

Measurement of Relative Fragmentation Fractions of B Hadrons at CDF



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Recent B Physics Results from CDF

B_s mixing



Brashly alluring

B fragmentation fractions



Demure, but charming

Outline

- ❑ B fragmentation overview
- ❑ Semileptonic signal reconstruction
- ❑ Semileptonic sample composition
- ❑ Reconstruction efficiencies
- ❑ Fit for fragmentation fractions
- ❑ Fragmentation fraction results
- ❑ Outlook

Outline

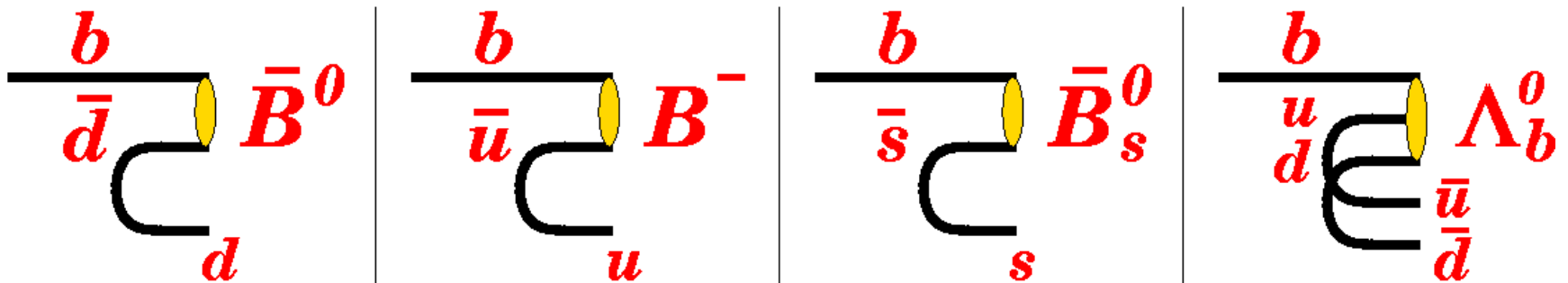
- B fragmentation overview
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B Physics at Tevatron

- Reconstruct all flavors of B hadrons
 - $B_d^0, B_u^+, B_s^0, B_c^+, \Lambda_b^0$
 - Contrast to B factories, Y(4S) [Y(5S)]
 - $B_d^0, B_u^+ [B_s^0]$
- Large dataset of B hadrons
 - $\sim 1 \text{ fb}^{-1}$ data available for B measurements
 - Very large production cross-section makes Tevatron competitive w/B factories
 - Make exciting new measurements
 - B_s mixing (1 fb^{-1})
 - Refine older measurements
 - B fragmentation fractions (360 pb^{-1})

B Fragmentation

- Probability of b quark hadronizing with an anti-quark or a di-quark pair
 - $f_q \equiv \mathcal{B}(b \rightarrow B_q)$
- Many models for heavy flavor fragmentation
 - Petersen, Lund, ...
- B fragmentation fractions inherently empirical
 - Include B^* , B^{**} in fragmentation fractions



Why Fragmentation Fractions?

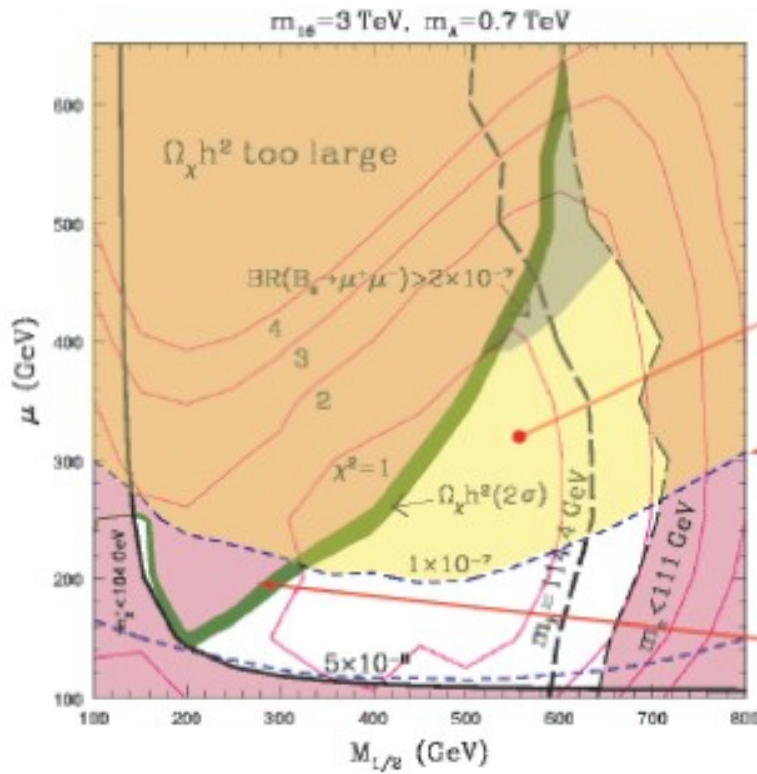
□ Search for $B_s \rightarrow \mu^+ \mu^-$

