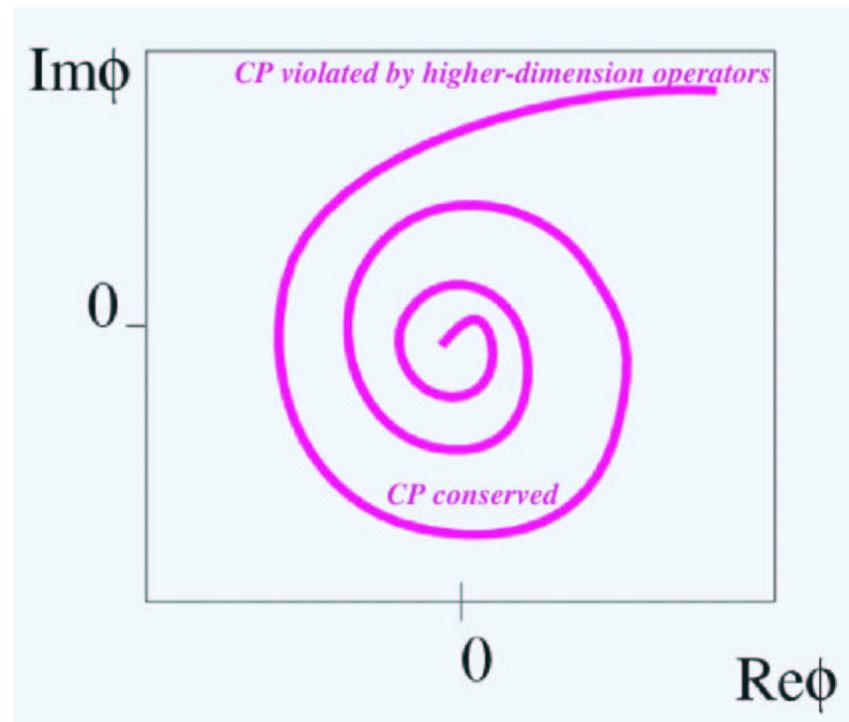
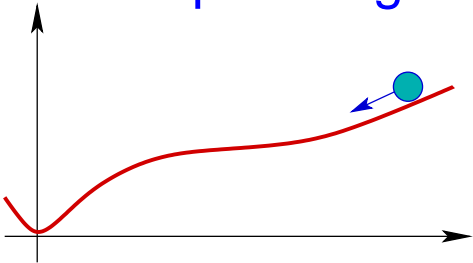
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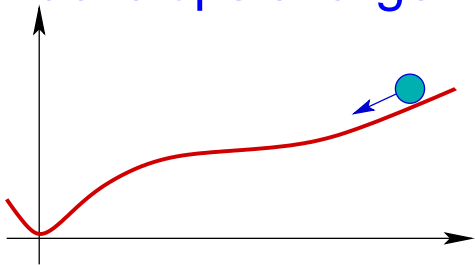
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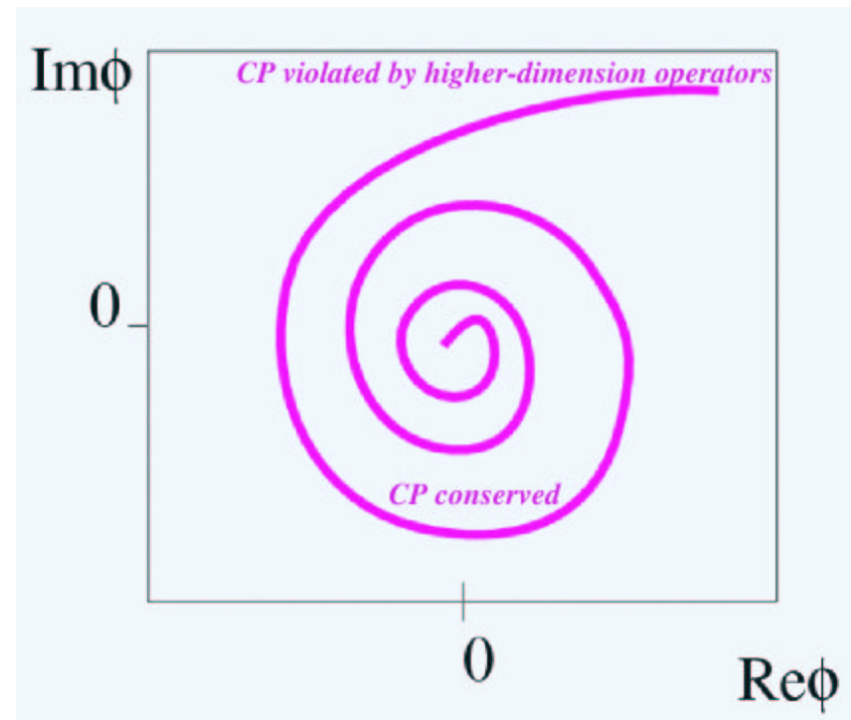


