

# Charm Weak Decays in the SM and Beyond

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## Outline

- Semileptonic Charm Decays: The impact of precision measurements in exclusive semileptonic  $D$  decays.
- $D^0 - \bar{D}^0$  Mixing: How close is the Long Distance wall?
- Rare Charm Decays in the Standard Model:
  - Radiative Decays:  $D \rightarrow X\gamma$ .
  - Semileptonic Modes:  $D \rightarrow \pi\ell^+\ell^-$ ,  
 $D\rho\pi\ell^+\ell^-$ , ...
- New Physics: Effects of Supersymmetry.
  - Non-universal soft term in SUSY with  $R_P$  conservation.
  - Effects of  $R_P$  violation.
- Conclusions

## $D$ Semileptonic Decays

- Why do we need precision measurements of exclusive semileptonic decays?  $D \rightarrow K^{(*)} \ell \nu$  and  $D \rightarrow \pi(\rho) \ell \nu$ .
- Study of hadronic physics at  $m_c$ . Form-factor normalization and  $q^2$  dependence.
- Impact on  $B$  physics I: Comparison with  $B \rightarrow \pi \ell \nu$  and  $B \rightarrow \rho \ell \nu$ . Test of  $HQET$ : are  $1/M_Q$  large?  $V_{ub}$ ? New Physics: same form-factors for rare decays  $B \rightarrow K^* \ell^+ \ell^-$ ,
- Impact on  $B$  physics II: Are the  $SU(3)$  corrections under control?
- Impact on  $B$  physics III: Precision SL and Leptonic decays of charm will test Lattice calculations  $\Rightarrow$  Lattice predictions of  $B \rightarrow \pi \ell \nu$ ,  $B \rightarrow K^* \ell^+ \ell^-$ , etc.
- $|V_{cd}|$ .

## Heavy Quark Symmetry (*Isgur-Wise '89*)

In the  $m_Q \rightarrow \infty$  limit ( $m_Q \gg \Lambda_{\text{QCD}}$ ),

- *Flavor Symmetry*: Light degrees of freedom can't tell the heavy flavor.  
 $\Rightarrow b \longleftrightarrow c$ . Applications: extraction of  $|V_{cb}|$  from inclusive and exclusive semileptonic  $b \rightarrow c\ell\nu$  decays. Works best at low recoil (Luke's Theorem at zero recoil).
- *Spin Symmetry*: Spin decouples in the  $m_Q \rightarrow \infty$  limit. E.g.:  $\Delta m_B \equiv m_{B^*} - m_B \rightarrow 0$ .

But for **Heavy**  $\rightarrow$  **Light** decays applications are more limited:

$$\begin{array}{ccccc} D & \longrightarrow & K^* \ell \nu & & \\ SU(2)_F & \updownarrow & \updownarrow & SU(3) & \\ B & \longrightarrow & \rho \ell \nu & & \end{array}$$

## Heavy Quark Symmetry and $H \rightarrow \pi \ell \nu$

- One form-factor:

$$\langle \pi(k) | (\bar{q} \gamma_\mu c) | D(p) \rangle = f_+(q^2) (P + k)_\mu + f_-(q^2) (P - k)_\mu$$

But if  $m_\ell \rightarrow 0$

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cd}|^2 k^3 |f_+(q^2)|^2$$

$\Rightarrow$  precision measurement of  $d\Gamma/dq^2$  in  $D \rightarrow \pi \ell \nu$  gives  $f_+(q^2)$ .

- $B$  Physics Impact: Heavy Quark Symmetry  $\Rightarrow$   $B \rightarrow \pi \ell \nu$  given by same  $f_+$  up to heavy mass scaling:

$$\frac{f_+^{B \rightarrow \pi}(v.k)}{f_+^{D \rightarrow \pi}(v.k)} = \left( \frac{\alpha_s(m_b)}{\alpha_s(m_c)} \right)^{-6/25} \sqrt{\frac{m_B}{m_D}} \times \left\{ 1 + \mathcal{C} \left( \frac{1}{m_b} - \frac{1}{m_c} \right) + \dots \right\}$$

with  $v.k = E_\pi$  in the heavy meson rest frame.

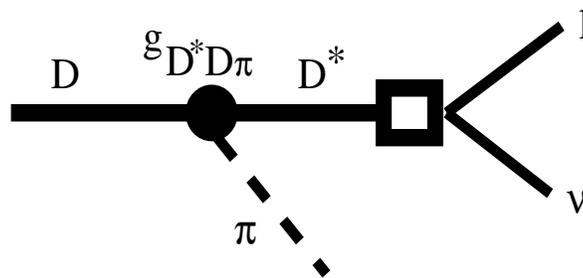
$$\Rightarrow E_\pi < 1 \text{ GeV}$$

Chiral Symmetry helps at low recoil (*M. Wise;*

*G.B. and J. Donoghue '92*) • Chiral Perturbation Theory for Heavy Hadrons (ChPTHH) predicts  $f_+(v.p_\pi)$  at low  $p_\pi$  to be

$$f_+(v.p_\pi) = \frac{g_{D^*D\pi} f_{D^*}}{2f_\pi} \left( \frac{m_D - v.p_\pi}{v.p_\pi + \Delta} \right) + \frac{f_D}{2f_\pi}$$

with  $\Delta_D \equiv m_{D^*} - m_D$ . This is dominated by the  $D^*$  pole contribution.



This is valid to Next-to-Leading Order in the  $1/M$  expansion. (*G.B., Z. Ligeti, M. Neubert and Y. Nir '93*)

## SU(3) Breaking

- How large is  $SU(3)$  breaking in semileptonic form-factors?  
Relevant e.g. for  $B \rightarrow \pi \ell \nu \leftrightarrow B \rightarrow K \ell^+ \ell^-$ .
- Compare  $D \rightarrow \pi \ell \nu$  to  $D \rightarrow K \ell \nu$ . What can we expect? The lesson from decay constants:



$$\frac{f_{D_s}}{f_D} - 1 \simeq \frac{(1 + 3g_{D^* D \pi}^2)}{32\pi^2 f_\pi^2} \left\{ m_K^2 \log \left( \frac{m_K^2}{\mu^2} \right) + m_\eta^2 \log \left( \frac{m_\eta^2}{\mu^2} \right) \right\}$$

Which gives  $f_{D_s}/f_D \simeq 1.10$ . (*B. Grinstein, E. Jenkins, A. Manohar and M. Wise '92*)

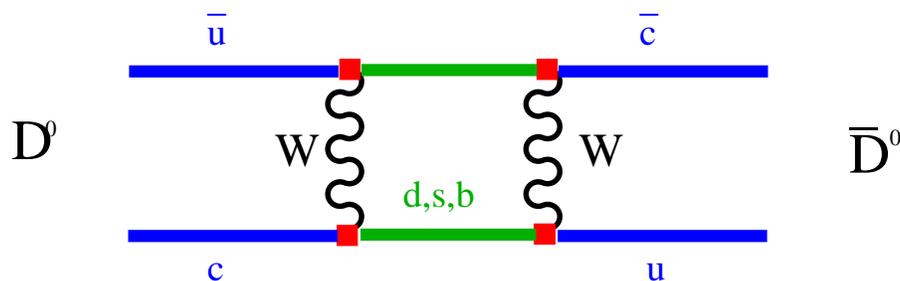
- For the semileptonic decays, the  $SU(3)$  breaking coming from the chiral logarithms is around  $20 - 30\%$ , strongly depending on the value of  $g_{D^* D \pi}$ . (*A. Falk and B. Grinstein '93*)
- But these are not the only terms. How large are the counter-term contributions? The data will tell us.