■ $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = f_u/f_s \times \mathcal{B}(B^+ \rightarrow J/\psi K^+) \times \dots$

■ Improvement in limit @95% CL if

□ Reduce uncertainty on f_s/f_d

□ f_s/f_d at Tevatron is higher than world average...



e.g., Dermisek et al., [hep-ph/0507233](https://arxiv.org/abs/hep-ph/0507233)
dark matter and $S(10)$ with soft SUSY breaking,
other experimental constraints

Excluded at 95% CL! (CDF Limit)

Contour of equal $Br(B_s \rightarrow \mu^+ \mu^-)$

Allowed by dark matter constraints

Fragmentation Fraction Status

□ Measured many times before

■ LEP (ALEPH, DELPHI, OPAL)

□ $f_u, f_d, f_s, f_{b\text{-baryon}}$

□ e^+e^- collisions

□ $p_T(b) \sim 40 \text{ GeV}/c$

□ $f_s/(f_u+f_d) = 0.109 \pm 0.026$

2004 PDG,
dominated by LEP

■ Tevatron

□ $f_u/f_d, f_s/(f_u+f_d), f_{\Lambda b}/(f_u+f_d)$

□ $p\bar{p}$ collisions

□ $p_T(b) \sim 10\text{-}15 \text{ GeV}/c$

□ CDF Run I: $f_s/(f_u+f_d) = 0.213 \pm 0.038$

Average between two CDF
Run I results

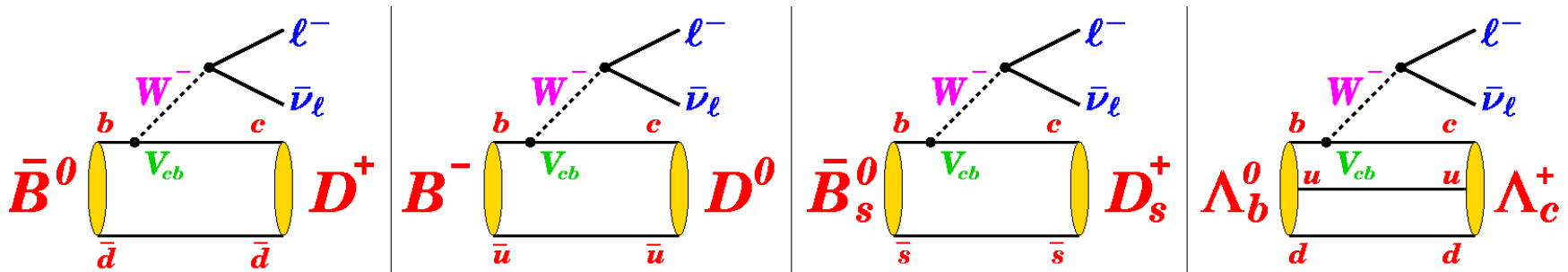
B Fragmentation Intrigue

- Other ~ 2.5 sigma discrepancies observed between LEP and CDF Run I
 - $\bar{\chi} = f_d \chi_d + f_s \chi_s$
 - 0.118 ± 0.005 average measured at LEP
 - 0.152 ± 0.013 measured at CDF Run I (110 pb⁻¹)
 - The discrepancies could be due to
 - New physics present in $p\bar{p}$ collisions
 - **OR** f_s is simply higher at Tevatron
 - **OR** just fluctuations, etc...

Note: PDG 2004 calculates $f_s/(f_u+f_d) = 0.134 \pm 0.014$ when $\bar{\chi}$ constraints are included

B Frag. Fractions in Run II

- Use method similar to Run I measurement
 - Reconstruct five semileptonic B signals
 - $\ell^- D^+, \ell^- D^0, \ell^- D^{*+} (\rightarrow D^0 \pi^+), \ell^- D_s^+, \ell^- \Lambda_c^+$ ($\ell = e, \mu$)
 - Relate to parent B hadrons
 - $\bar{B}_d^0, B_u^-, \bar{B}_s^0, \Lambda_b^0$
 - Cross-talk from excited charm states makes life complicated!