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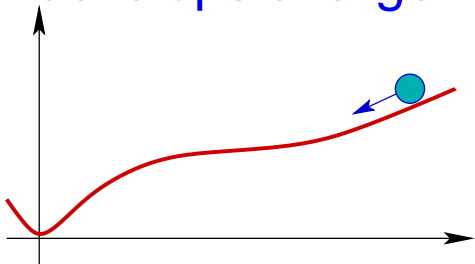
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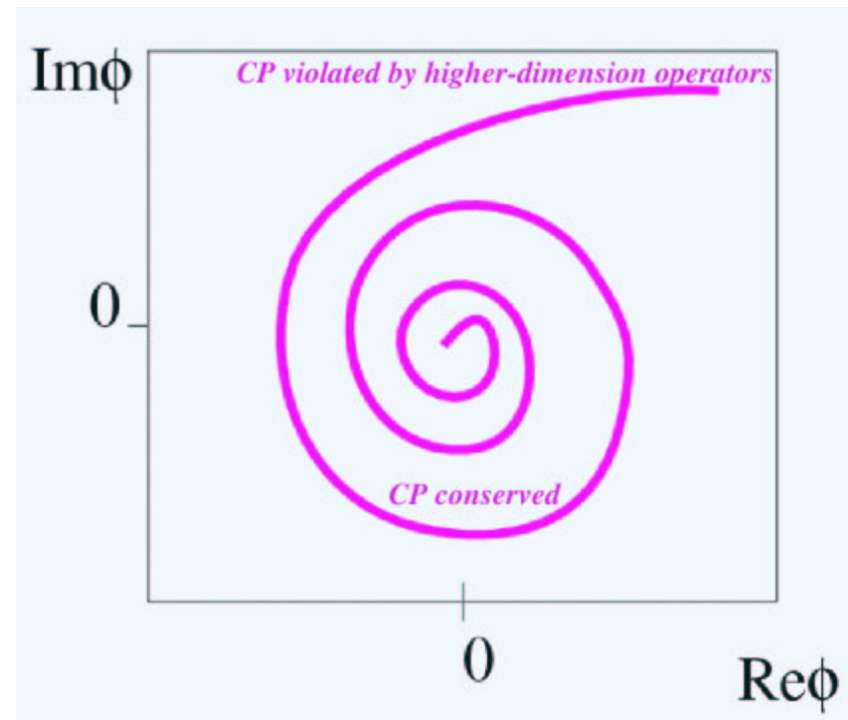
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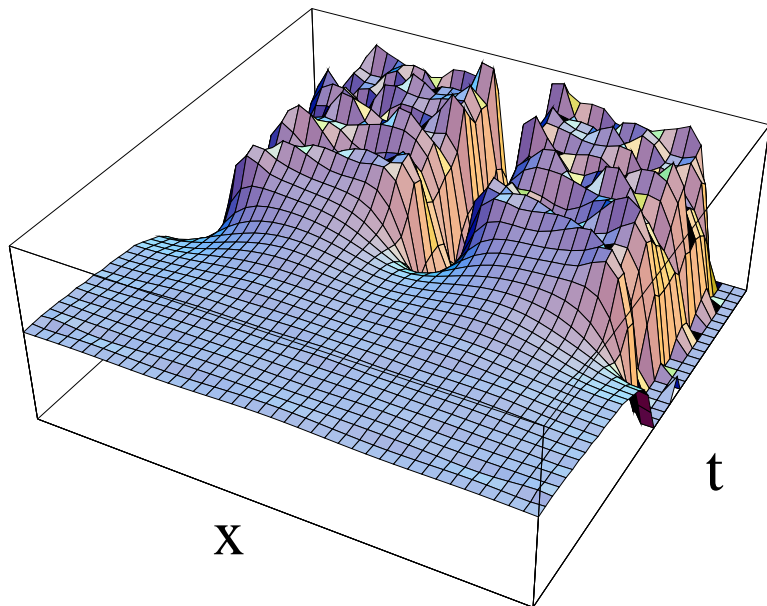


