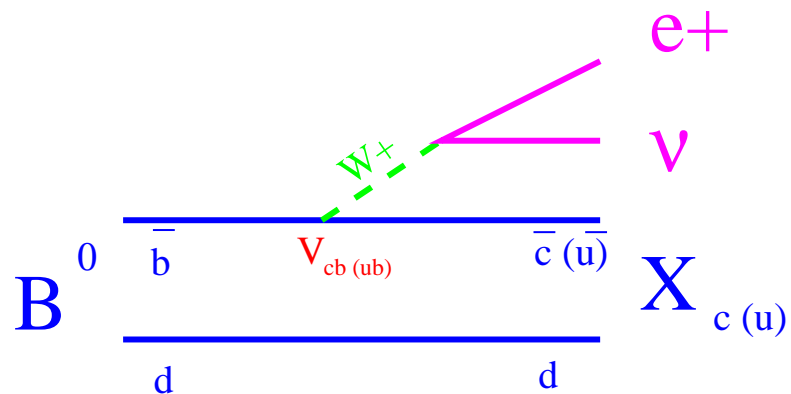


Semileptonic B decays – $|V_{ub}|$ and $|V_{cb}|$

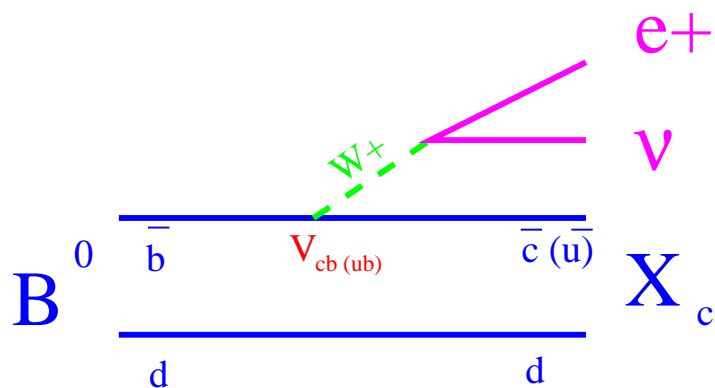


Karl Ecklund, Cornell University
May 18, 2002

Outline

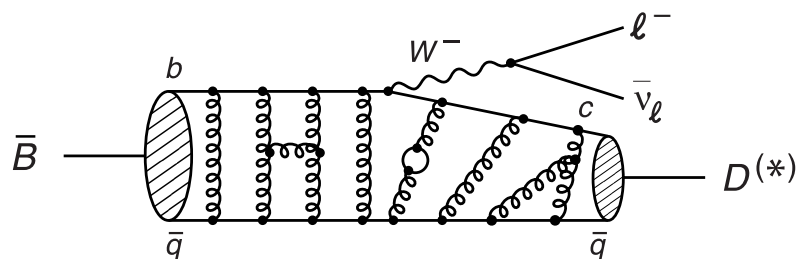
- Introduction: CKM from semileptonic B decays
- $|V_{cb}|$
 - Exclusive decays: $B \rightarrow D^{(*)} \ell \nu$
 - Inclusive decays: $B \rightarrow X_c \ell \nu$
- $|V_{ub}|$
 - Exclusive decays: $B \rightarrow \pi \ell \nu, \rho \ell \nu$
 - Inclusive decays: $B \rightarrow X_u \ell \nu$
- Summary and Outlook

CKM Measurements in Semileptonic B Decays



$$\Gamma(b \rightarrow x \ell \nu) = \frac{G_F^2 m_b^5}{192 \pi^3} |V_{xb}|^2$$

$X_{c(u)}$ Rates give CKM²



Complication!

QCD Corrections needed to extract weak decay physics

perturbative corrections and

non-perturbative QCD Corrections: from HQET, Lattice QCD

Use many techniques and compare results to gain confidence in QCD corr.

$|V_{cb}|$ from $\bar{B} \rightarrow D^{(*)} \ell \bar{\nu}$

Extracting $|V_{cb}|$ from exclusive decays:

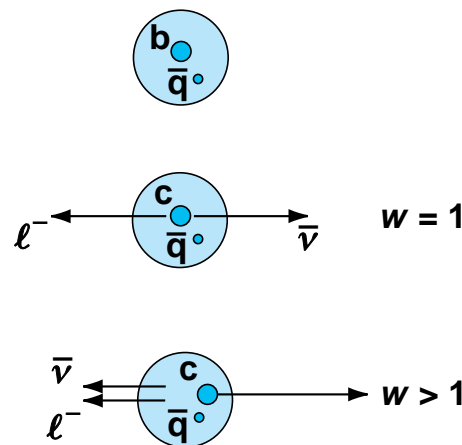
The decay rate is given by

$$\frac{d\Gamma}{dw} = \frac{G_F^2}{48\pi^3} |V_{cb}|^2 [\mathcal{F}(w)]^2 \mathcal{K}(w)$$

$$w = v_B \cdot v_{D^{(*)}} = \frac{m_B^2 + m_{D^{(*)}}^2 - q^2}{2m_B m_{D^{(*)}}}$$

- $\mathcal{K}(w)$ contains kinematic factors and is *known*
- $\mathcal{F}(w)$ is the form factor describing $B \rightarrow D^{(*)}$ transition
- HQET relations simplify the form factor
- HQS normalizes at zero recoil ($w = 1$): As $M_Q \rightarrow \infty$, $\mathcal{F}(1) \rightarrow 1$

Plan: Measure $d\Gamma/dw$ and Extrapolate to $w = 1$ to extract $\mathcal{F}(1)|V_{cb}|$.



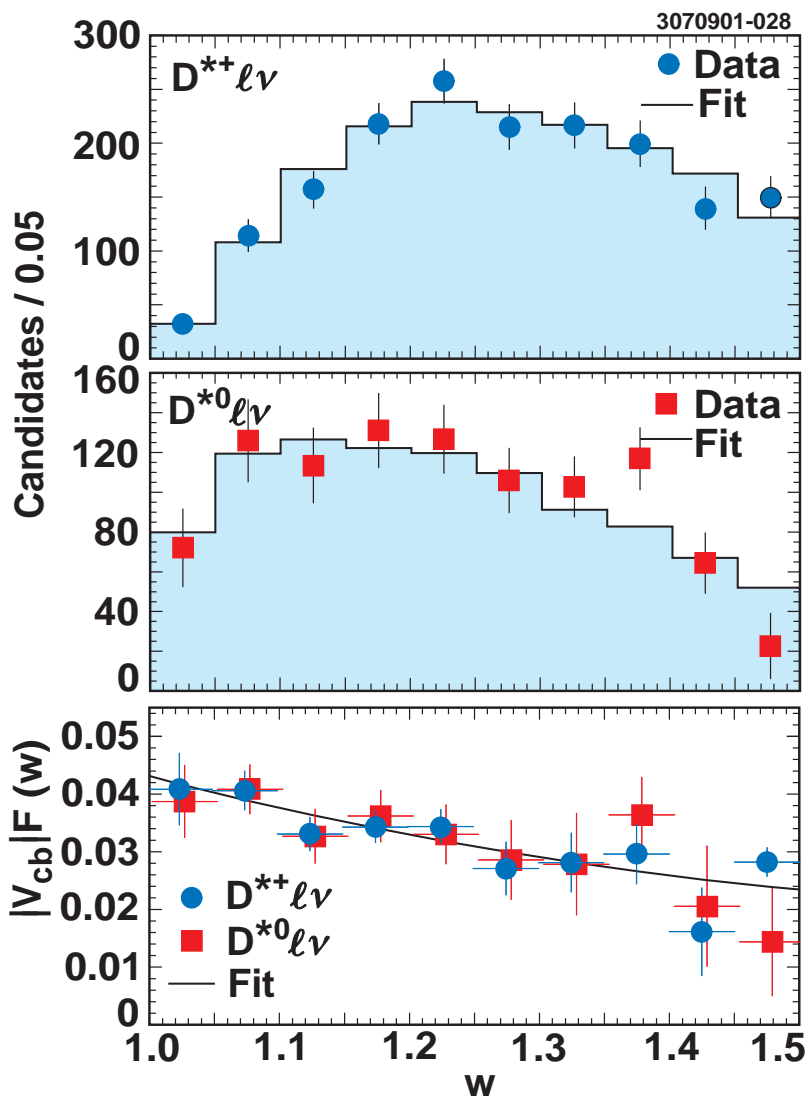
$B \rightarrow D^{(*)}$ Form Factor - QCD complications

- Must know form factor shape to extrapolate
- Must know $\mathcal{F}(1)$ to extract $|V_{cb}|$

The most general Lorentz-invariant form factor is simplified by

- **Massless leptons**
 - For $B \rightarrow D\ell\nu$ only vector current one FF: F_1
 - For $B \rightarrow D^*\ell\nu$ three FFs: A_1, A_2, V but ...
- **Heavy Quark Symmetry**
 - $M_Q \rightarrow \infty$: one form factor, the famous Isgur-Wise Function
 - Form Factor Ratios R_1 and R_2 approximately constant in w
- **QCD dispersion relations** constrain the shape (Boyd *et al.*)
 - Parameterization of FF: Caprini *et al.* NPB530 (1998) 153
 - Includes curvature but one shape parameter: ρ^2 , slope at $w = 1$

CLEO $\bar{B} \rightarrow D^* \ell \bar{\nu}$ hep-ex/0203032



(3.1 fb^{-1} $3.3 \text{ M } B\bar{B}$)

Reconstruct $D^{*+} \ell \nu$ and $D^{*0} \ell \nu$

Given yields in 10 w bins

Fit using Caprini form factor

Parameters:

- $\mathcal{F}(1)|V_{cb}|$ (intercept)
- ρ^2 (slope)

$$\mathcal{F}(1)|V_{cb}| = (43.1 \pm 1.3 \pm 1.8) \times 10^{-3}$$

$$\rho^2 = 1.61 \pm 0.09 \pm 0.21$$

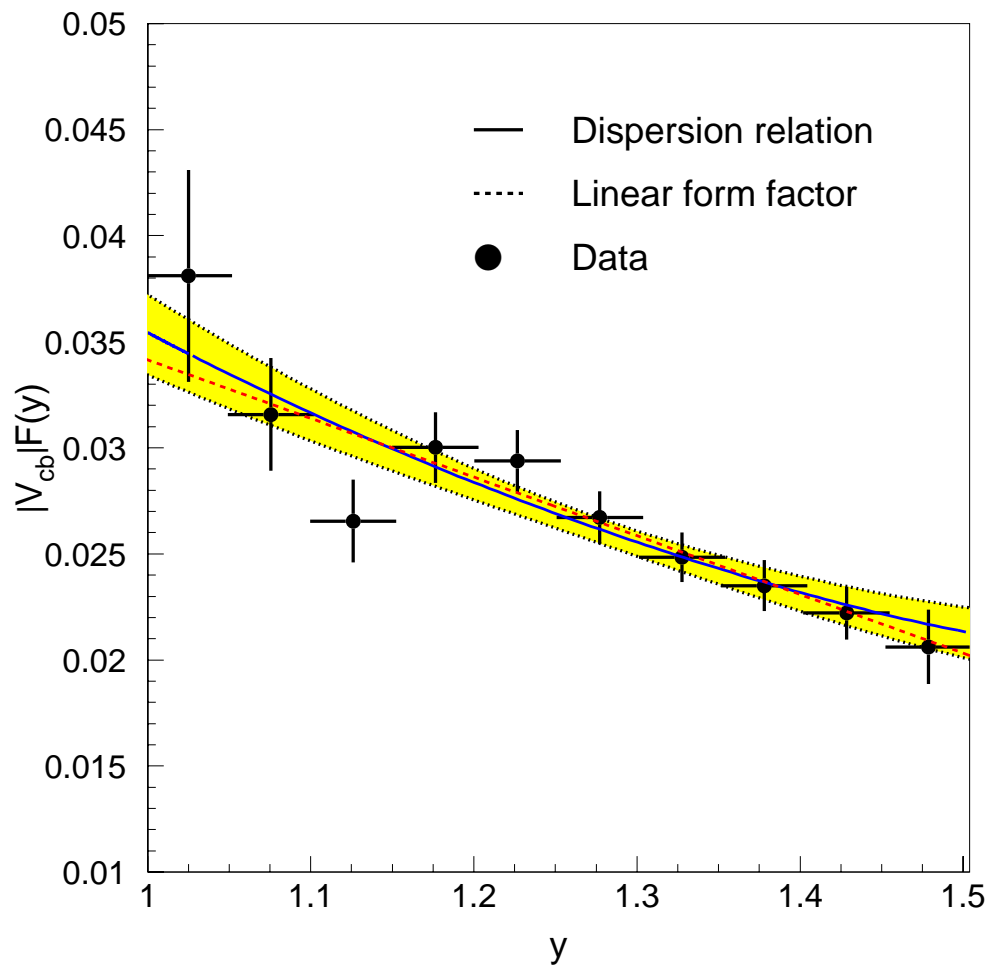
Theory: $\mathcal{F}(1) = 0.91 \pm 0.04$