## D<sup>0</sup>- $\bar{D}^0$ Mixing

The mixing rate is

$$r_D \equiv \frac{\Gamma(D^0 \rightarrow \ell^- X)}{\Gamma(D^0 \rightarrow \ell^+ X)} \simeq \frac{1}{2} [x^2 + y^2]$$

with  $x \equiv \Delta m/\Gamma$  and  $y \equiv \Delta\Gamma/2\Gamma$ .



### Theoretical Expectations

- Short distance in the SM: Box + Penguin diagrams give  $x \lesssim 10^{-4}$ .
- But potentially large contributions from higher dimensional operators could give  $x \simeq 10^{-3}$ . (With very large uncertainties). This typically signals large long distance contributions!
- Long Distance effects in  $x$  and  $y$  from real intermediate states  $\Rightarrow$  expect

$$x_{LD} \simeq y \lesssim 10^{-3}$$

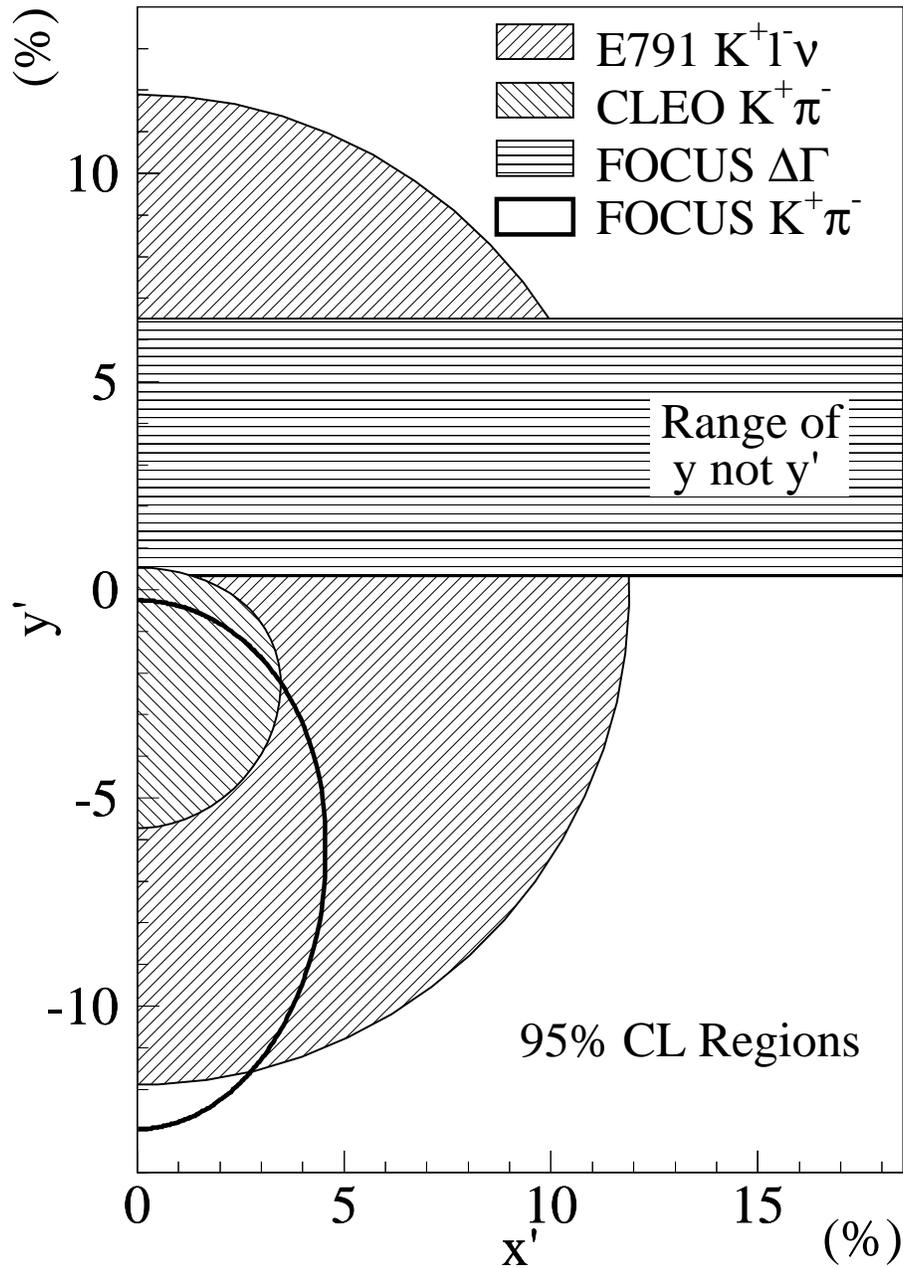
- Relative strong phase  $\delta$ , between CF and DCS amplitudes rotates  $x, y$  to

$$x' = x \cos \delta + y \sin \delta$$

$$y' = y \cos \delta - x \sin \delta$$

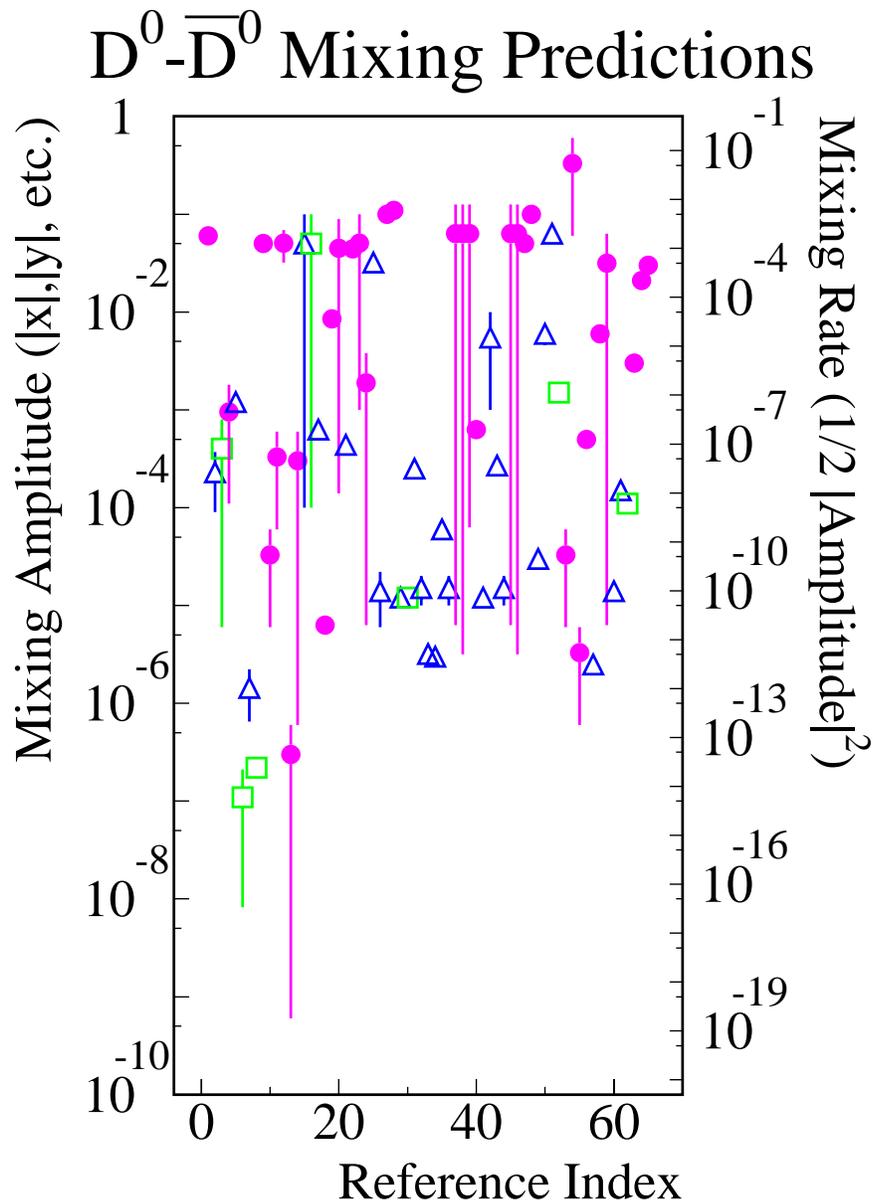
- Data seems to suggest  $\delta$  not small.