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**CP violation seed – from high-scale physics**

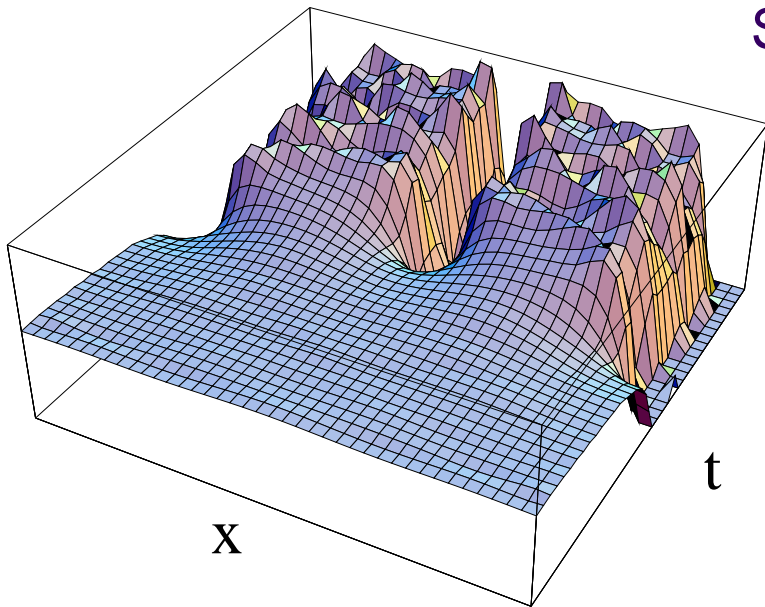


## Fragmentation of Affleck-Dine condensate can produce Q-balls

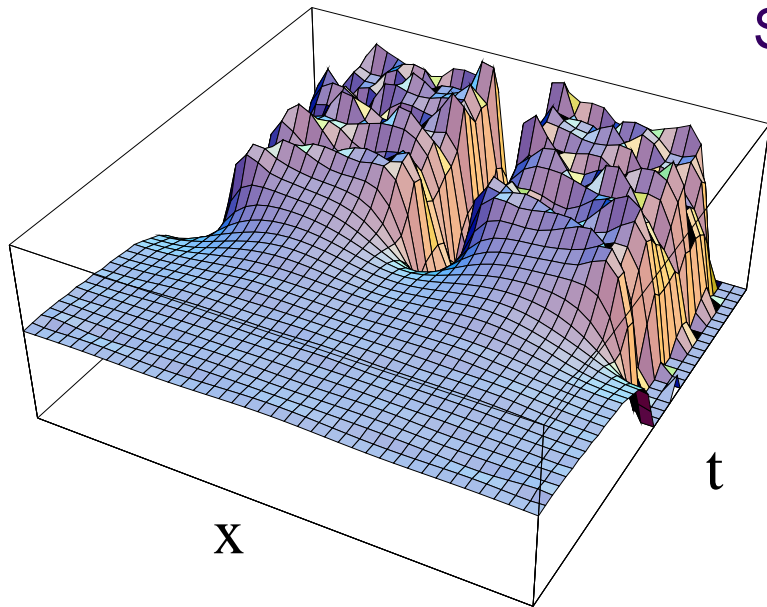


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SUSY Q-balls may be stable or unstable