$$|V_{cb}| = (47.4 \pm 1.4 \pm 2.0 \pm 2.1) \times 10^{-3}$$

7% precision

Systematics! efficiency, bkgds, BF's

BELLE $\bar{B} \rightarrow D^{*+} e^{-} \bar{\nu}$ PLB 526 (2002) 258



(10 fb^{-1} 11 M $B\bar{B}$)

Similar to CLEO and
LEP analyses

Uses only electrons

Extrapolation procedure gives correlation for ρ^2 and $\mathcal{F}(1)|V_{cb}|$

Average for $B \rightarrow D^* \ell \nu$

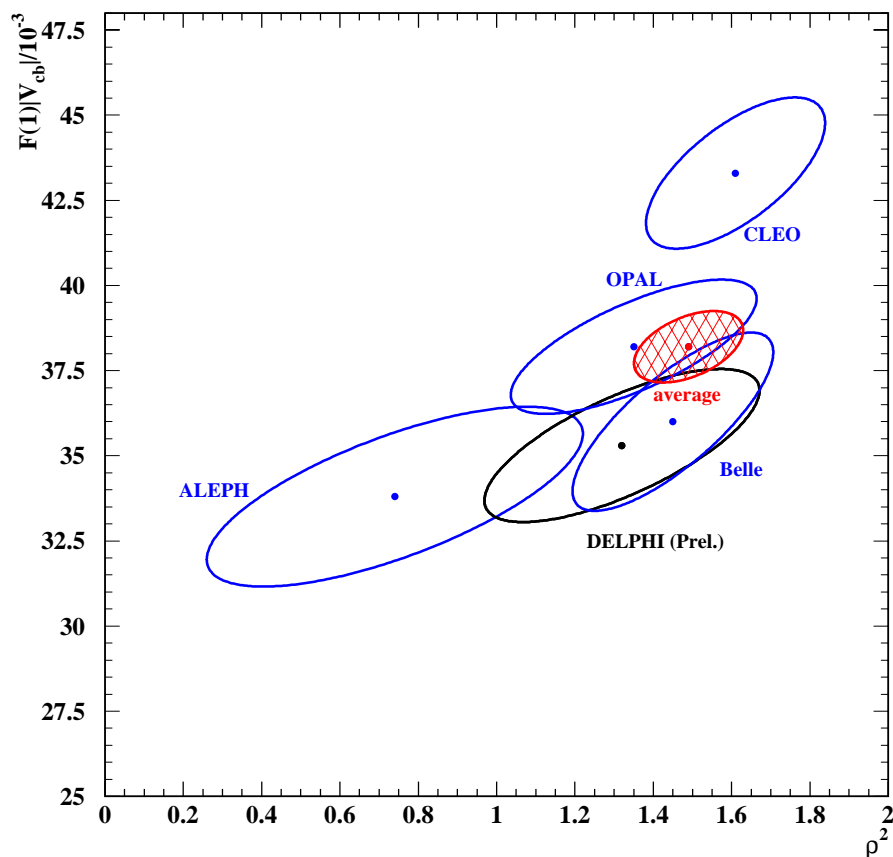
From LEP $|V_{cb}|$ working group updated for PDG02

Adjusted to common set of input parameters

- D branching fractions and B lifetimes
- Form-factor ratios R_1 and R_2
- $B \rightarrow D^* X \ell \nu$ background parameters

Fits for $\mathcal{F}(1)|V_{cb}|$ and ρ^2 accounting for correlations between experimental inputs, systematics and statistical correlation between $\mathcal{F}(1)|V_{cb}|$ ρ^2

Results of Average I



Note correlations in $\mathcal{F}(1)|V_{cb}|$ and ρ^2

5% C.L. from combined fit

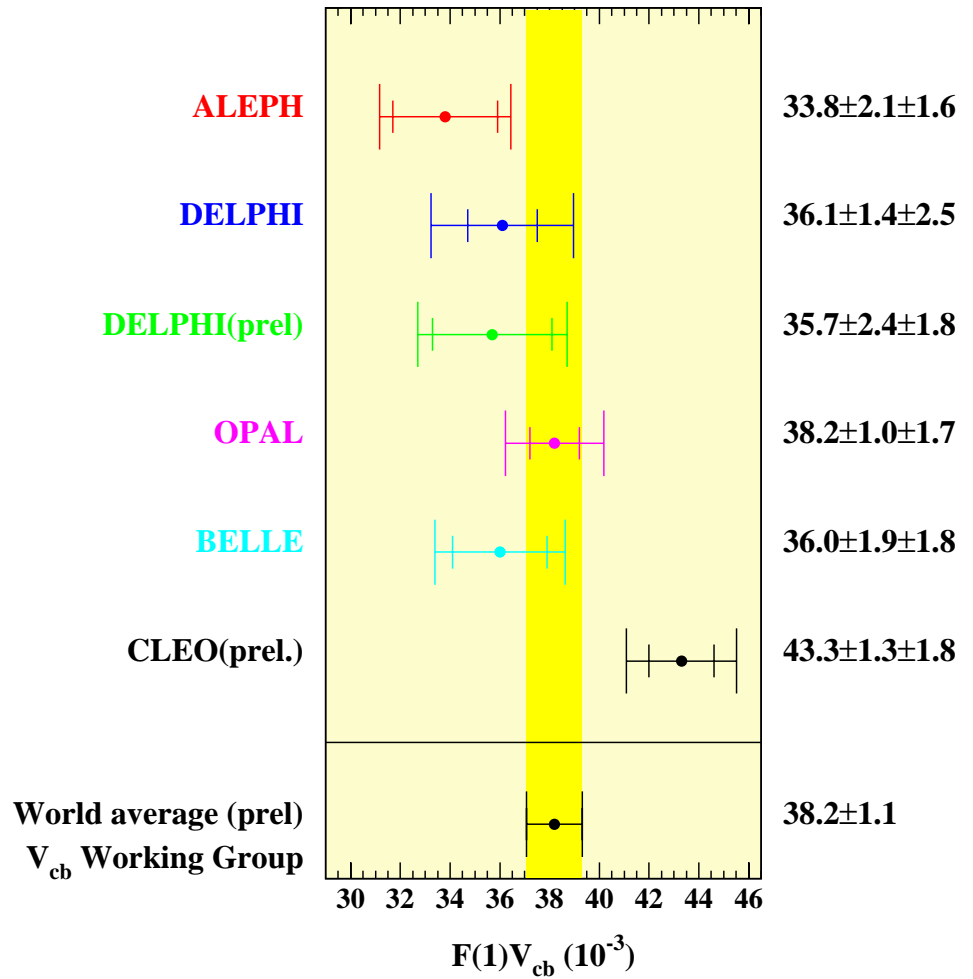
N.B. CLEO

- Includes D^{*0}
- Fits data simultaneously for $D^*Xl\nu$ background

Others share $D^*Xl\nu$ estimate & model

Ellipses are $\Delta\chi^2 = 1$ for each measurement (stat+syst)

Results of Average II



$$\mathcal{F}(1)|V_{cb}| = (38.2 \pm 1.1) \times 10^{-3}$$

With $\mathcal{F}(1) = 0.91 \pm 0.04$ $|V_{cb}| = (42.2 \pm 1.1_{\text{exp}} \pm 1.9_{\text{thr}}) \times 10^{-3}$

Comments about Average

- Need common treatment of input parameters and systematic errors
- Essential to use same form factor parameterization
- $C(\mathcal{F}(1)|V_{cb}|, \rho^2)$ on systematic errors needed

Important Issues For Future

- Background from $B \rightarrow D^* X \ell \nu$ - input from new data
- Form Factor Ratios R_1 and R_2 poorly known - can be measured
- Effect of EW radiative corrections on extrapolation and efficiency
- $\mathcal{F}(1)$ theory uncertainty currently $\sim 5\%$
should be reduced with unquenched Lattice results

Choosing Exclusive Final States

- $D^*\ell\nu$ has larger rate than $D\ell\nu$
- larger background in $D\ell\nu$ (from $D^*\ell\nu!$)
- $V - A$ kinematics favors D^* in extrapolation to low w
 - $\mathcal{K}_D(w) = (M_B + M_D)^2 M_D^3 (\sqrt{w^2 - 1})^3$
 - $\mathcal{K}_{D^*}(w) \propto \sqrt{w^2 - 1}$

- Luke's Theorem: For $\mathcal{F}(1)$, HQS-breaking corrections $\mathcal{O}(1/M_Q^2)$ for $D^*\ell\nu$ and at $\mathcal{O}(1/M_Q)$ for $D\ell\nu$

Bottom line: Most information from $B \rightarrow D^*\ell\nu$, but $B \rightarrow D\ell\nu$ can help in the end with FF parameter determinations.

ALPHA, BELLE and CLEO have $B \rightarrow D\ell\nu$ measurements:

- Less precise than $B \rightarrow D^*\ell\nu$
- Consistent determination of $|V_{cb}| = (41.3 \pm 4.0_{\text{exp}} \pm 2.9_{\text{th}}) \times 10^{-3}$

Inclusive $b \rightarrow cl\nu$

Rather than focussing on one hadronic final state where corrections may be calculated reliably,

Sum over all states and compare to quark-level calculation

$$\sum_i \Gamma(B \rightarrow X_c^{(i)} l \nu) = \Gamma(b \rightarrow cl\nu)$$

Relies on **assumption of quark-hadron duality**

Hard to quantify; must be tested!

Theoretical Tools for Inclusive $b \rightarrow c\ell\nu$

Heavy Quark Expansion in powers of $1/M_B$ and α_s

Operator Product Expansion - introduce parameters as matrix elements of nonperturbative operators:

At order $1/M$:

$\bar{\Lambda} \approx M_B - m_b$ energy of light degrees of freedom

At order $1/M^2$:

Λ_1 - kinetic energy of b quark in B meson

Λ_2 - hyperfine interaction of b spin with light d.o.f.