# $D^0-\bar{D}^0$ Mixing Experimental Situation



Is there room for **New Physics beyond the SM** ?

(*H. Nelson '99*)



## Rare Charm Decays

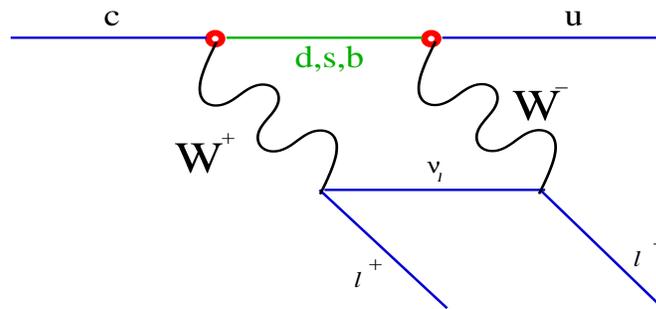
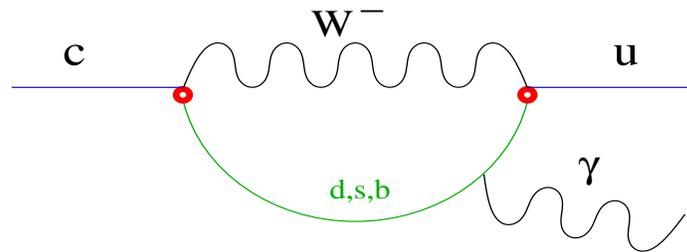
Q:

- $D \rightarrow X\gamma, D \rightarrow X\ell^+\ell^-, \dots$   
Can Rare Charm Decays test the SM ?
- Short distance SM very suppressed.
- Long distance (e.g. resonances) dominate rates.
- Is there room to see new physics ?

A:

- $D \rightarrow X\gamma, D^0 \rightarrow \gamma\gamma$ : Dominated by large long distance contributions.
- $D \rightarrow X\ell^+\ell^-$ : Long distance dominates the rates but maybe room for short distance away from the resonances.
- Other modes:  $D^0 \rightarrow \ell^+\ell^-, D \rightarrow X\nu\bar{\nu}$ , etc. Very small short and long distance  $\Rightarrow$  only large new physics effects.

## Rare Charm Decays



SO

	$i$	$F(x_i)$	$\lambda_i F(x_i)$
$c \rightarrow u \gamma$	d	$1.6 \times 10^{-9}$	$3.4 \times 10^{-10}$
	s	$2.9 \times 10^{-7}$	$6.3 \times 10^{-8}$
	b	$3.3 \times 10^{-4}$	$3.2 \times 10^{-8}$
$b \rightarrow s \gamma$	u	$2.3 \times 10^{-9}$	$1.3 \times 10^{-12}$
	c	$2.0 \times 10^{-4}$	$7.3 \times 10^{-6}$
	t	0.4	$1.6 \times 10^{-2}$

## Factorization of Short Distance Physics in $c \rightarrow u$ Transitions

Effective Hamiltonian at low energies:

$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$

Integrating out heavy particles.

- $C_i$ : Wilson coefficients. Content of the short distance physics, e.g. the stuff inside the loop.
- $\mathcal{O}_i$ : Operator basis. All possible (Lorentz invariant, etc.) giving  $c \rightarrow u$ . Matrix elements contain long distance physics.

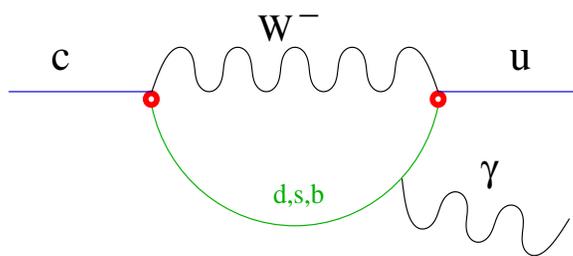
New Physics will affect matching conditions on the  $C_i$  at  $\mu = M$ .

E.g. in the SM  $M \simeq M_W$ .

# Radiative Decays

(*G.B., E. Golowich, J. Hewett and S. Pakvasa '95; B. Bajc et al. '95; C. Greub et al. '96* )

- $c \rightarrow u\gamma$ : Short distance determined by  $C_7(\mu)$  corresponding to the photon penguin diagram



and to the operator

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_c (\bar{u}_L \sigma_{\mu\nu} c_R) F^{\mu\nu}$$

The branching ratio is

$$Br(D \rightarrow X_u \gamma) = \dots |C_7(m_c)|^2$$

which is  $\mathcal{O}(10^{-17})$ .

- Operator mixing, mainly with  $O_2 = (\bar{u}_L \gamma_\mu q_L)(\bar{q}_L \gamma^\mu c_L)$ , plus large QCD corrections, result in

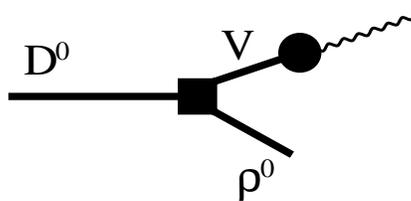
$$C_7(m_c) \longrightarrow C_7^{\text{eff.}}(m_c)$$

which give  $Br(c \rightarrow u\gamma) \simeq \mathcal{O}(10^{-8})$ .