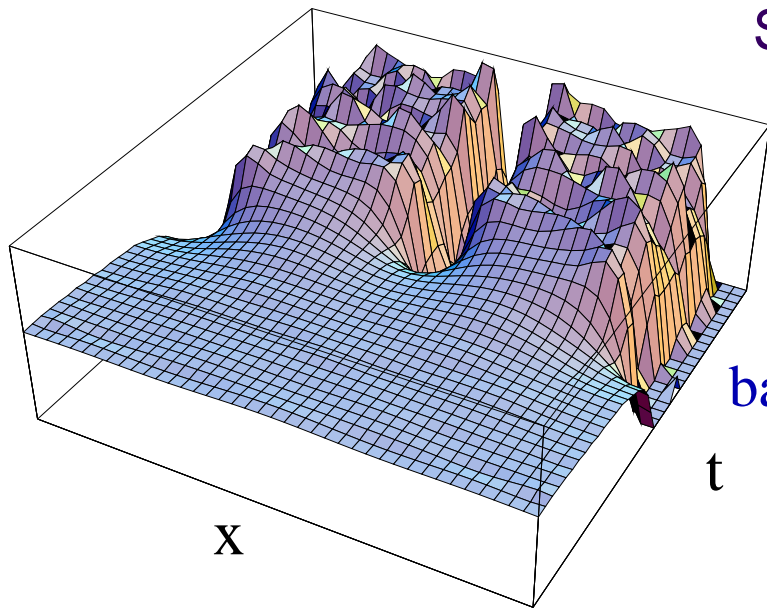


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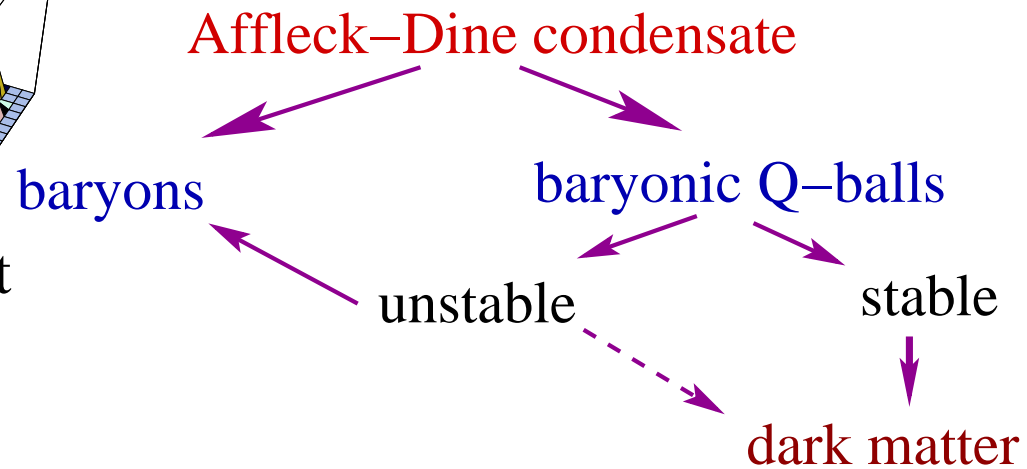


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[AK, Shaposhnikov]

# EW baryogenesis at preheating

## **EW baryogenesis at preheating**

**Inflation probably took place in the early universe**

## EW baryogenesis at preheating

### Inflation probably took place in the early universe

At the end of inflation, the problems disappear:

- **Preheating** following inflation is a period when the universe is very far from thermal equilibrium
- Time-dependent scalar condensate, coherent on large scales, creates a **CP non-invariant background** sufficient for generating  $\eta \sim 10^{-10}$ .
- Wash-out of baryon asymmetry can be prevented if the reheat temperature is below electroweak transition temperature



⇒ **EW baryogenesis at preheating**

Krauss, Trodden  
García-Bellido, Grigoriev,  
AK, Shaposhnikov

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Can **B-violating transitions** similar to sphalerons take place during reheating?