At order $1/M^3$:

ρ, \mathcal{T} - six more parameters with less-intuitive interpretations
and so on ...

Use HQE/OPE tools to predict rate

$$\Gamma = \frac{G_F^2 |V_{cb}|^2 M_B^5}{192\pi^3} \left[\mathcal{G}_0 + \frac{1}{M_B} \mathcal{G}_1(\bar{\Lambda}) + \frac{1}{M_B^2} \mathcal{G}_2(\bar{\Lambda}, \lambda_1, \lambda_2) \right. \\ \left. + \frac{1}{M_B^3} \mathcal{G}_3(\bar{\Lambda}, \lambda_1, \lambda_2 | \rho_1, \rho_2, \mathcal{T}_1, \mathcal{T}_2, \mathcal{T}_3, \mathcal{T}_4) + \mathcal{O}\left(\frac{1}{M_B^4}\right) \right]$$

and moments of decay spectra in $B \rightarrow X_c \ell \nu$:

$$\langle E_\ell \rangle, \langle E_\ell^2 \rangle, \langle M_X^2 \rangle \quad [\text{Falk, Luke, Savage, Gremm, Kapustin}]$$

$$\text{and } B \rightarrow X_s \gamma: \langle E_\gamma \rangle, \langle E_\gamma^2 \rangle \quad [\text{Bauer, Z. Ligeti } et al.]$$

Example:

$$\langle E_\gamma \rangle = \frac{M_B}{2} \left[1 - .385 \frac{\alpha_s}{\pi} - .620 \beta_0 \left(\frac{\alpha_s}{\pi} \right)^2 - \frac{\bar{\Lambda}}{M_B} \left(1 - .954 \frac{\alpha_s}{\pi} - 1.175 \beta_0 \left(\frac{\alpha_s}{\pi} \right)^2 \right) \right. \\ \left. - \frac{13\rho_1 - 33\rho_2}{12M_B^3} - \frac{\mathcal{T}_1 + 3\mathcal{T}_2 + \mathcal{T}_3 + 3\mathcal{T}_4}{4M_B^3} - \frac{\rho_2 C_2}{9M_B M_D^2 C_7} + \mathcal{O}(1/M_B^4) \right]$$

Roadmap for Inclusive $|V_{cb}|$

Milestones:

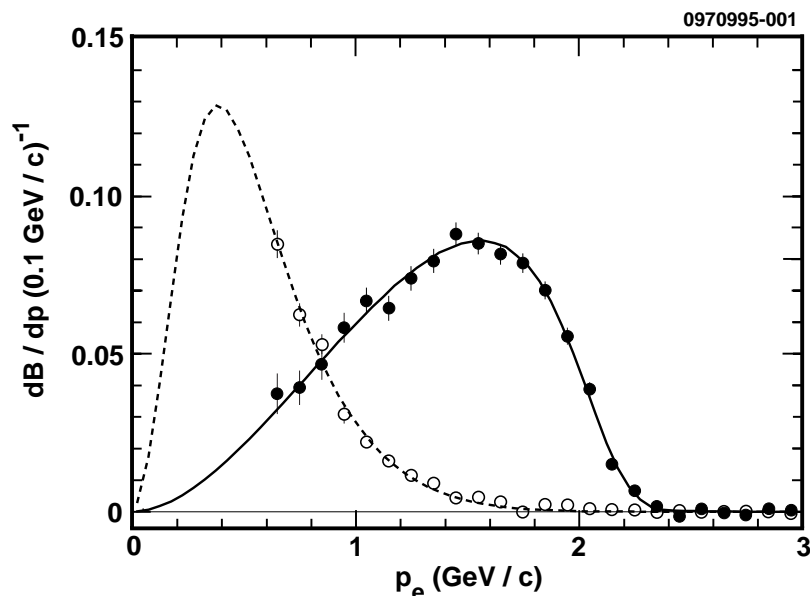
- Theory
 - Expressions for Γ and moments
- Experiment
 - Inclusive branching fraction $\mathcal{B}(B \rightarrow X\ell\nu)$
 - Lifetimes
 - Moments: $\langle E_\gamma \rangle$ in $b \rightarrow s\gamma$, $\langle M_X^2 \rangle$ in $B \rightarrow X_c\ell\nu$

Recent improvements on $|V_{cb}|$ use experimental measurements of theory parameters to bound HQET parameters.

Other improvements come from new branching fraction and lifetime measurements.

Inclusive Semileptonic Branching Fraction

Analyses by CLEO, BABAR, BELLE (ARGUS)



Use high p lepton to tag B
 Measure second lepton
 Separate primary and secondary
 using charge and
 angular correlations

CLEO PRL76 (1996)1570 (2 fb^{-1}) $\mathcal{B}(B \rightarrow X e \nu) = (10.49 \pm 0.17 \pm 0.43)\%$

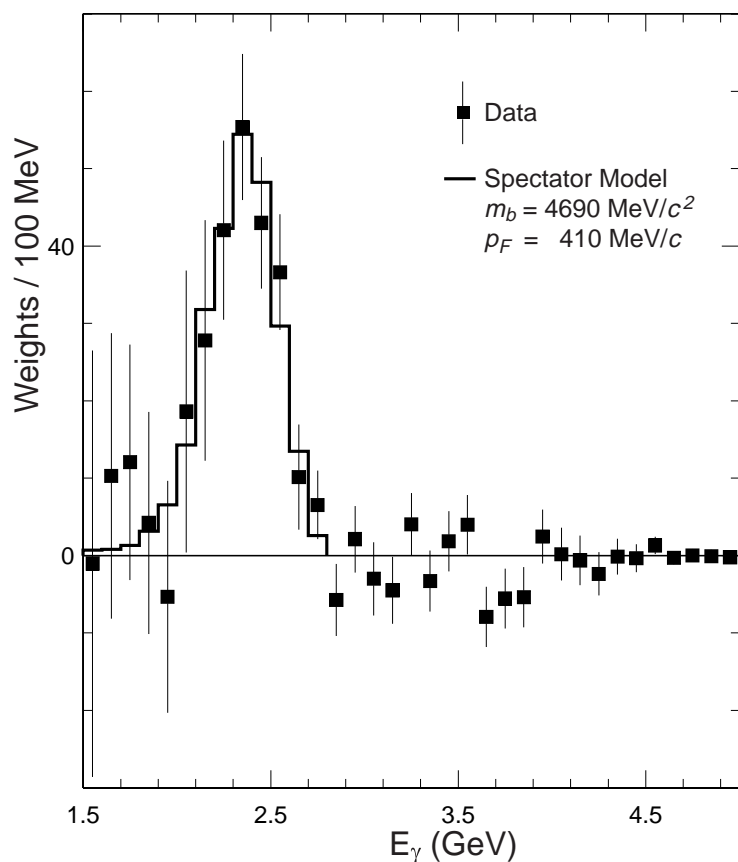
BELLE CONF-0123 (5 fb^{-1}) $\mathcal{B}(B \rightarrow X e \nu) = (10.86 \pm 0.14 \pm 0.47)\%$

BABAR PRELIMINARY (5 fb^{-1}) $\mathcal{B}(B \rightarrow X e \nu) = (10.82 \pm 0.21 \pm 0.38)\%$

Compare to

LEP Avg Working Group $\mathcal{B}(b \rightarrow X l \nu) = (10.59 \pm 0.09 \pm 0.15 \pm 0.26)\%$

$B \rightarrow X_s \gamma: E_\gamma$ Moments



CLEO $b \rightarrow s\gamma$ spectrum

PRL **87**, 251807 (2001) $\langle E_\gamma \rangle \approx m_b/2$

Broadened by

- Fermi motion
- gluon bremsstrahlung
- B boost in lab

Use first moment to determine $\bar{\Lambda}$

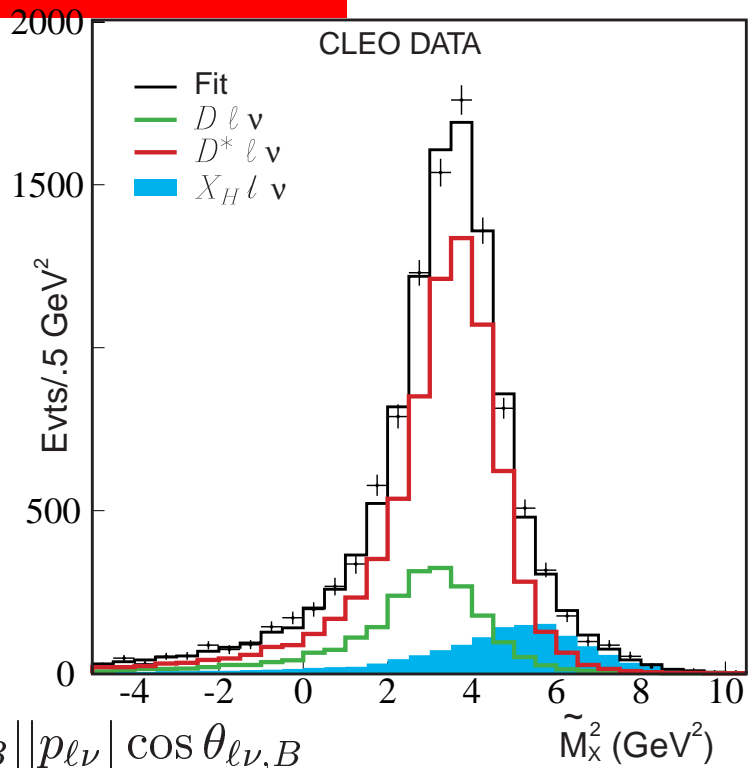
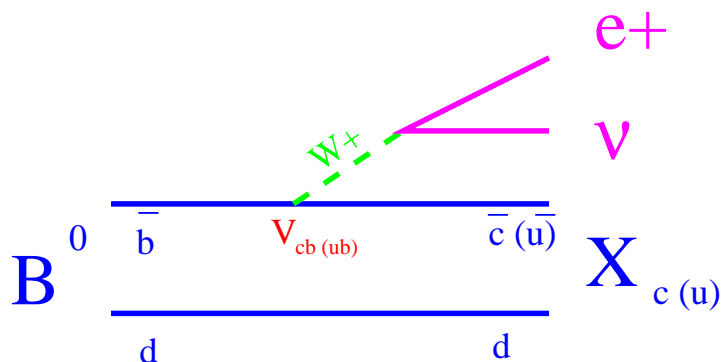
$$\bar{\Lambda} = 0.35 \pm 0.08 \pm 0.10 \text{ GeV}$$

Theory: Bauer PRD57, 5611 (1998)

Ligeti *et al.*, PRD60, 034019 (1999)

$$\begin{aligned} \langle E_\gamma \rangle &= 2.346 \pm 0.032 \pm 0.011 \text{ GeV} \\ \langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle &= 0.0231 \pm 0.0066 \pm 0.0022 \text{ GeV}^2 \end{aligned}$$

$B \rightarrow X_c \ell \nu: M_X^2$ Moments



CLEO PRL 88, 251808 (2001)