- **Long Distance** contributions to  $D \rightarrow X\gamma$ : Take one example:  $D^0 \rightarrow \rho^0\gamma$ . Two types of **LD** diagrams:  
Pole diagrams:



Vector Meson Dominance:



Mode	$\mathcal{A}$ (in $\text{GeV}^{-1}$ )			$B_{D \rightarrow M\gamma}$ ( $10^{-5}$ )
	P-I	P-II	VMD <	
$D_s^+ \rightarrow \rho^+ \gamma$	8.2	-1.9	$\pm 6.0$	6 - 38
$D^0 \rightarrow \bar{K}^{*0} \gamma$	5.6	-5.9	$\pm 10$	7 - 12
$D_s^+ \rightarrow b_1^+ \gamma$	7.2	—	—	$\sim 6.3$
$D_s^+ \rightarrow a_1^+ \gamma$	1.2	—	—	$\sim 0.2$
$D_s^+ \rightarrow a_2^+ \gamma$	2.1	—	—	$\sim 0.01$
$D^+ \rightarrow \rho^+ \gamma$	1.3	-0.4	$\pm 3.5$	2 - 6
$D^+ \rightarrow b_1^+ \gamma$	1.2	—	—	$\sim 3.5$
$D^+ \rightarrow a_1^+ \gamma$	0.5	—	—	$\sim 0.04$
$D^+ \rightarrow a_2^+ \gamma$	3.4	—	—	$\sim 0.03$
$D_s^+ \rightarrow K^{*+} \gamma$	2.8	-0.5	$\pm 1.9$	0.8 - 3
$D_s^+ \rightarrow K_2^{*+} \gamma$	6.0	—	—	$\sim 0.2$
$D^0 \rightarrow \rho^0 \gamma$	0.5	-0.5	$\pm 2$	0.1 - 0.5
$D^0 \rightarrow \omega^0 \gamma$	0.6	-0.7	$\pm 1.3$	$\simeq 0.2$
$D^0 \rightarrow \phi^0 \gamma$	0.7	-1.6	$\pm 5$	0.1 - 3.4
$D^+ \rightarrow K^{*+} \gamma$	0.4	-0.1	$\pm 0.8$	0.1 - 0.3
$D^0 \rightarrow K^{*0} \gamma$	0.2	-0.3	$\pm 0.4$	$\simeq 0.01$

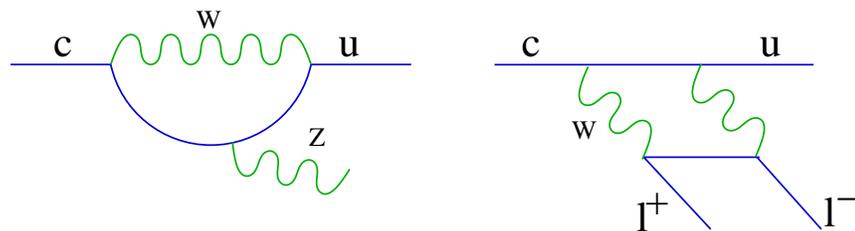
These contributions overwhelm (“irreducibly”) the short distance physics.

## Dilepton Modes

(*G.B., E. Golowich, J. Hewett and S. Pakvasa '01,*  
*also Fajfer, Prelovsekk and Singer '01*)

### $D \rightarrow X l^+ l^-$

- In addition to the photon penguin, now we also have



Then, the short distance is given by  $O_7$  plus

$$O_9 = \frac{e^2}{16\pi^2} (\bar{u}_L \gamma_\mu c_L) (\bar{l} \gamma^\mu l) ,$$

$$O_{10} = \frac{e^2}{16\pi^2} (\bar{u}_L \gamma_\mu c_L) (\bar{l} \gamma^\mu \gamma_5 l) .$$

- Compute  $C_7$ ,  $C_9$  and  $C_{10}$ . When QCD is added, mixing with other operators. In the SM we have

$$\mathcal{B}r_{D^+ \rightarrow X_u^+ e^+ e^-}^{(sd)} \simeq 2 \times 10^{-8}$$

$$\mathcal{B}r_{D^0 \rightarrow X_u^0 e^+ e^-}^{(sd)} \simeq 8 \times 10^{-9}$$

- Long Distance contributions: Dominated by intermediate vector meson states:

$D \rightarrow PV^0 \rightarrow P\ell^+\ell^-$ . For instance, in  $D^+ \rightarrow \pi^+\ell^+\ell^-$ ,  $\phi$  dominates.

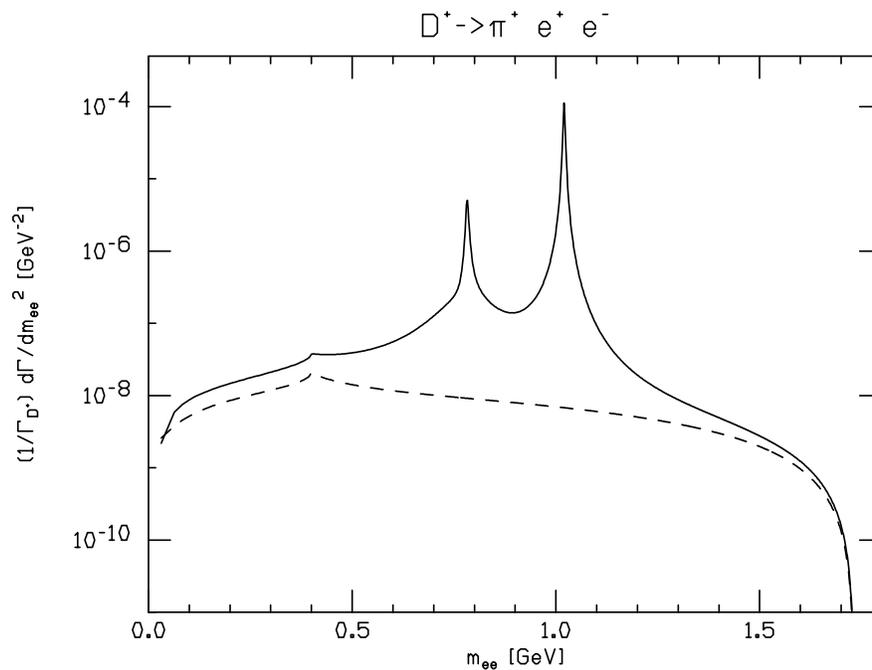
Mode	$\mathcal{B}r^{(\text{pole})}$	$\mathcal{B}r^{(\text{exp.})}$
$D^+ \rightarrow \pi^+\phi \rightarrow \pi^+e^+e^-$	$1.8 \cdot 10^{-6}$	$< 6.6 \cdot 10^{-5}$
$D^+ \rightarrow \pi^+\phi \rightarrow \pi^+\mu^+\mu^-$	$1.5 \cdot 10^{-6}$	$< 1.8 \cdot 10^{-5}$
$D_s^+ \rightarrow \pi^+\phi \rightarrow \pi^+e^+e^-$	$1.1 \cdot 10^{-5}$	— — —
$D_s^+ \rightarrow \pi^+\phi \rightarrow \pi^+\mu^+\mu^-$	$0.9 \cdot 10^{-5}$	$< 4.3 \cdot 10^{-4}$

- They affect the vector couplings of leptons.  $\Rightarrow$  the off-resonance effects can be included as