**-Yes.** Preheating pumps energy into long-wavelength modes that make sphaleron-like transitions possible.

**Parametric resonance:**

Equation of motion for the Higgs has growing solutions:

$$\ddot{\phi}_k + [k^2 - M^2 + 3\lambda\langle\phi^2\rangle + g^2\sigma^2(t)]\phi_k = 0$$

**Energy flow:** Inflaton  $\rightarrow$  Higgs  $\rightarrow$  W,Z,...sphalerons?

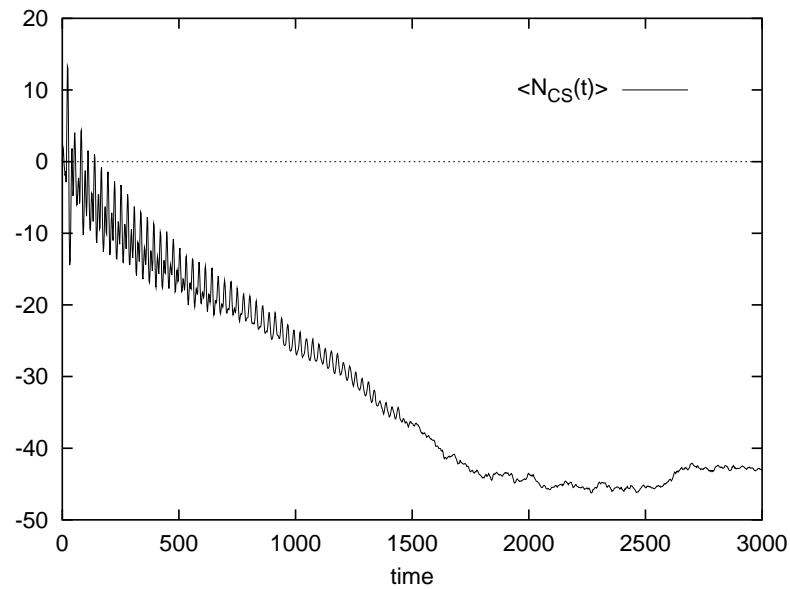
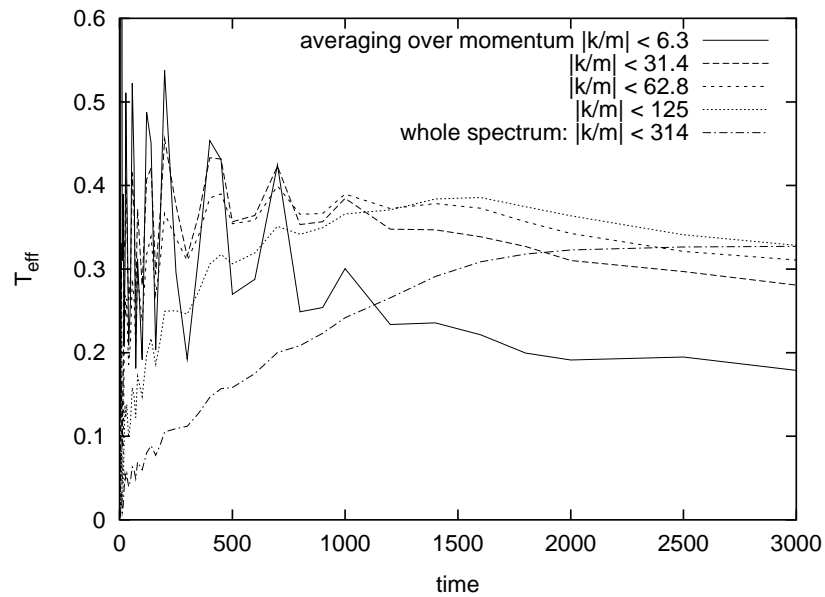
**Estimate:**  $\Gamma_{\text{sph}} \approx \alpha_W^4 T_{\text{eff}}^4$  ( $T_{\text{eff}}$  from the low-energy modes)

This estimate agrees with numerical simulations in 1+1 dimensions

García-Bellido, Grigoriev,  
AK, Shaposhnikov  
Phys.Rev.D60:123504,1999

Also, approximate analytical description [\[AK, Cornwall\]](#)

## Numerical model



U(1) gauge field  $A_\mu$  plus Higgs field  $\phi$ . C,CP violation introduced by term  $\kappa \phi^* \phi \epsilon_{\mu\nu} F^{\mu\nu}$ . In 1+1, the analogue of anomaly is  $\partial_\mu j_F^\mu = -\frac{e}{4\pi} \epsilon_{\mu\nu} F^{\mu\nu}$ , where  $j_F^\mu = \bar{\psi} \gamma^\mu \psi$

## possible seeds of CP violation

- **strong CP violation in the standard Model**, which vanishes in the present vacuum, may be inducted at the time of preheating and may provide a sufficient CP-violating background for baryogenesis via the coupling

$$\eta' \frac{1}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

- **CP violation in the Higgs sector**
- **higher derivative terms**

## Spontaneous baryogenesis at preheating

**Cohen, Kaplan and Nelson:** in a two Higgs doublet model, the Higgs field  $H(x)$  in the bubble wall breaks CP. Similar (but more effective!) scenario at preheating:  $H(x) \rightarrow H(t)$  [\[Cornwall,Grigoriev,AK\]](#) .