Require $E_\ell > 1.5$ GeV

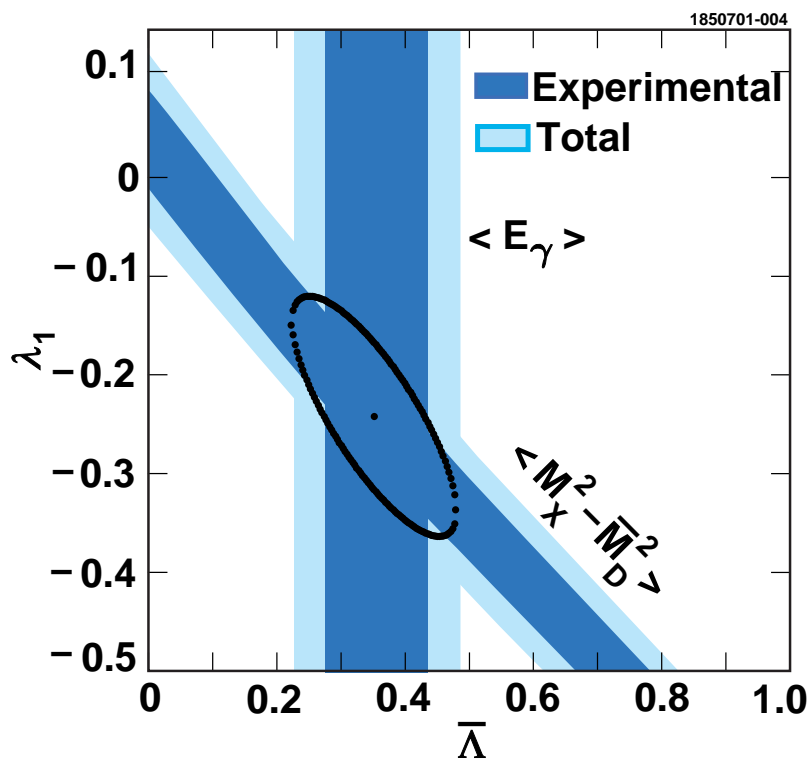
(P_ν, E_ν) from hermetic detector

$$\begin{aligned}
 M_X^2 &= M_B^2 + M_{\ell\nu}^2 - 2E_B E_{\ell\nu} + 2|p_B||p_{\ell\nu}| \cos \theta_{\ell\nu, B} \\
 \approx \widetilde{M}_X^2 &= M_B^2 + M_{\ell\nu}^2 - 2E_B E_{\ell\nu}
 \end{aligned}$$

$$\langle M_X^2 - \overline{M}_D^2 \rangle = 0.251 \pm 0.023 \pm 0.062 \text{ GeV}^2 \quad \text{Spin-average } D \text{ mass: } \overline{M}_D = (M_D + 3M_{D^*})/4$$

$$\langle (M_X^2 - \overline{M}_D^2)^2 \rangle = 0.639 \pm 0.056 \pm 0.178 \text{ GeV}^4$$

Determination of $\bar{\Lambda}$ and λ_1



Using

$$\mathcal{B}(B \rightarrow X_c \ell \nu) = (10.39 \pm 0.46)\%$$

(CLEO $B \rightarrow X_u \ell \nu$ removed)

τ_B (PDG2000)

gives

$$|V_{cb}| = (40.4 \pm 0.5 \pm 0.9 \pm 0.8) \times 10^{-3}$$

(M) (Γ) (T)

3.2% determination of V_{cb}

implicit q-H duality assumption

Work in progress on E_ℓ moments

Consistency?

Stay tuned Summer results expected

from many experiments

$$\bar{\Lambda} = 0.35 \pm 0.07 \pm 0.10 \text{ GeV}$$

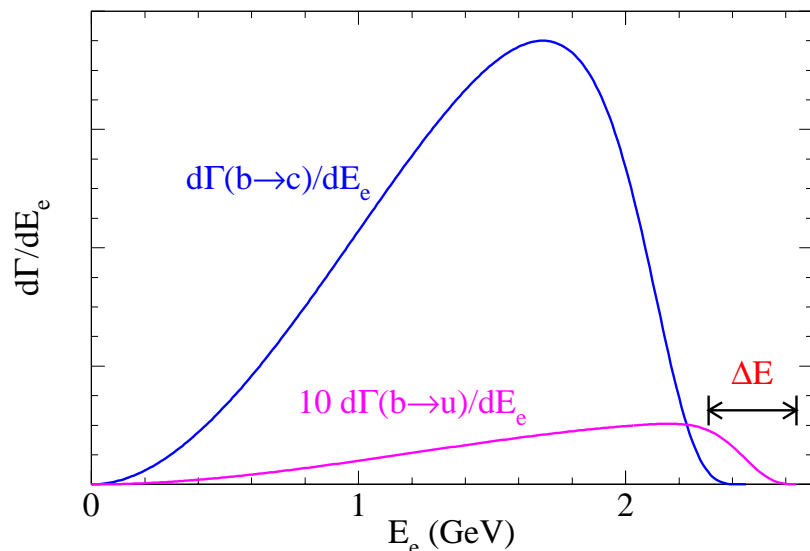
$$\lambda_1 = -0.238 \pm 0.071 \pm 0.078 \text{ GeV}^2$$

Warning: scheme dependence

\overline{MS} to order $1/M^3$, $\beta_0 \alpha_s^2$

Experimental Challenges in $b \rightarrow ul\nu$

From Leibovich hep-ph/0011181



Large $b \rightarrow cl\nu$ backgrounds

- Signal is 1% of background!
- Suppress using kinematics

Approaches:

- Exclusive
 - + Constraints from full recon
- Inclusive
 - + Kinematic cuts
 - $E_\ell > \sim 2.4$ GeV
 - $M_X < M_D$
 - $q^2 > \sim 12$ GeV²

Both approaches currently suffer from large uncertainties

- Exc. Unknown form factors
- Inc. Effect of kinematic cuts

Exclusive $B \rightarrow \pi \ell \nu$ and $B \rightarrow \rho \ell \nu$

Powerful kinematic constraints for full reconstruction ($\Delta E, M_B$)

ν reconstruction using hermiticity of detector:

- $E_{\text{miss}} = 2E_{\text{beam}} - \sum_i E_i$
- $\vec{p}_{\text{miss}} = -\sum_i \vec{p}_i$

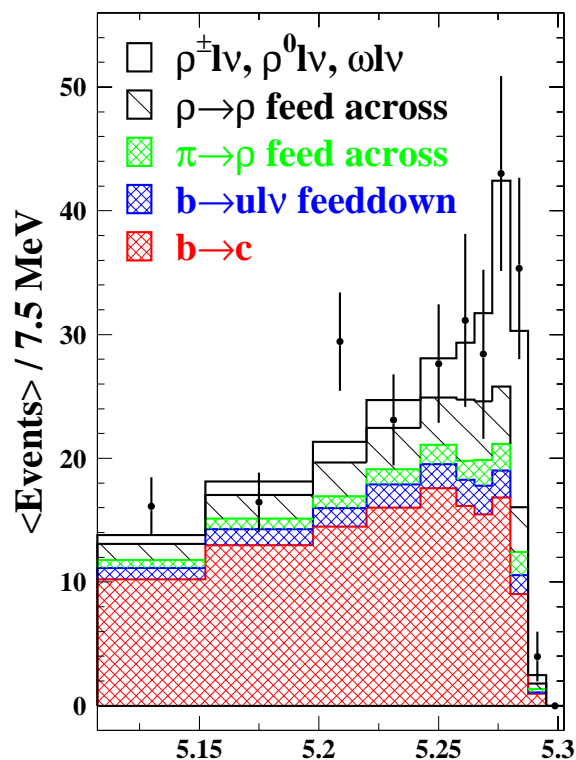
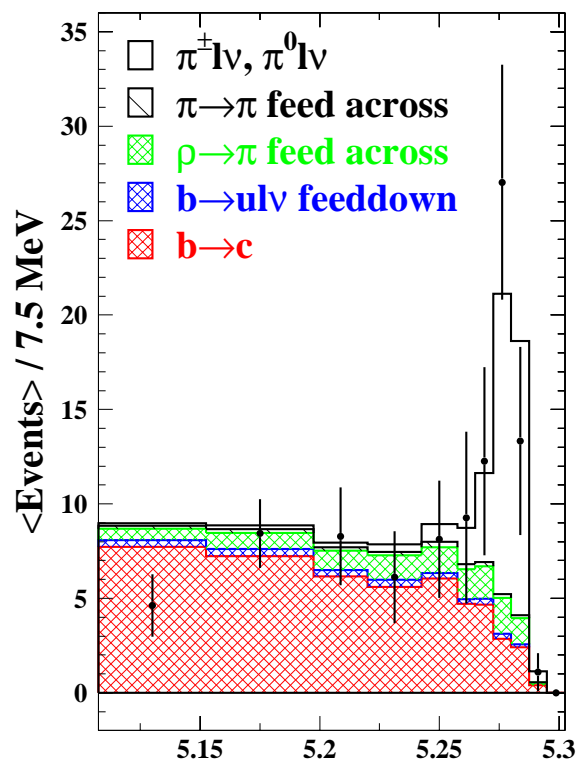
Evaluate \mathcal{B} using form factors and extract $|V_{ub}|$ from

$$\Gamma = \frac{\mathcal{B}}{\tau_B} = \gamma_u |V_{ub}|^2$$

Form factors (and γ) from

- Lattice - *e.g.* UKQCD
- Quark Models - *e.g.* ISGW2, WSB
- Light Cone Sum Rules - *e.g.* Ball and Braun
- HQS - *e.g.* Ligeti and Wise from $D \rightarrow K^* \ell \nu$

CLEO PRL77, 5000(1996) First Observation $\bar{B} \rightarrow \pi \ell \bar{\nu}$ and $\bar{B} \rightarrow \rho \ell \bar{\nu}$



(2.66 fb^{-1})
 $E_\ell > 1.5 \text{ GeV}$
 $S/N \approx 2$
 Isospin constraint

- $\Gamma_{\pi^-} = 2\Gamma_{\pi^0}$
- $\Gamma_{\rho^-} = 2\Gamma_{\rho^0}$

M_{cand} (GeV)

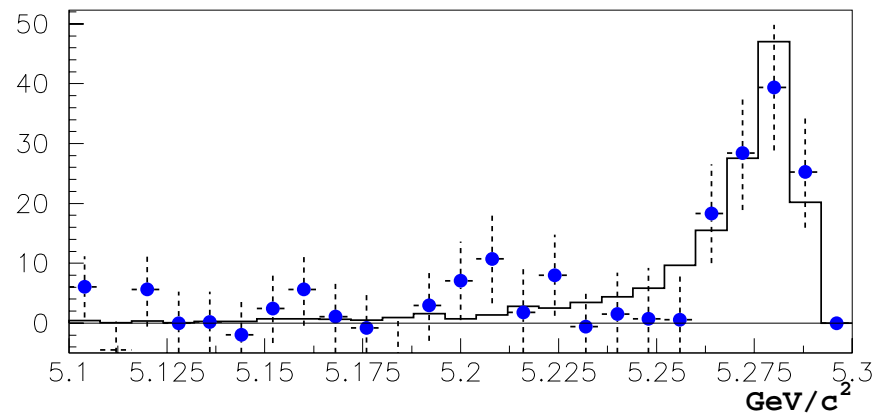
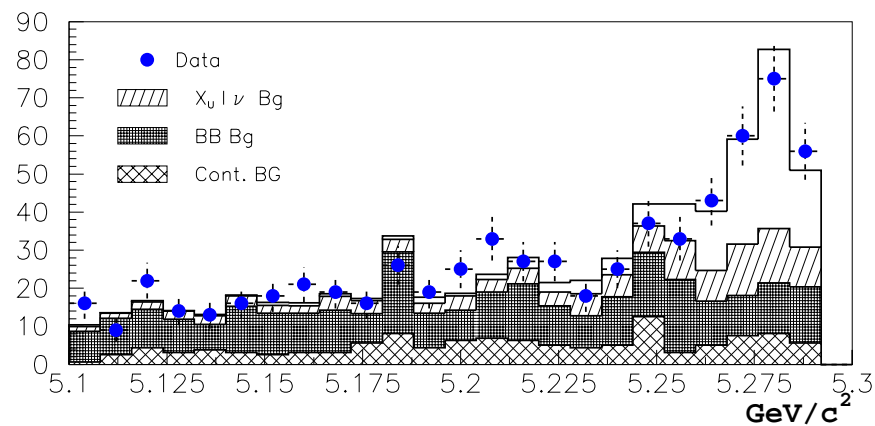
M_{cand} (GeV)