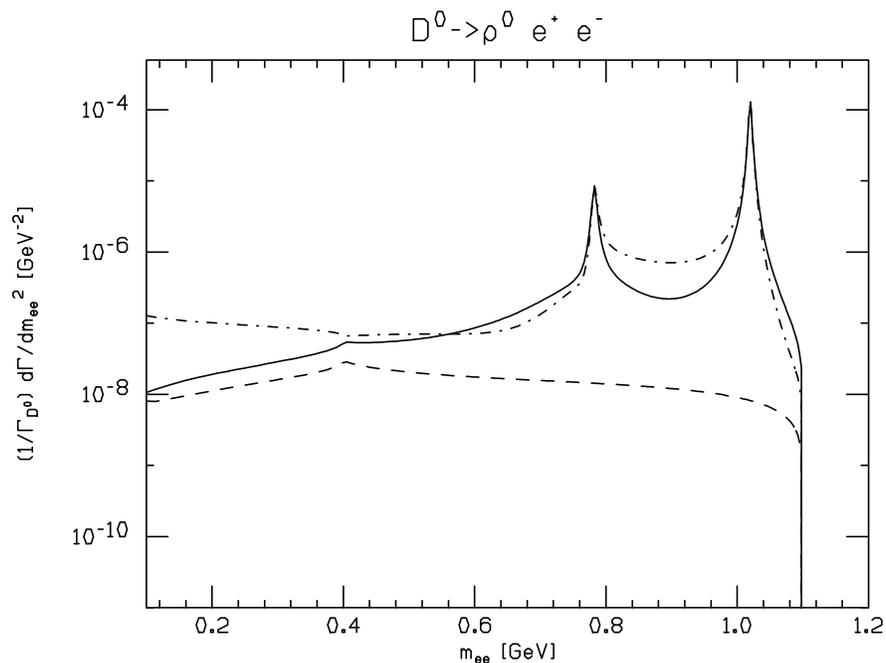
$$C_9 \rightarrow C_9 + \frac{3\pi}{\alpha^2} \sum_i \kappa_i \frac{m_{V_i} \Gamma_{V_i \rightarrow \ell^+\ell^-}}{m_{V_i}^2 - s - im_{V_i} \Gamma_{V_i}},$$

with the  $\kappa_i$ 's fit to  $D^+ \rightarrow \pi^+V_i$  data.

Finally, using semileptonic form-factors gives predictions for  $D^+ \rightarrow \pi^+ l^+ l^-$ ,



and  $D^0 \rightarrow \rho^0 l^+ l^-$ :

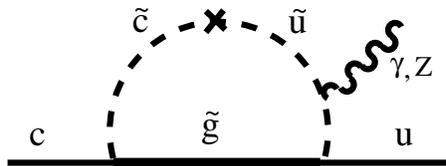


## Rare D Decays in the MSSM

- Non-universal soft breaking terms:

$$\begin{aligned} \mathcal{L}_{\text{soft}}^{\text{n.u.}} = & -Q^{i\dagger} (M_Q^2)^{ij} Q^j - D^{i\dagger} (M_D^2)^{ij} D^j \\ & -U^{i\dagger} (M_U^2)^{ij} U^j + \dots \\ & + (A_D^{ij} H^1 Q^i D^j + A_U^{ij} H^2 Q^i U^j + \dots) \end{aligned}$$

- Stability bounds apply to trilinear terms  $A^{ij}$ .
- Bounds on off-diagonal  $M_Q$ , etc. from FCNC.



=> bounds on

$$(\delta_{ij}^u)_{AB} \equiv \frac{(M_{ij}^U)_{AB}^2}{M_{\tilde{q}}^2}$$

and  $A, B = L, R$ .

Effects of **squark-gluino** in Wilson coefficients:

- The operators  $O_7$  and  $O_9$  get

$$C_7^{\tilde{g}} = -\frac{16}{9} \left( \frac{v}{M_{\tilde{q}}} \right)^2 \pi \alpha_s \left\{ (\delta_{12}^u)_{LL} \frac{P_{132}(u)}{4} + (\delta_{12}^u)_{RL} P_{122}(u) \frac{M_{\tilde{g}}}{m_c} \right\}$$

$$C_9^{\tilde{g}} = -\frac{16}{27} \left( \frac{v}{M_{\tilde{q}}} \right)^2 \pi \alpha_s (\delta_{12}^u)_{LL} P_{042}(u)$$

- $C_{10}$  requires *two* mass insertions

$$C_{10}^{\tilde{g}} = -\frac{1}{9} \frac{\alpha_s}{\alpha} (\delta_{22}^u)_{RL} (\delta_{12}^u)_{LR} P_{032}(u)$$

$$u \equiv \left( \frac{M_{\tilde{g}}}{M_{\tilde{q}}} \right)^2$$

- Operator basis is extended to include:

$$O'_7 = \frac{e}{16\pi^2} m_c (\bar{u}_R \sigma_{\mu\nu} c_L) F^{\mu\nu}$$

$$O'_9 = \frac{e^2}{16\pi^2} (\bar{u}_R \gamma_\mu c_R) (\bar{\ell} \gamma^\mu \ell)$$

$$O'_{10} = \frac{e^2}{16\pi^2} (\bar{u}_R \gamma_\mu c_R) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

- These get

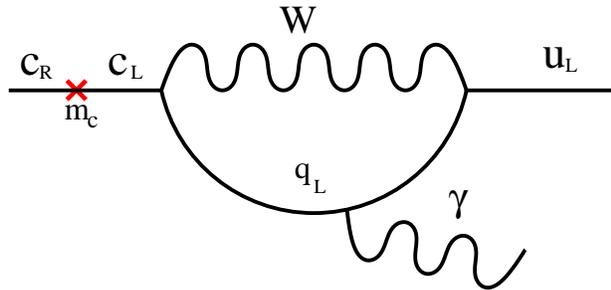
$$C'_7{}^{\tilde{g}} = -\frac{16}{9} \left( \frac{v}{M_{\tilde{q}}} \right)^2 \pi \alpha_s \left\{ (\delta_{12}^u)_{RR} \frac{P_{132}(u)}{4} + (\delta_{12}^u)_{LR} P_{122}(u) \frac{M_{\tilde{g}}}{m_c} \right\}$$

$$C'_9{}^{\tilde{g}} = -\frac{16}{27} \left( \frac{v}{M_{\tilde{q}}} \right)^2 \pi \alpha_s (\delta_{12}^u)_{RR} P_{042}(u)$$

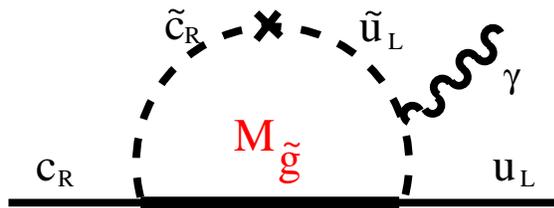
$$C'_{10}{}^{\tilde{g}} = -\frac{1}{9} \frac{\alpha_s}{\alpha} (\delta_{22}^u)_{LR} (\delta_{12}^u)_{LR} P_{032}(u)$$

## $M_{\tilde{g}}$ enhancement

- In the SM  $O_7 = \frac{e}{16\pi^2} m_c (\bar{u}_L \sigma_{\mu\nu} c_R) F^{\mu\nu}$  requires  $m_c$  insertion



- But here the flip is done in the **gluino** line



$\Rightarrow C_7$  (and  $C'_7$ ) pick up a factor of  $M_{\tilde{g}}/m_c$ .