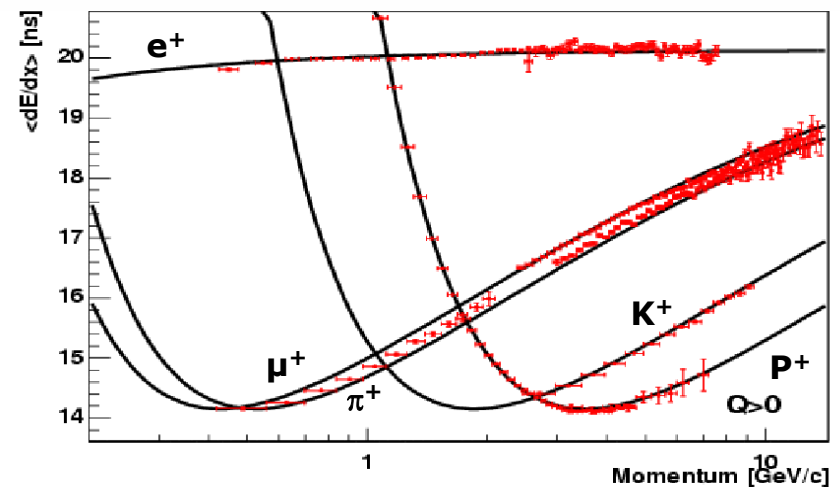
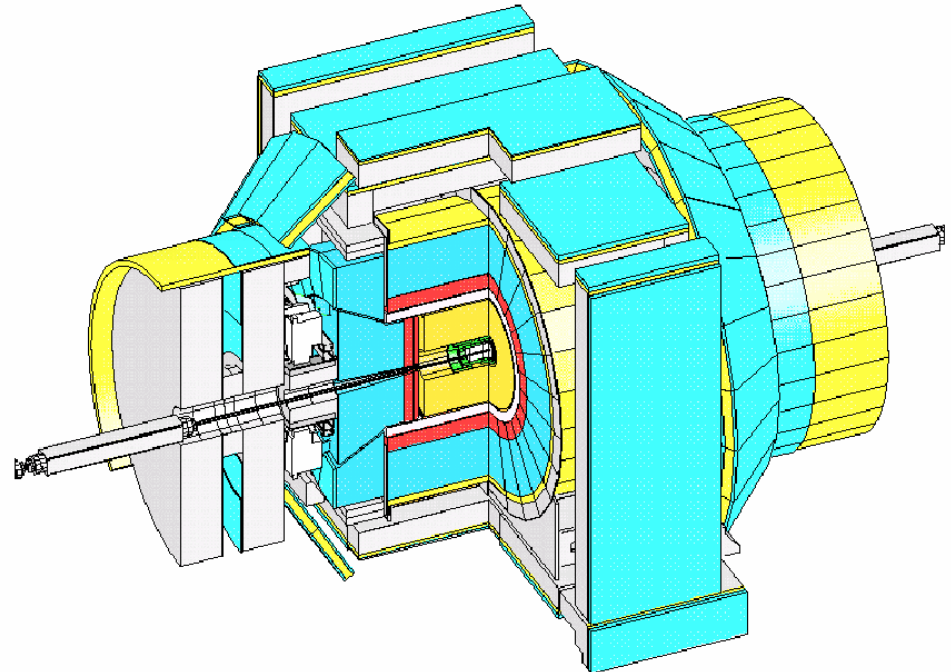


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CDF Detector

- Tracking chamber
 - Eight layers of silicon
 - Precision detection of displaced tracks
 - Drift Chamber
 - dE/dx
- Lepton Identification
 - Electromagnetic Calorimeter
 - Hadronic Calorimeter
 - Muon chambers



SVT

- ❑ Hardware trigger
- ❑ Can trigger on displaced tracks in Run II
 - Allows for accumulation of large sample of B events
 - Uses information from
 - ❑ Drift chamber (XFT)
 - ❑ Silicon detector