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.8 \pm 0.4 \pm 0.3 \pm 0.2) \times 10^{-4}$$

$$\mathcal{B}(B^0 \rightarrow \rho^- \ell^+ \nu) = (2.5 \pm 0.4_{-0.7}^{+0.5} \pm 0.5) \times 10^{-4}$$

Evaluate $|V_{ub}|$ using five form factors

BELLE-CONF-0124 (2001) $\bar{B} \rightarrow \pi \ell \bar{\nu}$



(21.3 fb⁻¹)

Belle ν reconstruction

$$E_{\text{miss}} = 2E_{\text{beam}} - \sum_i E_i$$

$$\vec{p}_{\text{miss}} = - \sum_i \vec{p}_i$$

$$E_\nu = |\vec{P}_{\text{miss}}| \text{ and } \vec{p}_\nu = \vec{p}_{\text{miss}}$$

Cut $|\Delta E| < 0.3 \text{ GeV}$

Fit M_{bc}

Preliminary

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.28 \pm 0.20 \pm 0.26) \times 10^{-4}$$

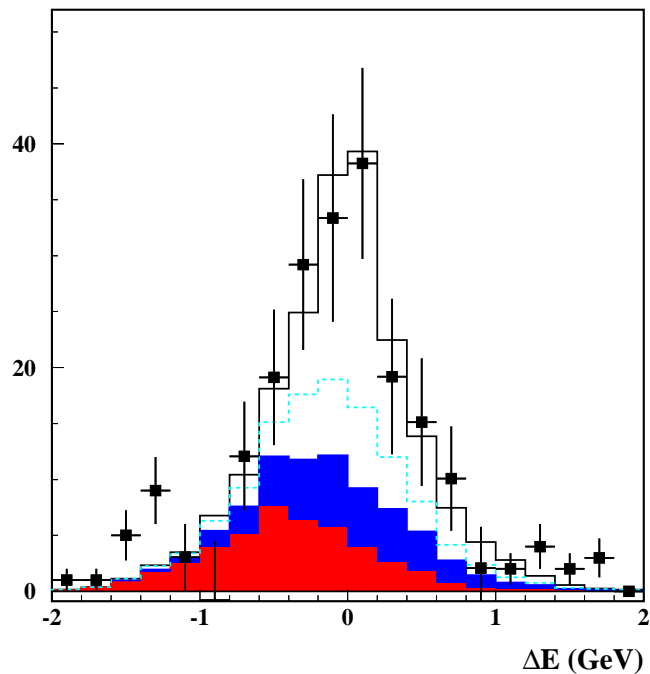
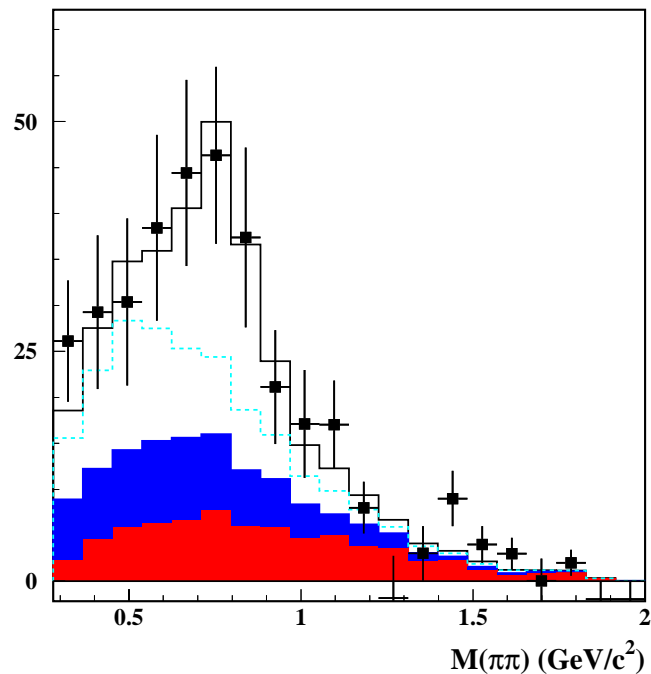
ISGW2 + WSB

Updated at Moriond02 (H. Ishino): 29.2 fb^{-1}
2d-fit to ΔE and p_ℓ

Uses more recent models for form factors

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.89 \pm 0.15 \pm 0.30) \times 10^{-4} \quad \text{LCSR}$$

$$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.92 \pm 0.16 \pm 0.30) \times 10^{-4} \quad \text{UKQCD}$$

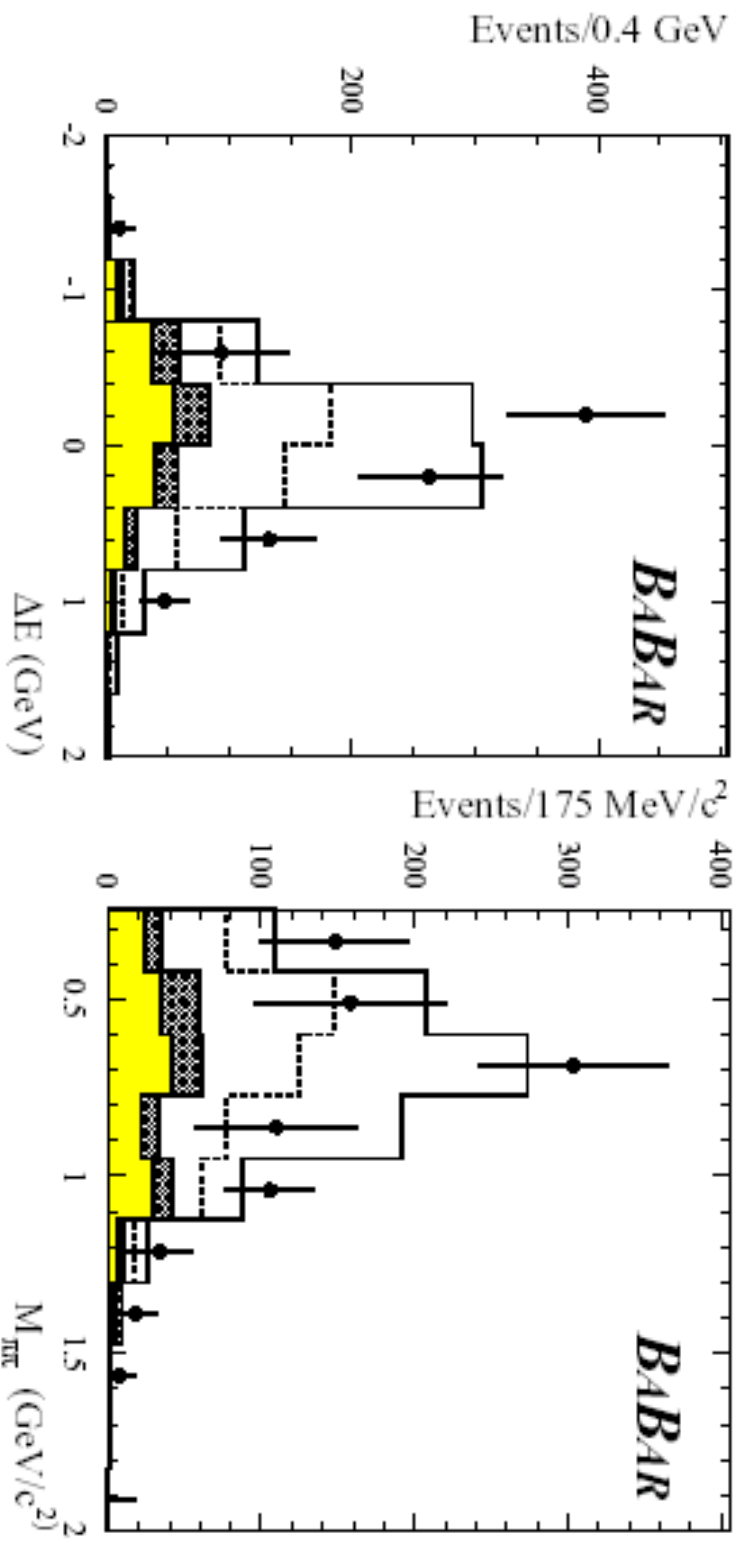
CLEO PRD61, 052001 (2000) $\bar{B} \rightarrow \rho \ell \bar{\nu}$ HILEP ρ modes with $M(\pi\pi)$ cutHILEP ρ modes with ΔE cut

Looser cuts than 1996; 3.1 fb^{-1}

$E_\ell > 1.7 \text{ GeV}$; Most sensitivity for $E_\ell > 2.3 \text{ GeV}$

$$\mathcal{B}(B^0 \rightarrow \rho^- \ell^+ \nu) = (2.69 \pm 0.41_{-0.40}^{+0.35} \pm 0.50) \times 10^{-4}$$

Statistically independent of 1996 analysis

BABAR PRELIMINARY $\bar{B} \rightarrow \rho e \bar{\nu}$ - B. Serfas at CERN CKM Workshop

Uses 20.2 fb^{-1} ; Very similar to CLEO's $\bar{B} \rightarrow \rho l \bar{\nu}$

$$\mathcal{B}(B^0 \rightarrow \rho^- e^+ \nu) = (3.26 \pm 0.65^{+0.63}_{-0.65} \pm 0.44) \times 10^{-4}$$

Exclusive $|V_{ub}|$ Summary

	$\mathcal{B}(B^0 \rightarrow \pi^- \ell^+ \nu)$ $\times 10^{-4}$	$\mathcal{B}(B^0 \rightarrow \rho^- \ell^+ \nu)$ $\times 10^{-4}$
CLEO	$1.8 \pm 0.4 \pm 0.3 \pm 0.2$	$2.5 \pm 0.4_{-0.7}^{+0.5} \pm 0.5$
Belle	$1.28 \pm 0.20 \pm 0.26 \pm ?.??$	$2.69 \pm 0.41_{-0.40}^{+0.35} \pm 0.5$
BaBar		$3.26 \pm 0.65_{-0.65}^{+0.63} \pm 0.44$

CLEO Combined:

$$|V_{ub}| = (3.25 \pm 0.14_{-0.29}^{+0.21} \pm 0.55) \times 10^{-3}$$

- Limited by knowledge of form factors
- Lattice calculations can help
- Updates coming from all experiments