## Bounds on the $(\delta_{ij}^u)_{AB}$

- Best limits on  $(\delta^u)_{AB}$  come from  $D^0 - \bar{D}^0$  mixing (CLEO, FOCUS)

$$\frac{1}{2} \left\{ \left( \frac{\Delta m_D}{\Gamma_{D^0}} \right)^2 \cos \delta + \left( \frac{\Delta \Gamma_D}{2\Gamma_{D^0}} \right)^2 \sin \delta \right\} < 0.04\%$$

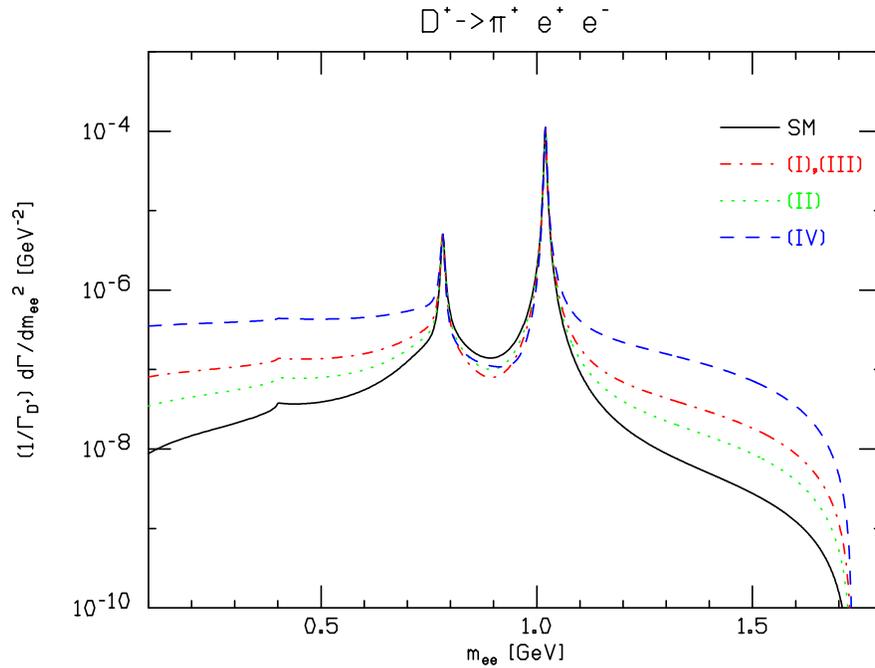
with  $\delta$  relative strong phase between  $D^0 \rightarrow K^- \pi^+$  and  $D^0 \rightarrow K^+ \pi^-$ .

- Assuming  $\delta$  is negligible

$M_{\tilde{g}}^2 / M_{\tilde{q}}^2$	$(\delta_{12}^u)_{LL}$	$(\delta_{12}^u)_{LR}$
0.3	0.03	0.04
1.0	0.06	0.02
4.0	0.14	0.02

$\times M_{\tilde{q}} / 500 \text{ GeV}$ .

The effects in  $D \rightarrow \pi \ell^+ \ell^-$  moderately constraining

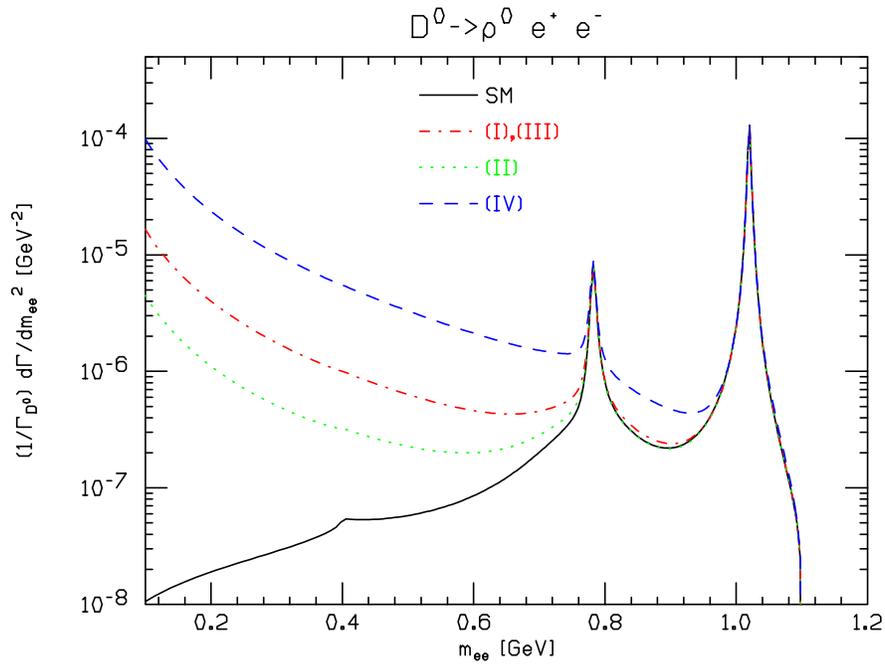


with

- (I) :  $M_{\tilde{g}} = M_{\tilde{q}} = 250$  GeV
- (II) :  $M_{\tilde{g}} = 2 M_{\tilde{q}} = 500$  GeV
- (III):  $M_{\tilde{g}} = M_{\tilde{q}} = 1000$  GeV
- (IV):  $M_{\tilde{g}} = (1/2) M_{\tilde{q}} = 250$  GeV.

and we take  $(\delta_{12}^u)_{RR} = 0$  and  $(\delta_{12}^u)_{RL} = (\delta_{12}^u)_{LR}$ .

## Potentially large effects in the $D \rightarrow \rho l^+ l^-$ channels



- Low  $q^2 = m_{ee}^2$  enhancement due to photon propagator in  $C_7$  term. In  $D \rightarrow \pi l^+ l^-$  this is cancelled by matrix element giving  $(q^2 \gamma_\mu - q_\mu \not{q})$ .
- $Br(D^0 \rightarrow \rho^0 e^+ e^-) \simeq 1.3 \times 10^{-5} \simeq 5 \text{ SM}$ .  
 $Br^{\text{exp.}}(D^0 \rightarrow \rho^0 e^+ e^-) < 1.2 \times 10^{-4}$ .

## R Parity Violation in SUSY

- Large violation of R parity is possible if other symmetries invoked to avoid proton decay. RPV superpotential

$$\mathcal{W}_{R_p} = \epsilon_{ab} \tilde{\lambda}'_{ijk} L_i^a Q_j^b \bar{D}_k + \dots$$

- In the mass eigenbasis we get

$$\mathcal{W}_{R_p} = \lambda'_{ijk} [N_i V_{jl} D_l - E_i U_j] \bar{D}_k + \dots$$

with

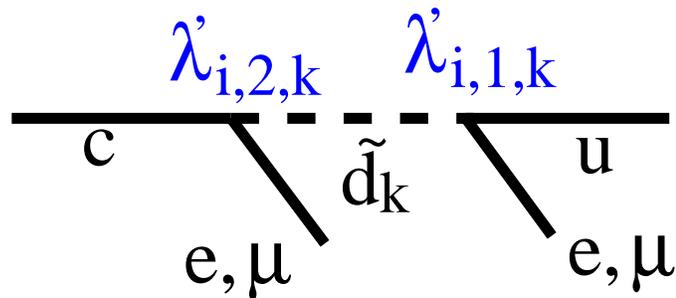
$$\lambda'_{ijk} \equiv \tilde{\lambda}'_{irs} \mathcal{U}_{rj}^L \mathcal{D}_{sk}^{*R}$$

and  $\mathcal{U}$ ,  $\mathcal{D}$  rotate quarks to mass basis.

The interesting part of the super-potential gives  
(expanded in components in the mass basis)

$$\mathcal{W}_{\lambda'} = \lambda'_{ijk} \left\{ V_{jl} [\tilde{\nu}_L^i \bar{d}_R^k d_L^l + \tilde{d}_L^l \bar{d}_R^k \nu_L^i + (\tilde{d}_R^k)^* \overline{(\nu_L^i)^c} d_L^l] \right. \\ \left. - \tilde{e}_L^i \bar{d}_R^k u_L^j - \tilde{u}_L^j \bar{d}_R^k e_L^i - (\tilde{d}_R^k)^* \overline{(e_L^i)^c} u_L^j \right\}$$

Two insertions of last term  $\Rightarrow c \rightarrow ull'$  transitions.