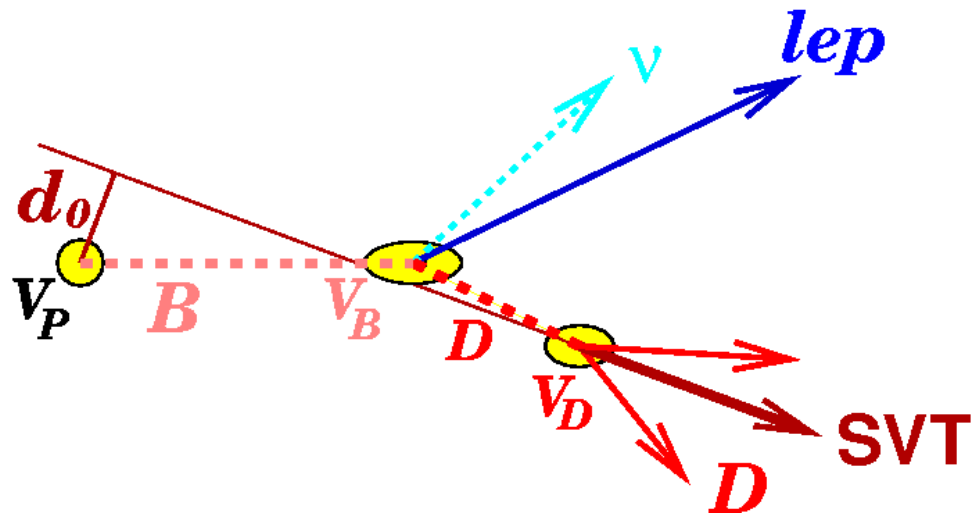
Semileptonic B Trigger

□ New ℓ +SVT trigger in Run II

- $p_T(\ell) > 4 \text{ GeV}/c$
- $p_T(\text{SVT}) > 2 \text{ GeV}/c$
- $120 \text{ }\mu\text{m} < d_0(\text{SVT}) < 1 \text{ mm}$
- $m(\ell, \text{SVT}) < 5 \text{ GeV}/c^2$

□ Run I trigger

- $p_T(\ell) > 8 \text{ GeV}/c$

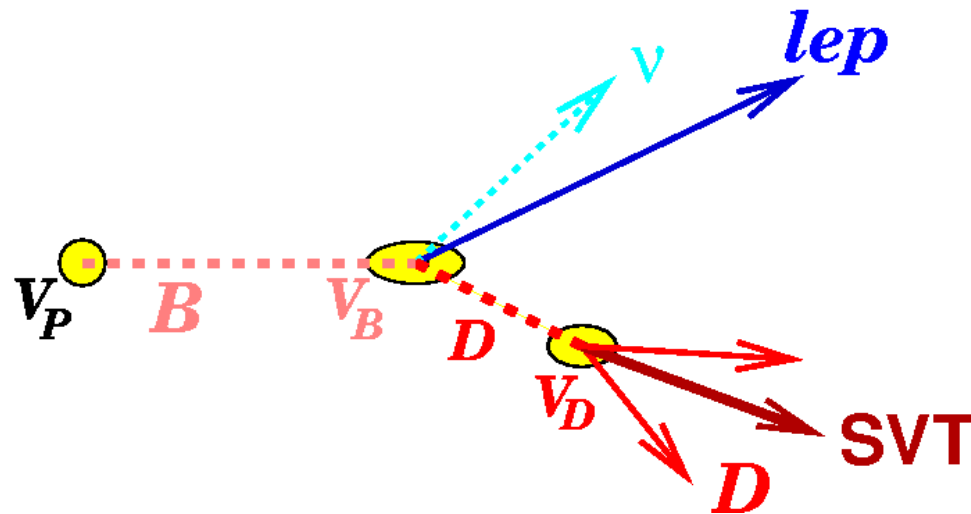


ℓ +Charm Reconstruction

□ Reconstruct 5 charm signals

- $D^+ \rightarrow K^- \pi^+ \pi^+$
- $D^0 \rightarrow K^- \pi^+$
- $D^{*+} \rightarrow D^0 \pi^+$
- $D_s^+ \rightarrow \phi \pi^+, \phi \rightarrow K^- K^+$
- $\Lambda_c^+ \rightarrow p K^- \pi^+$
- Require one of charm tracks be SVT track
- Require a trigger lepton in vicinity of charm hadron