Inclusive $\bar{B} \rightarrow X_u \ell \bar{\nu}$

Extract $|V_{ub}|$ from measured branching fraction using OPE

$$|V_{ub}| = 0.00445 \left[\frac{\mathcal{B}(B \rightarrow X_u \ell \nu) 1.55 \text{ ps}}{0.002 \tau_B} \right]^{\frac{1}{2}} (1.0 \pm 0.020 \pm 0.052)$$

Uncertainties from **OPE** and **b quark mass (± 90 MeV)**

Hoang *et al.* (1999) and Uraltsev *et al.* (1998)

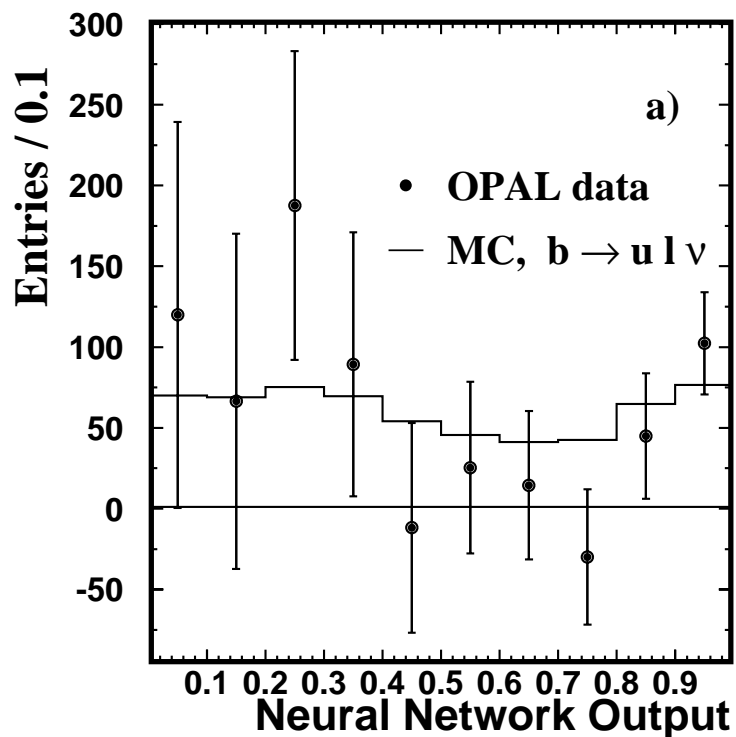
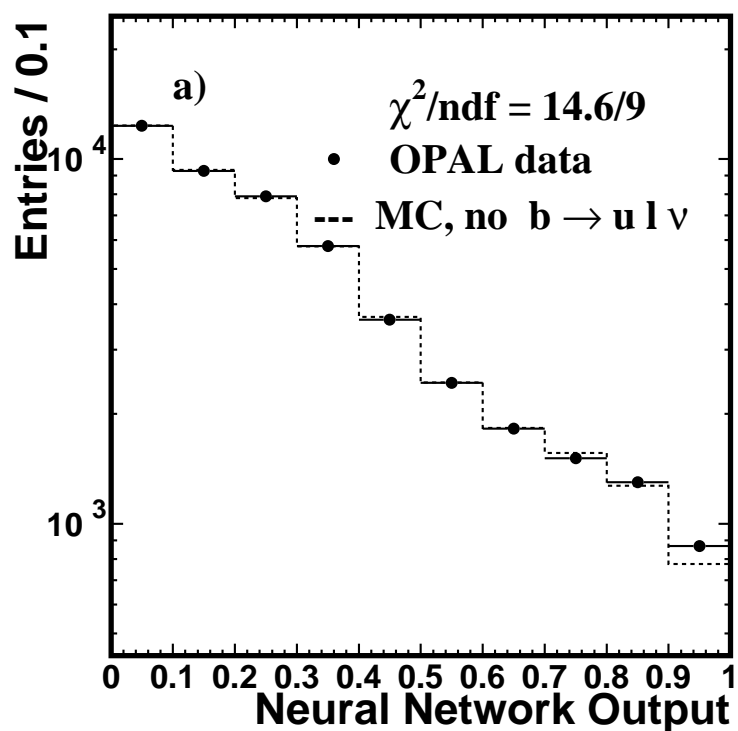
Different strategies for beating down the background

Choice of Kinematic Cuts

- $E_\ell > \sim 2.4$ GeV (keeps about 5–10% of $b \rightarrow u \ell \nu$)
- $q^2 > \sim 12$ GeV² (keeps about 20%)
- $M_X < M_D$ (keeps about 70%)

But these cuts introduce additional uncertainties

OPAL EPJ C21 (2001) 399

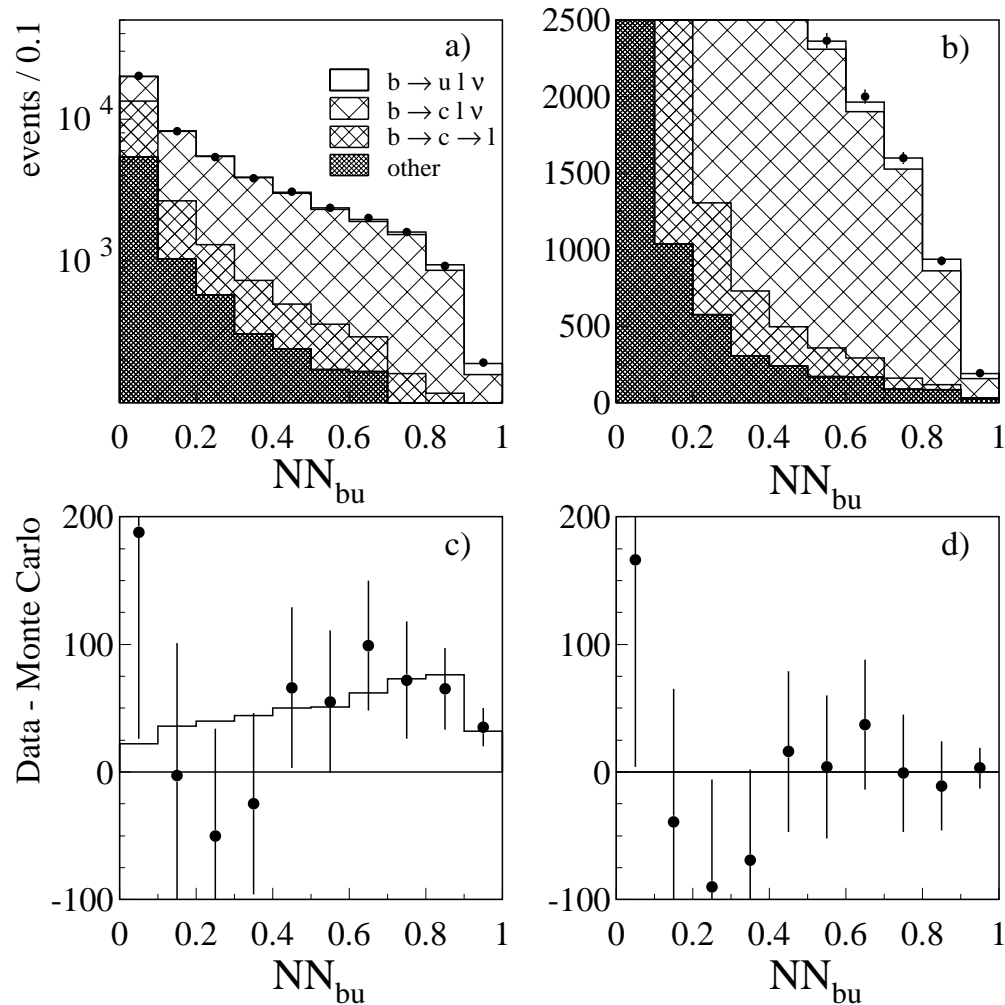


Huge background suppressed with 7 variable Neural Net

Small signal extraction depends on $b \rightarrow c l \nu$ model! $S/B = 0.05$

ALEPH EPJ C6 (1999) 555

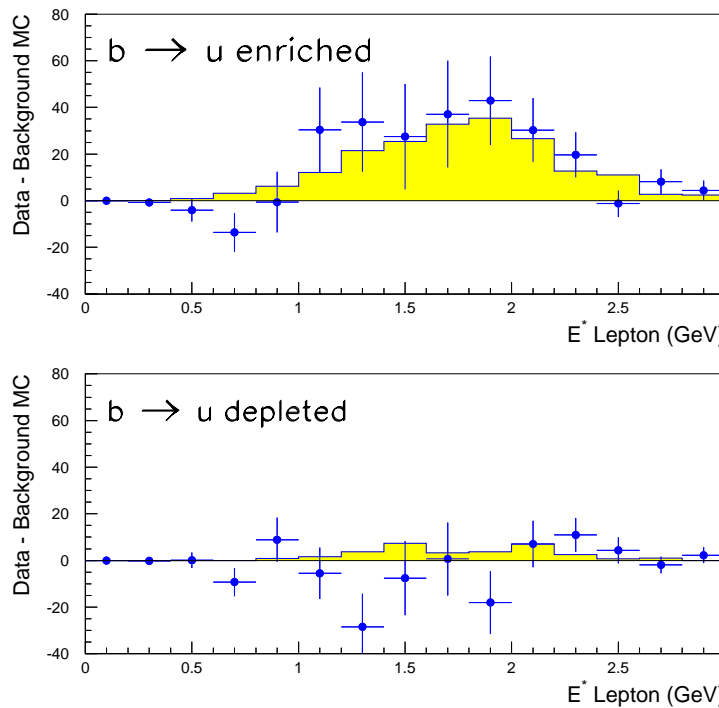
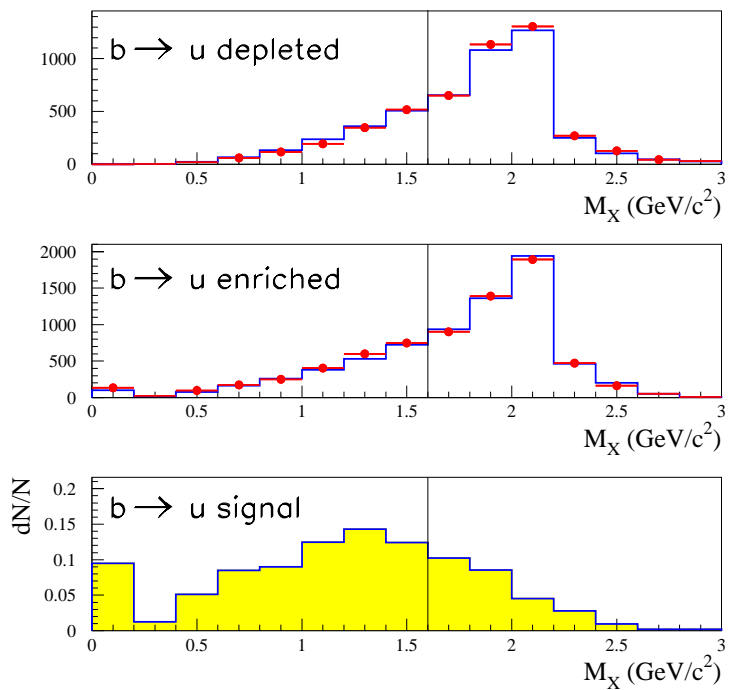
ALEPH