This induces

$$\delta\mathcal{H}_{\text{eff.}} = -\frac{\lambda'_{i2k}\lambda'_{i1k}}{2m_{\tilde{d}_R^k}^2} (\bar{u}_L\gamma_\mu c_L)(\bar{\ell}_L\gamma^\mu \ell_L)$$

leading to

$$\delta C_9 = -\delta C_{10} = \frac{s^2\theta_W}{2\alpha^2} \left(\frac{M_W}{m_{\tilde{d}_R^k}}\right)^2 \lambda'_{i2k}\lambda'_{i1k}$$

(More) model-independent bounds give -in units of  
 $\times (m_{\tilde{d}_R^k}/100)$  GeV-

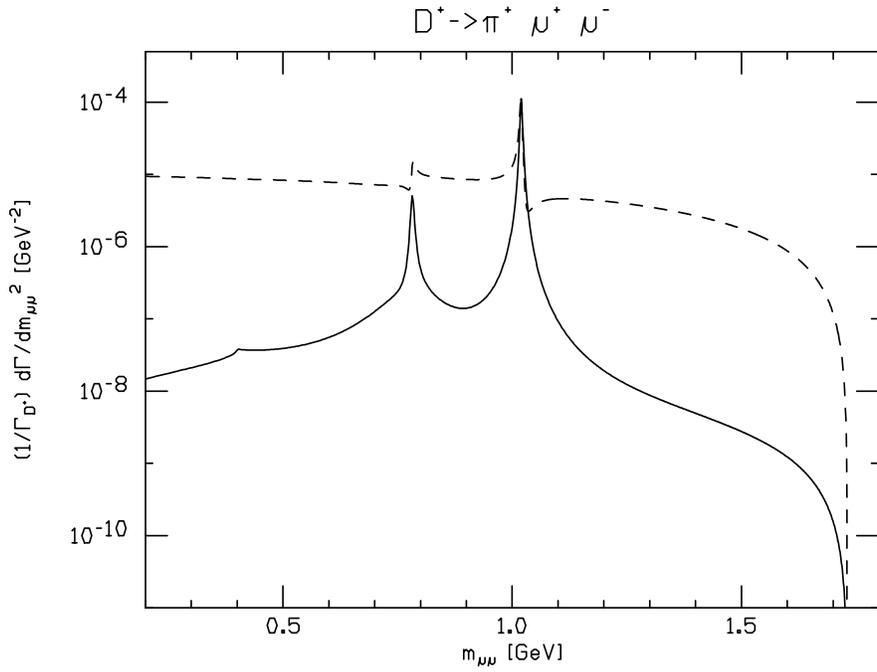
$\lambda'_{11k}$	$\lambda'_{12k}$	$\lambda'_{21k}$	$\lambda'_{22k}$
0.02 <sup>a)</sup>	0.04 <sup>a)</sup>	0.06 <sup>b)</sup>	0.21 <sup>c)</sup>

a) Charged current universality.

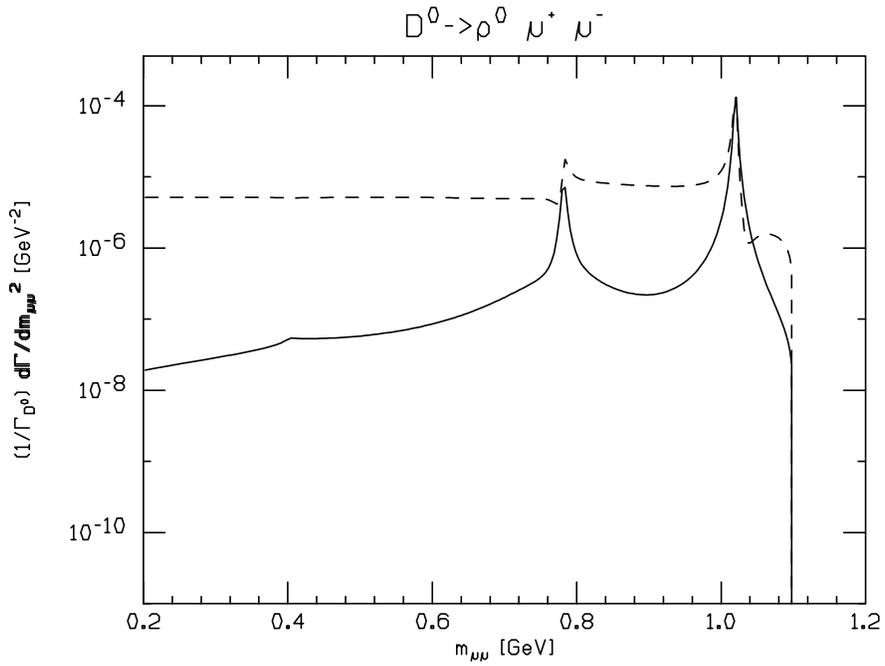
b)  $R_\pi = \Gamma(\pi \rightarrow e\nu)/\Gamma(\pi \rightarrow \mu\nu)$ .

c)  $D \rightarrow K\ell\nu$ .

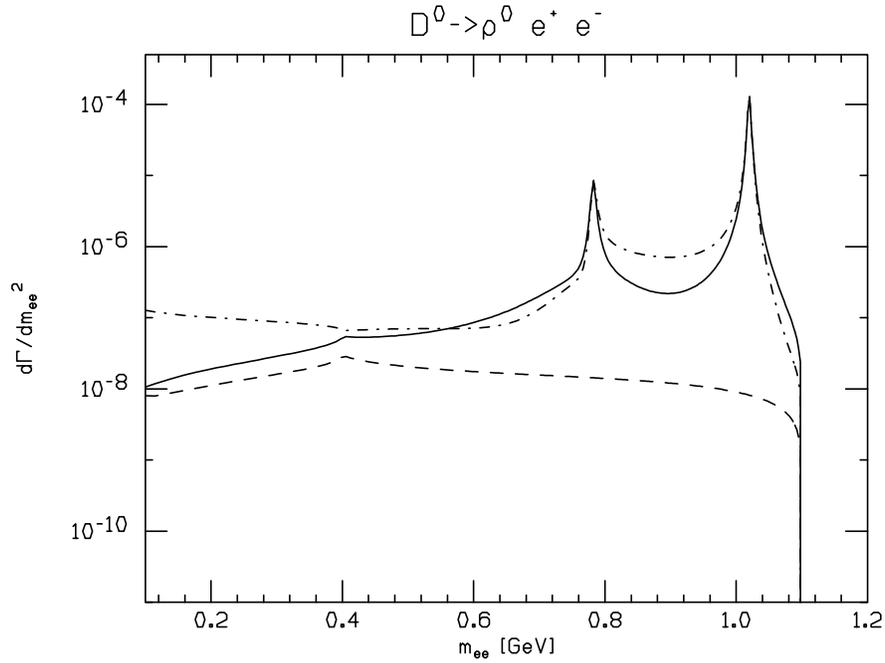
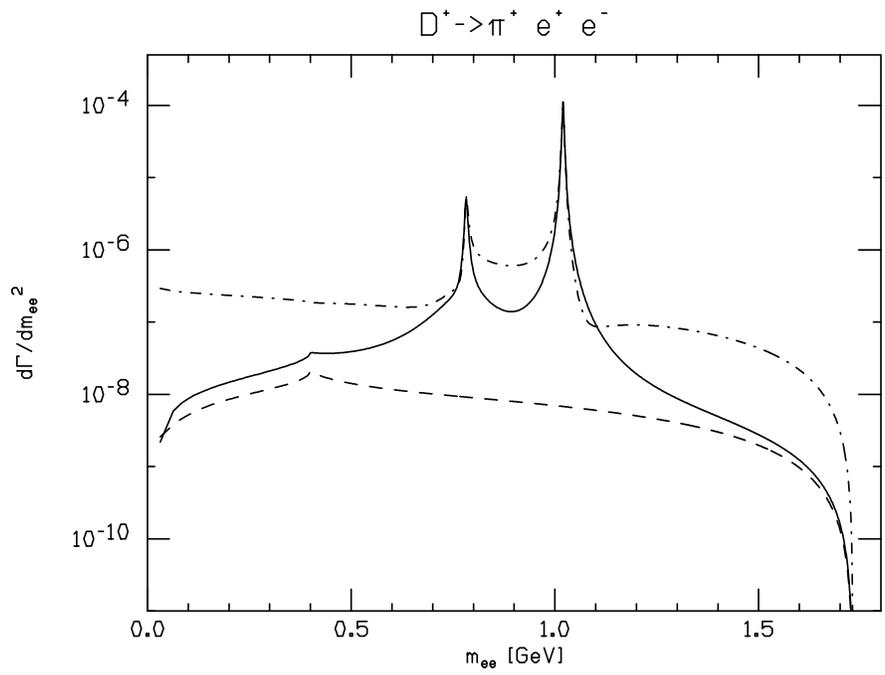
Large effects in the  $\mu^+ \mu^-$  channel.