□ Vertex charm hadron with trigger lepton



Signal Selection

□ Cut on quantities which distinguish B decays

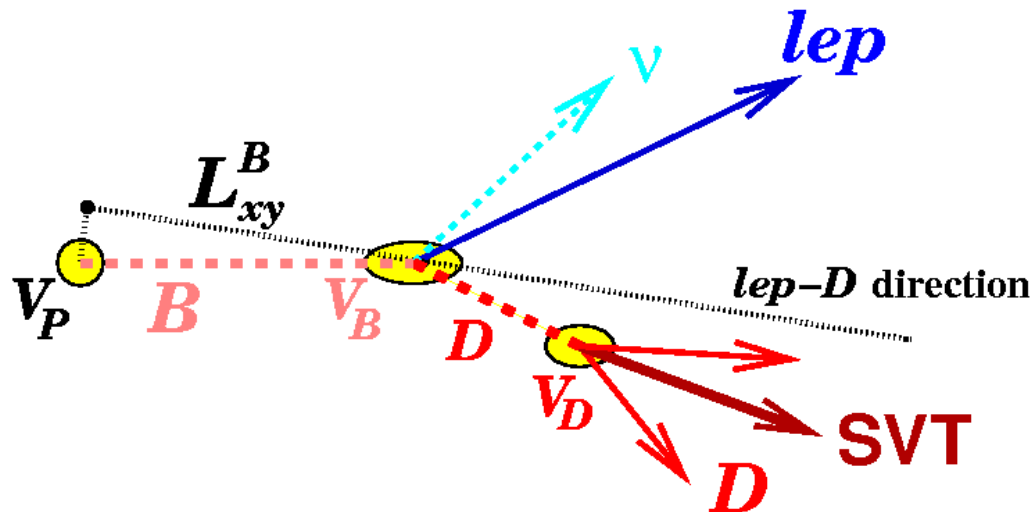
- $ct^*(\ell D) = L_{xy}(P.V. \rightarrow \ell D) \cdot m(B) / p_T(\ell D) > 200 \mu\text{m}$

- Inconsistent with being prompt

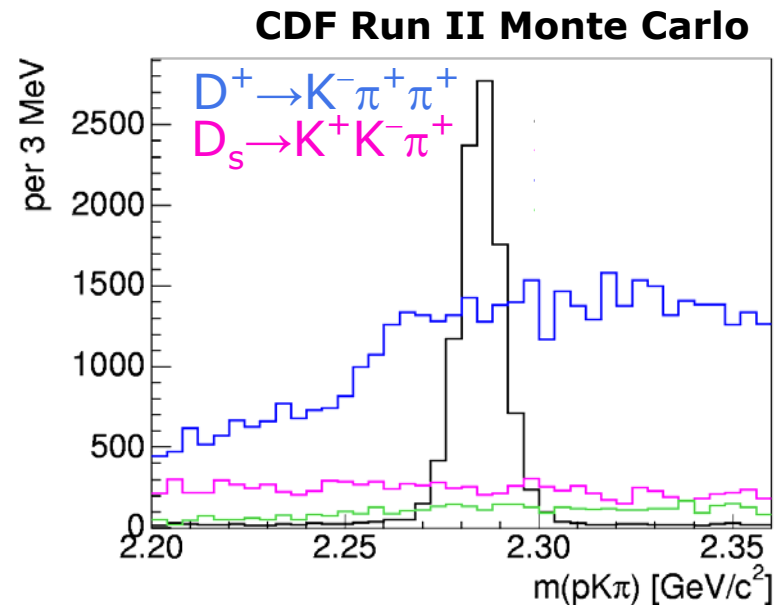
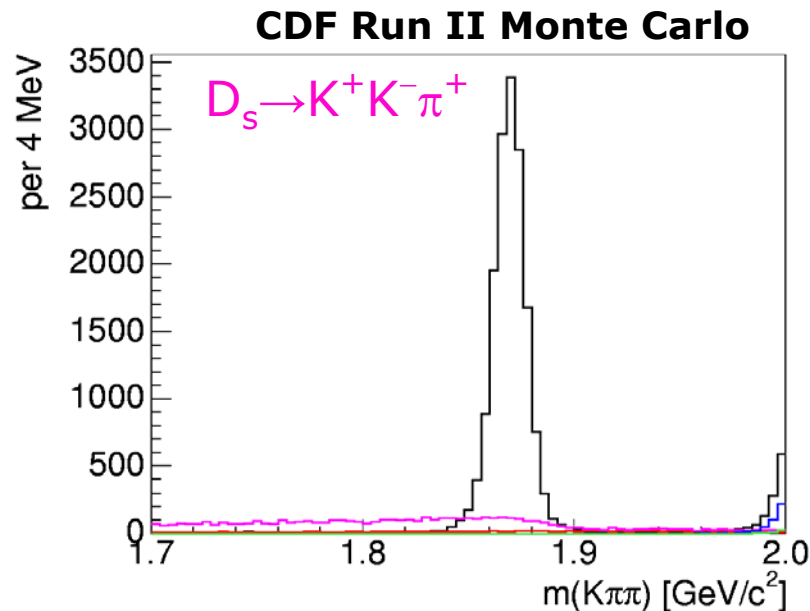
- $L_{xy}(P.V. \rightarrow D)$