Higgs potential:

$$\begin{aligned}
 V(H_1, H_2) &= \lambda_1(H_1^\dagger H_1 - v_1^2)^2 \\
 &+ \lambda_2(H_2^\dagger H_2 - v_2^2)^2 \\
 &+ \lambda_3[(H_1^\dagger H_1 - v_1^2) + (H_2^\dagger H_2 - v_2^2)]^2 \\
 &+ \lambda_4[(H_1^\dagger H_1)(H_2^\dagger H_2) - (H_1^\dagger H_2)(H_2^\dagger H_1)] \\
 &+ \lambda_5[\text{Re}(H_1^\dagger H_2) - v_1 v_2 \cos \xi]^2 \\
 &+ \lambda_6[\text{Im}(H_1^\dagger H_2) - v_1 v_2 \sin \xi]^2
 \end{aligned}$$



At finite temperature, all  $\lambda_k$  and  $v_i$  receive thermal corrections and depend on the temperature. During preheating the Higgs fields move along classical trajectory

$$H_i = \rho_i(t) e^{i\theta_i(t)}$$

that satisfies the equations of motion

$$\begin{aligned} \ddot{\theta}_i + 3h\dot{\theta}_i + \frac{\dot{\rho}_i}{\rho_i} + \rho_i^{-1} \frac{\partial V}{\partial \theta_i} &= 0, \\ \ddot{\rho}_i + 3h\dot{\rho}_i - \dot{\theta}_i^2 \rho_i + \frac{\partial V}{\partial \rho_i} &= 0, \end{aligned}$$

During preheating, the Higgs fields change from their zero-temperature values at the end of inflation to some temperature-dependent VEV:

$$\begin{aligned} \text{at } T &= 0, \quad \rho_i = v_i; \\ \text{at } T &= T_R, \quad \rho_i = v_i(T_R). \end{aligned}$$

At the same time, the phase  $\theta$  also changes:

$$\begin{aligned} \theta(0) &\equiv \theta_1(0) - \theta_2(0) = \xi, \\ \theta(T_R) &\equiv \theta_1(T_R) - \theta_2(T_R) = \xi(T_R). \end{aligned}$$

The time derivative of  $\theta$  serves as a chemical potential for the fermion number because of an effective coupling

$$(\partial_0 \theta) [\bar{\psi} \gamma^\mu \psi + \dots]$$

B violation much faster than thermalization  $\Rightarrow$  baryon number has time to equilibrate to min of free energy

The effective chemical potential  $\mu_B$  is proportional to  $\dot{\theta}$ , and the equilibrium value of baryon asymmetry is

$$n_B \sim \langle \dot{\theta} \rangle T_R^2 \sim 10^{-10} T_R^3 \left( \frac{10^{-5} t_H}{t_R} \right)$$

where  $t_R$  is the time of reheating and  $t_H$  is the Hubble time at the electroweak scale

Cohen, Kaplan, Nelson:  $H(x)$  and  $n_B$  far from equilibrium value. CGK:  $H(t)$  and  $n_B$  close to instantaneous equilibrium

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Experiment:  $|\bar{\theta}| \ll 10^{-10}$  !



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Additional U(1) symmetry, **Peccei-Quinn symmetry** is spontaneously broken by instantons  $\Rightarrow$  axion has small mass.