This actually  $\Rightarrow \lambda'_{22k} \lambda'_{21k} < 0.004$  and gives



# Effects in the $e^+e^-$ channel.

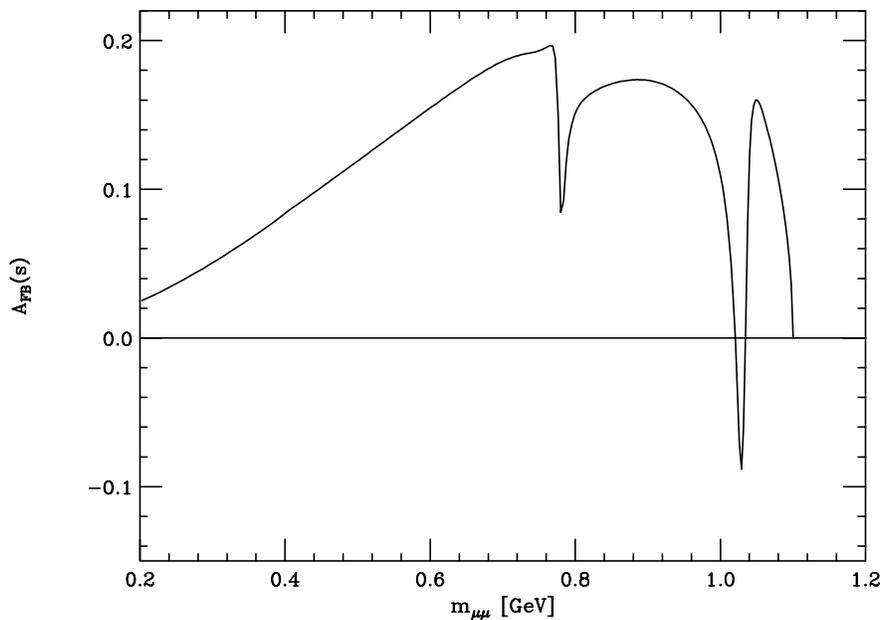


# Forward-Backward Asymmetry in $D \rightarrow \rho l^+ l^-$

FB Asymmetry for leptons

$$A_{FB}(q^2) = \frac{\int_0^1 \frac{d^2\Gamma}{dx dq^2} dx - \int_{-1}^0 \frac{d^2\Gamma}{dx dq^2} dx}{\frac{d\Gamma}{dq^2}}$$

with  $x = \cos \theta$ . **It's negligible in the SM!** But if  $C_{10} \simeq C_9$  it could be observable:



$$A_{FB}^{\text{tot.}} \lesssim 0.15 \text{ for } \mu^+ \mu^-.$$

$$A_{FB}^{\text{tot.}} \lesssim 0.08 \text{ for } e^+ e^-.$$

Decay Mode	SM	$\mathcal{R}_p$	Exp. Limit.
$D^+ \rightarrow \pi^+ e^+ e^-$	$2.0 \times 10^{-6}$	$2.3 \times 10^{-6}$	$5.2 \times 10^{-5}$
$D^0 \rightarrow \rho^0 e^+ e^-$	$2.5 \times 10^{-6}$	$5.1 \times 10^{-6}$	$1.2 \times 10^{-4}$
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	$1.9 \times 10^{-6}$	$1.5 \times 10^{-5}$	$1.5 \times 10^{-5}$
$D^0 \rightarrow \rho^0 \mu^+ \mu^-$	$4.5 \times 10^{-6}$	$8.7 \times 10^{-6}$	$2.2 \times 10^{-5}$
$D^0 \rightarrow \mu^+ \mu^-$	$3.0 \times 10^{-15}$	$3.5 \times 10^{-6}$	$5.2 \times 10^{-6}$
$D^0 \rightarrow e^+ e^-$	few $10^{-24}$	$1.0 \times 10^{-10}$	$6.2 \times 10^{-6}$
$D^0 \rightarrow \mu^+ e^-$	0	$1.0 \times 10^{-6}$	$8.1 \times 10^{-6}$
$D^+ \rightarrow \pi^+ \mu^+ e^-$	0	$3.0 \times 10^{-5}$	$3.4 \times 10^{-5}$
$D^0 \rightarrow \rho^0 \mu^+ e^-$	0	$1.4 \times 10^{-5}$	$6.6 \times 10^{-5}$

## Conclusions

- Semileptonic Decays: Precision measurements of  $D \rightarrow (\pi, \rho)l\nu$ ,  $D \rightarrow K^{(*)}l\nu \Rightarrow$  Tests of HQET,  $SU(3)$ , Lattice calculations. Impact on  $B$  physics:  $V_{ub}$ , predictions for exclusive rare  $B$  decays ( $B \rightarrow K^{(*)}l^+l^-$ ).
- $D^0 - \bar{D}^0$  Mixing: theoretical limitation, need to understand long distance contributions.
- Charm decays induced by FCNC are sensitive to short distance physics if one stays away from resonances: e.g. this is possible in  $D \rightarrow \pi l^+l^-$  and  $D \rightarrow \rho l^+l^-$
- $D \rightarrow \pi l^+l^-$  and *especially*  $D \rightarrow \rho l^+l^-$ , are sensitive to non-universal effects in the MSSM scalar sector if sensitivities around ( $10^{-6}$ - $10^{-7}$ ) are achieved.
- With current sensitivity around  $10^{-5}$  these modes are already constraining R-parity violating couplings.