20 variable NN

$S/B = 0.07$

DELPHI PLB 478 (2000) 14

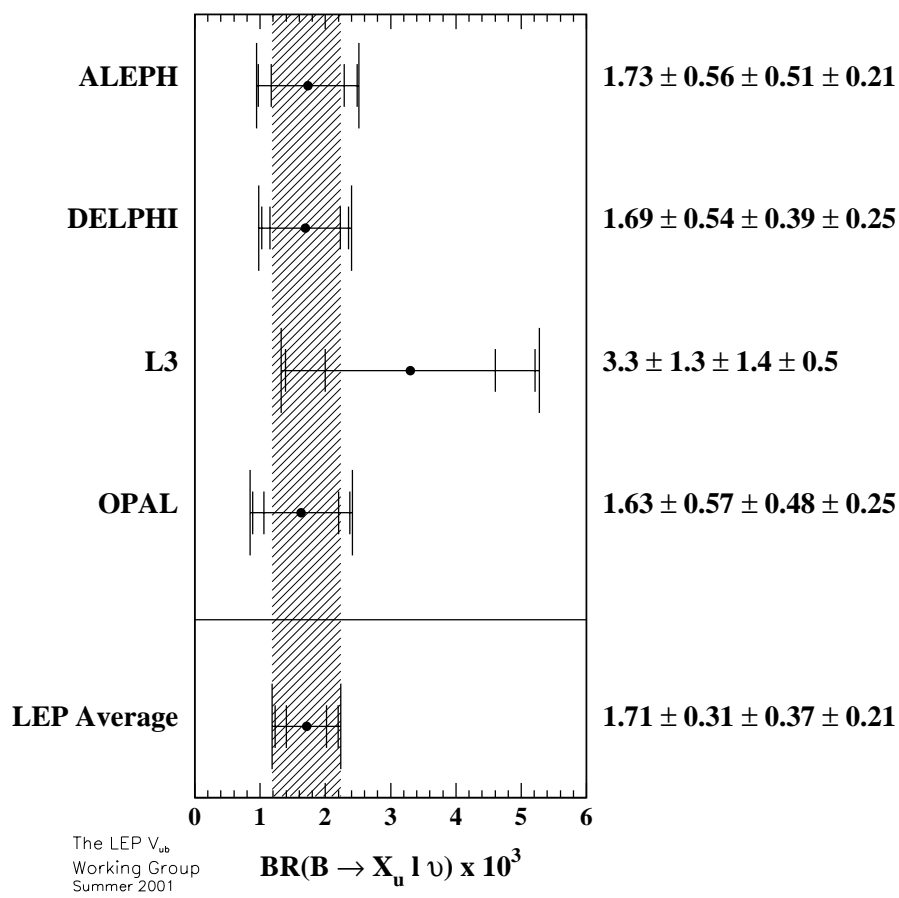


Use charm vertex to suppress bkgd

$M_X < 1.6$ signal region

$S/B = 0.10$

Inclusive $|V_{ub}|$ - LEP Summary



LEP $|V_{ub}|$ Working Group

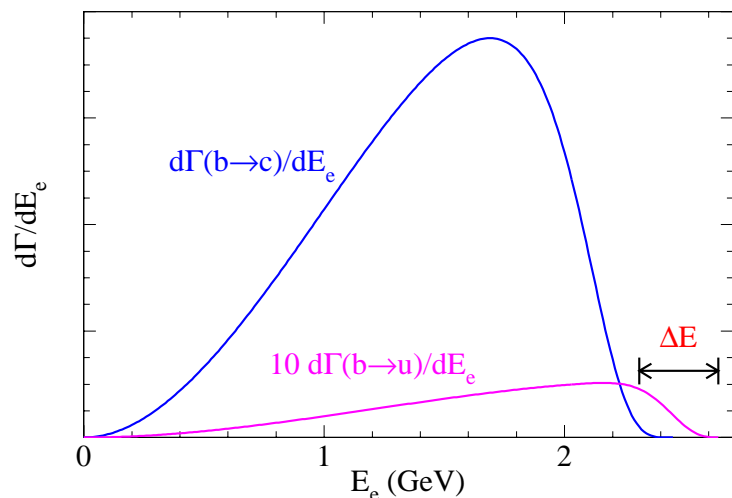
$|V_{ub}|$ from lepton spectrum and $b \rightarrow s\gamma$

To measure $b \rightarrow u\ell\nu$

Must suppress $b \rightarrow c\ell\nu$

Cutting on E_ℓ introduces problems:

- Large model dependence
(What fraction above cut?)
- At edge of spectrum
sensitive to b quark motion



Idea:¹ Reduce problems by using $b \rightarrow s\gamma$ photon spectrum

Common shape function for $b \rightarrow$ light transitions (to leading order)

Tells how to smear from $b \rightarrow s\gamma$ to $B \rightarrow X_s\gamma$ and $b \rightarrow u\ell\nu$ to $B \rightarrow X_u\ell\nu$

¹(Neubert, Kagan, De Fazio ; Leibovich, Low, Rothstein)

$|V_{ub}|$ from lepton spectrum and $b \rightarrow s\gamma$

Measure $B \rightarrow X_u \ell \nu$ in a lepton momentum interval (p) at the $\bar{B} \rightarrow X \ell \bar{\nu}$ endpoint

- $\Delta\mathcal{B}_{ub}(p)$ is the branching fraction for $B \rightarrow X_u \ell \nu$ in (p),
- $f_u(p)$ is the fraction of the $B \rightarrow X_u \ell \nu$ spectrum in (p), and
- $\mathcal{B}_{ub} \equiv \mathcal{B}(B \rightarrow X_u \ell \nu)$ is the $B \rightarrow X_c \ell \nu$ branching fraction.

New measurement of $f_u(p)$

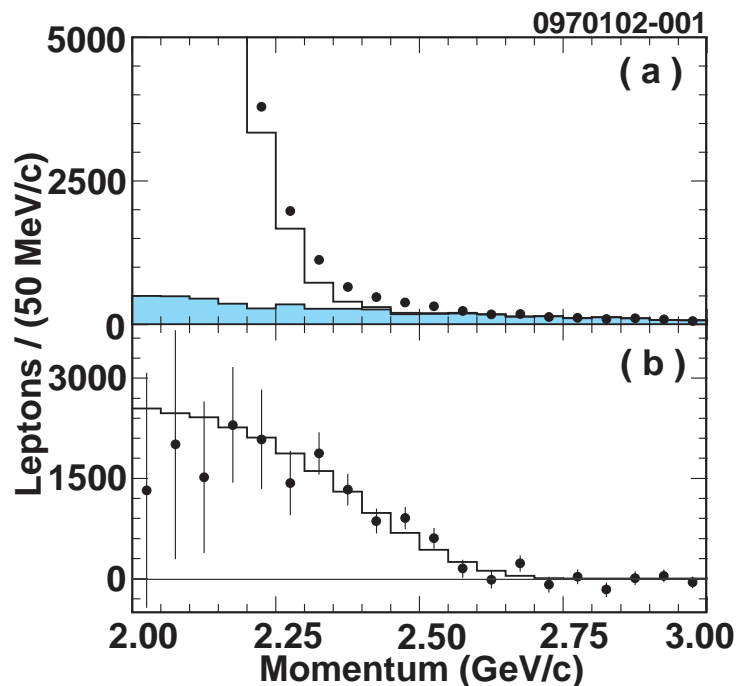
- fit $b \rightarrow s\gamma$ data to a shape function (Kagan-Neubert)
- use shape parameters to determine $f_u(p)$ (De Fazio-Neubert)

Then get \mathcal{B}_{ub} from $\Delta\mathcal{B}_{ub}(p) = f_u(p)\mathcal{B}_{ub}$ and obtain $|V_{ub}|$ from

$$|V_{ub}| = \left[(3.07 \pm 0.12) \times 10^{-3} \right] \times \left[\frac{\mathcal{B}_{ub}}{0.001} \frac{1.6 \text{ ps}}{\tau_B} \right]^{\frac{1}{2}}$$

(Hoang-Ligeti-Manohar) (Bigi-Uraltsev-Shifman-Vainshtein)

$|V_{ub}|$ from lepton spectrum and $b \rightarrow s\gamma$



In ($2.2 < p_\ell < 2.6$) GeV/ c

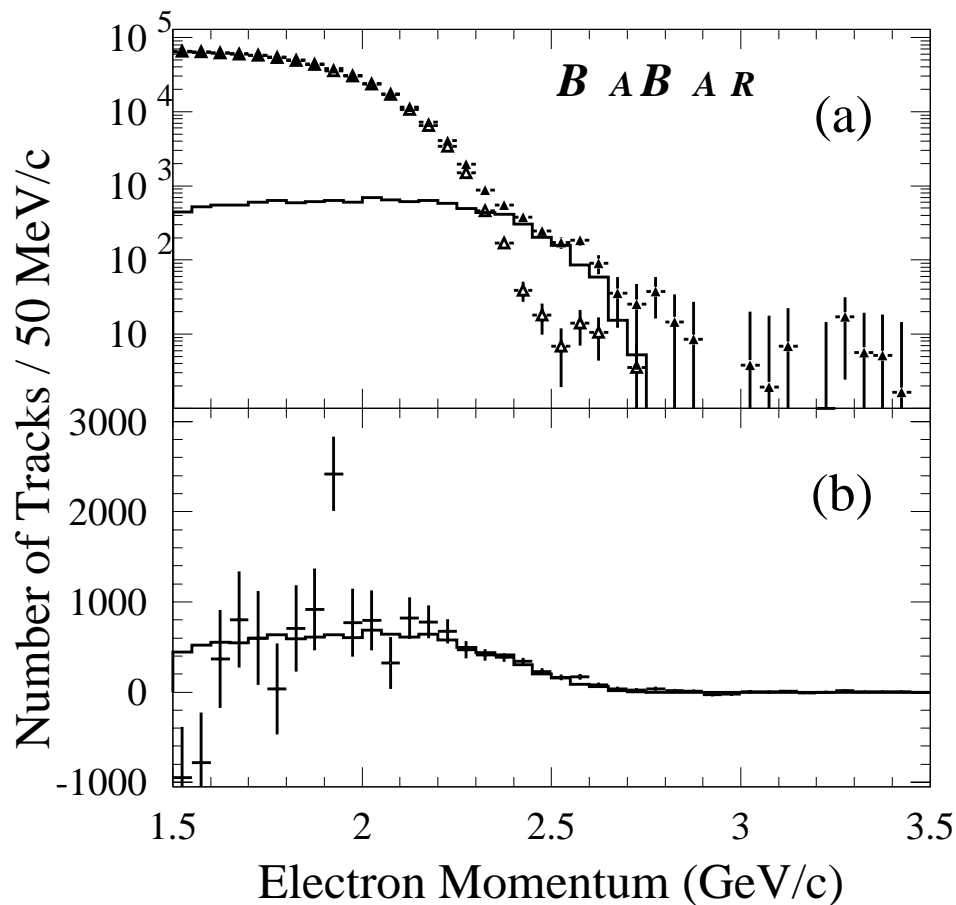
- suppress and subtract $q\bar{q}$
- subtract $B \rightarrow X_c \ell \nu$ yield
- $N_{ub} = 1901 \pm 122 \pm 256$
 $B \rightarrow X_u \ell \nu$ events
- $\Delta B_{ub} = (2.35 \pm 0.15 \pm 0.35) \times 10^{-4}$
- From the $b \rightarrow s\gamma$ spectrum
 $f_u = 0.130 \pm 0.024 \pm 0.015$