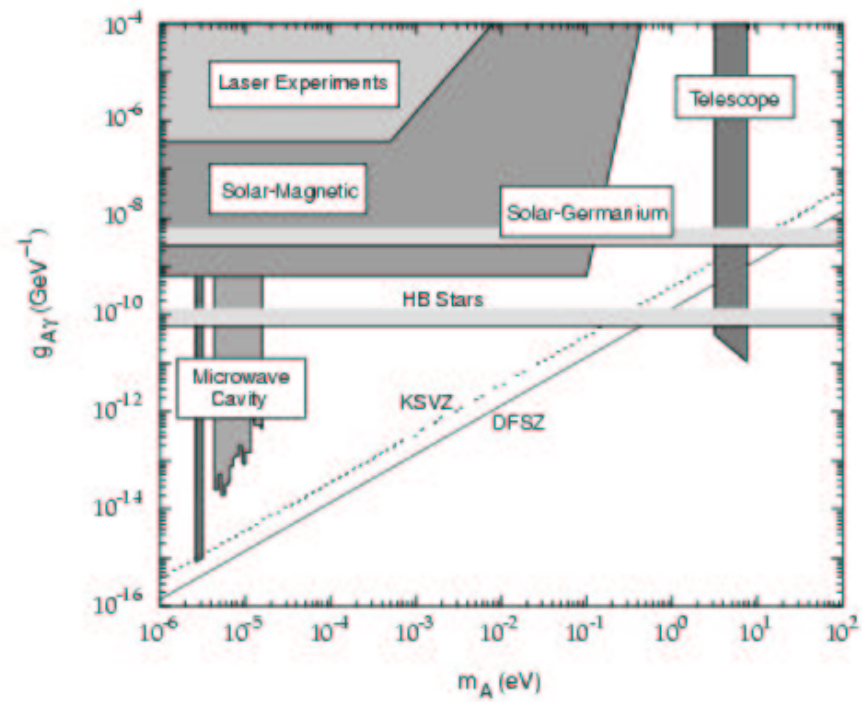
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**Axion is a weakly interacting particle**  $\Rightarrow$  **dark matter**

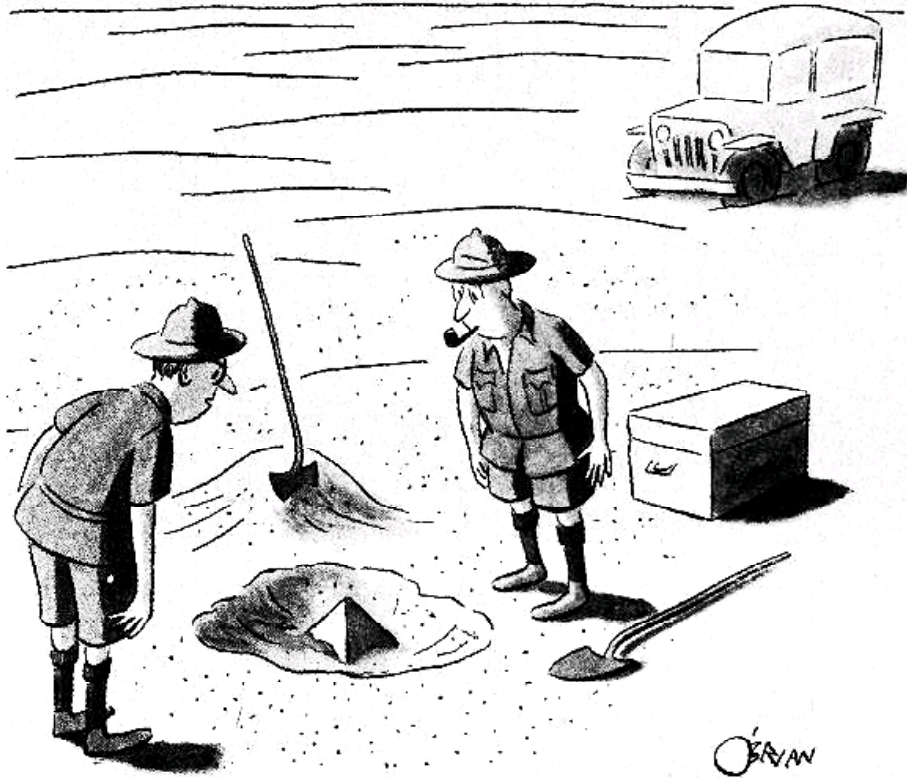
# Axion dark matter



# Conclusion

**CP violation may be the reason we exist... if it is big enough**

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*This could be the greatest discovery of the century.  
Depending, of course, on how far down it goes.*