Improvement on f_u from use of $b \rightarrow s\gamma$ spectrum –
knowledge of non-perturbative QCD in B to light decays

$$|V_{ub}| = (4.08 \pm 0.34_{\text{exp}} \pm 0.44_{f_u} \pm 0.16_{\Gamma} \pm 0.24_{\Lambda/M_B}) \times 10^{-3}$$

Improved 15% uncertainty CLEO hep-ex/0202019 (to appear in PRL)

BABAR lepton endpoint PRELIMINARY



(20.6 fb⁻¹)

Similar to CLEO (9.1 fb⁻¹)

Less Off- $\Upsilon(4S)$ data

(2.6 fb⁻¹ vs 4.35 fb⁻¹)

Fit $q\bar{q}$ to subtract

solid=data open= $B\bar{B}$ bkgd

hist= $b \rightarrow ul\nu$ ISGW2

$$\Delta B_{ub}(2.3-2.6 \text{ GeV}/c) = (0.152 \pm 0.014 \pm 0.014) \times 10^{-3}$$

Good agreement with CLEO $\Delta B_{ub} = (0.143 \pm 0.010 \pm 0.014) \times 10^{-3}$

Summary and Outlook

$|V_{cb}|$

- agreement(?) inclusive and exclusive techniques sub 5%
- data in hand at B factories to put our understanding to the test
- Exclusive Future
 - unquenched lattice for $\mathcal{F}(1)$
 - data on form factor R_1 , R_2 , shape
- Inclusive Future
 - new \mathcal{B} , τ from Belle and Babar
 - looks promising but need confirmation with more moments
 - E-moments in the summer

$|V_{ub}|$

- again good agreement on inclusive and exclusive 15–20%
- Exclusive Future
 - More statistics from Belle, Babar, CLEO
 - Lattice form factor for $\pi\ell\nu$
- Inclusive Future
 - better shape function from $b \rightarrow s\gamma$ statistics
 - use of M_X and q^2 cuts - is there agreement?
 - better control of theory uncertainties?
 - higher twist corrections to shape function?
 - better $b \rightarrow c\ell\nu$ improves $b \rightarrow u\ell\nu$

Many improvements in understanding to come with B factory data.

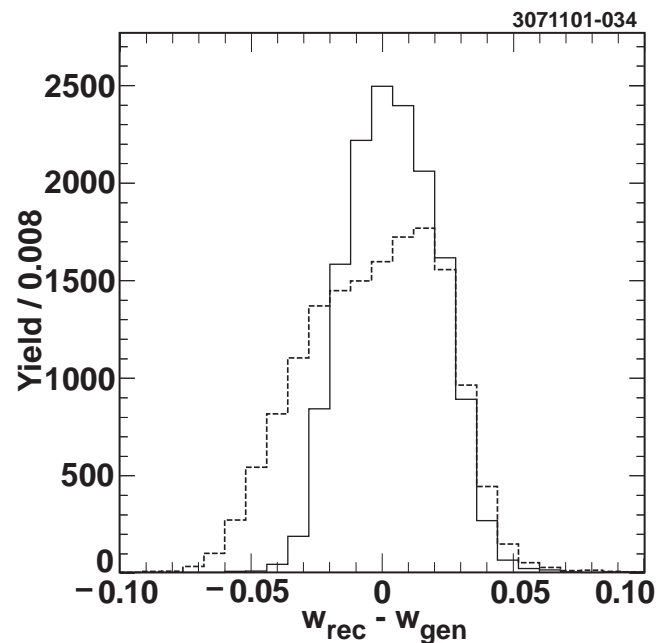
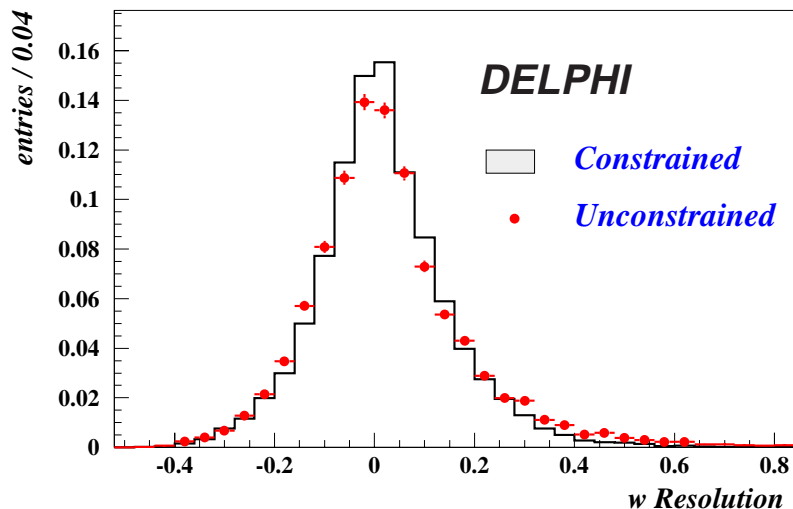
Backup Slides

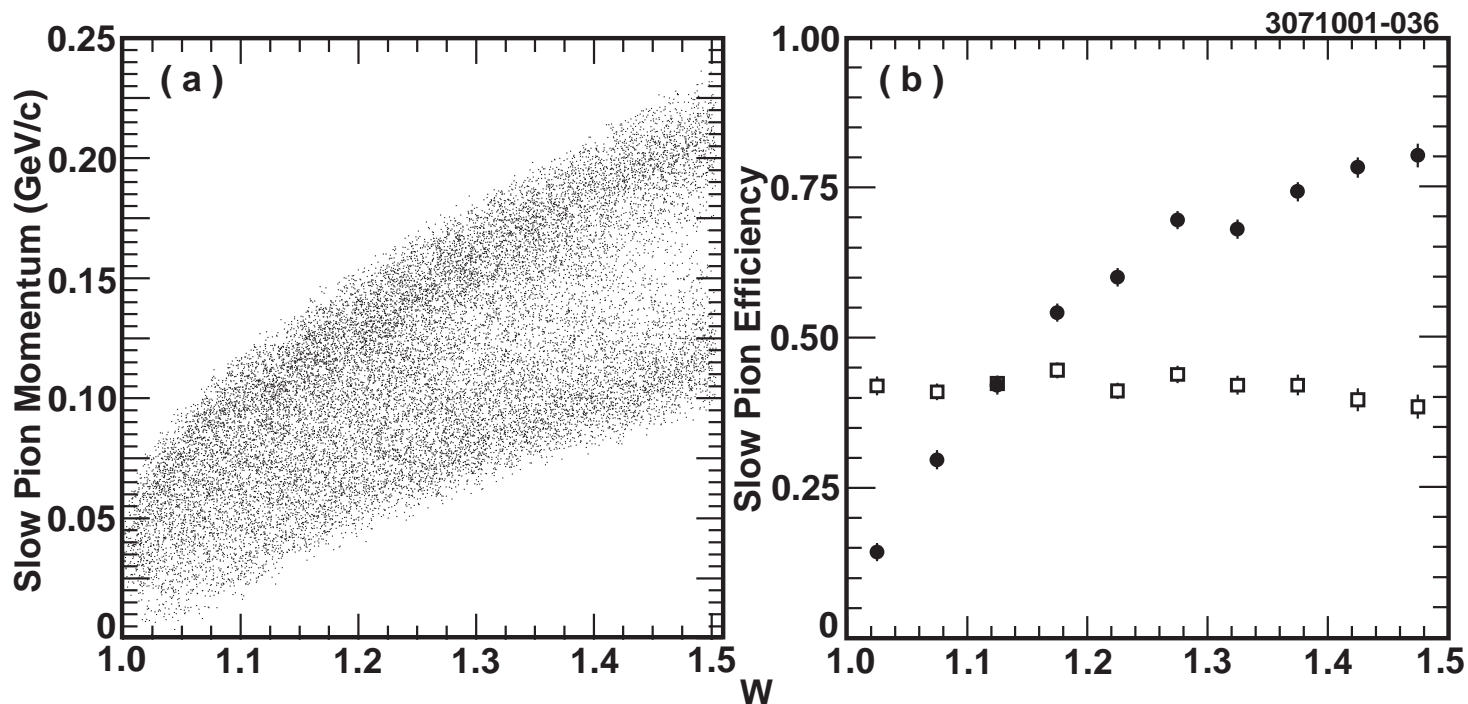
$D^* \ell \nu$ at $\Upsilon(4S)$ and Z Experiments

Main differences arise from B momentum in lab frame:

At LEP $p_B \sim 30 \text{ GeV}/c$; At $B\bar{B}$ threshold $p_B \sim 0.3 \text{ GeV}/c$

- w is boost of D^* in B rest frame
- LEP resolution on $\sigma_w \sim 0.07\text{--}0.14$ compared to $\sigma_w \sim 0.03$ at $4S$



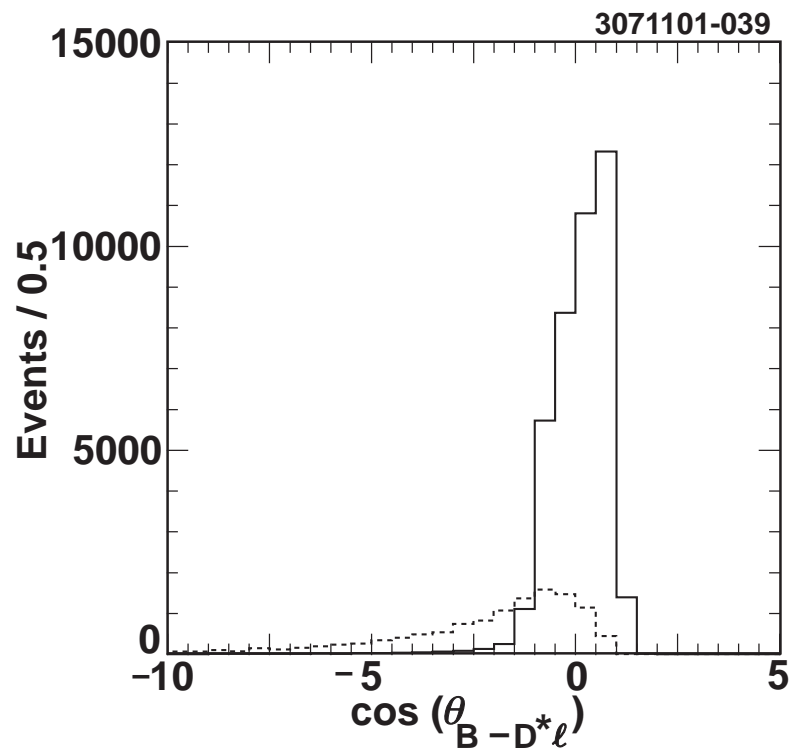


- 4S experiments suffer from π efficiency turn on

At LEP Efficiency is flat

- In $D^{*+} \rightarrow D^0\pi^+$ the π momentum comes from the boost of the D^*
- Low efficiency below 0.05 MeV - precisely most interesting events for extrapolation to $w=1$.
- Does not apply to $D^{*0} \rightarrow D^0\pi^0$; π^0 efficiency is flat.

- LEP expts. have more exposure to $B \rightarrow D^* X \ell \nu$
 - poorer missing mass resolution – 4S can separate sig/bkgd
 - larger systematic from poorly known $B \rightarrow D^{**} \ell \nu$ and non-resonant $B \rightarrow D^* \pi \ell \nu$ modes



CLEO fits $D^* X \ell \nu$ systematic=0.3%

BELLE cuts systematic=1.2%

LEP systematic=1.2–5%