- $p_T(\text{tracks})$

- Probability of vertex fits to bottom and charm hadrons



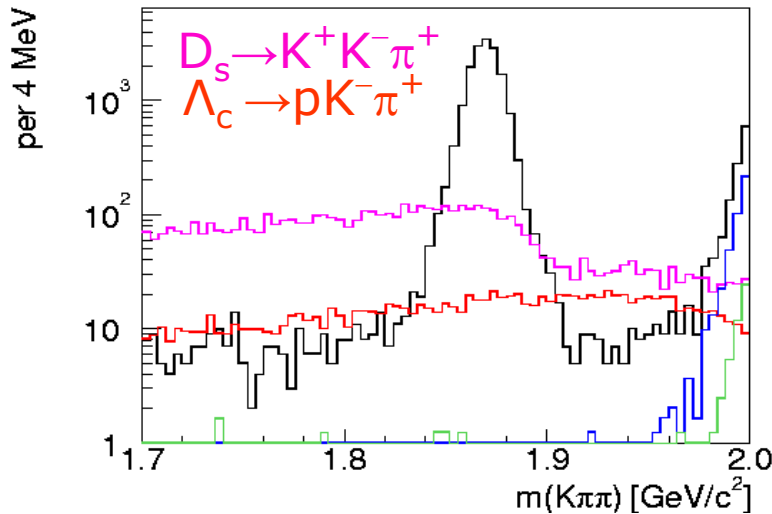
Reflection Backgrounds



- ❑ Combinatorial backgrounds present beneath all signals
- ❑ Significant reflection backgrounds present in two signals
 - D^+ signal contaminated by $D_s^+ \rightarrow K^+ K^- \pi^+$
 - ❑ Include reflection in fit to signal
 - Λ_c^+ signal contaminated by $D^+ \rightarrow K^- \pi^+ \pi^+$, $D_s^+ \rightarrow K^+ K^- \pi^+$
 - ❑ Use dE/dx cut on proton in $\Lambda_c^+ \rightarrow pK^- \pi^+$

D_s^+ Reflection in D^+ Signal

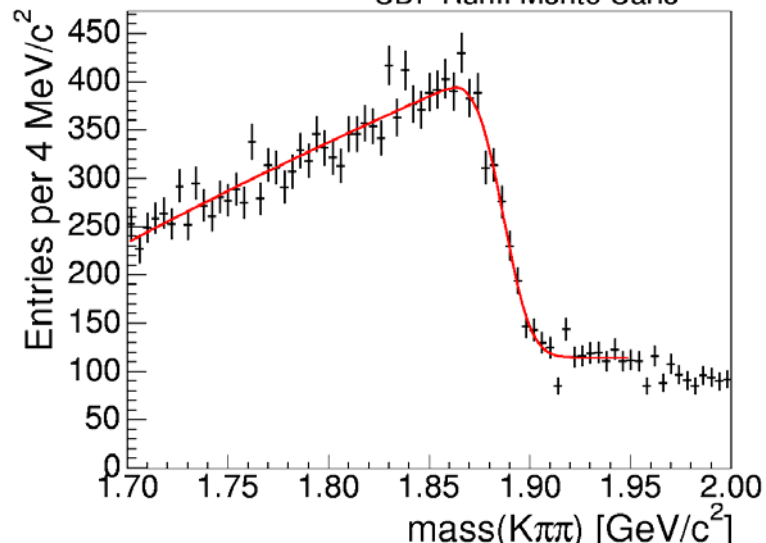
CDF Run II Monte Carlo



- Use MC to determine reflection shape
- Fit number of $D_s^+ \rightarrow \phi \pi^+$ observed in data
- Scale efficiency of $D_s^+ \rightarrow \phi \pi^+$ to generic $D_s^+ \rightarrow K^- K^+ \pi^+$

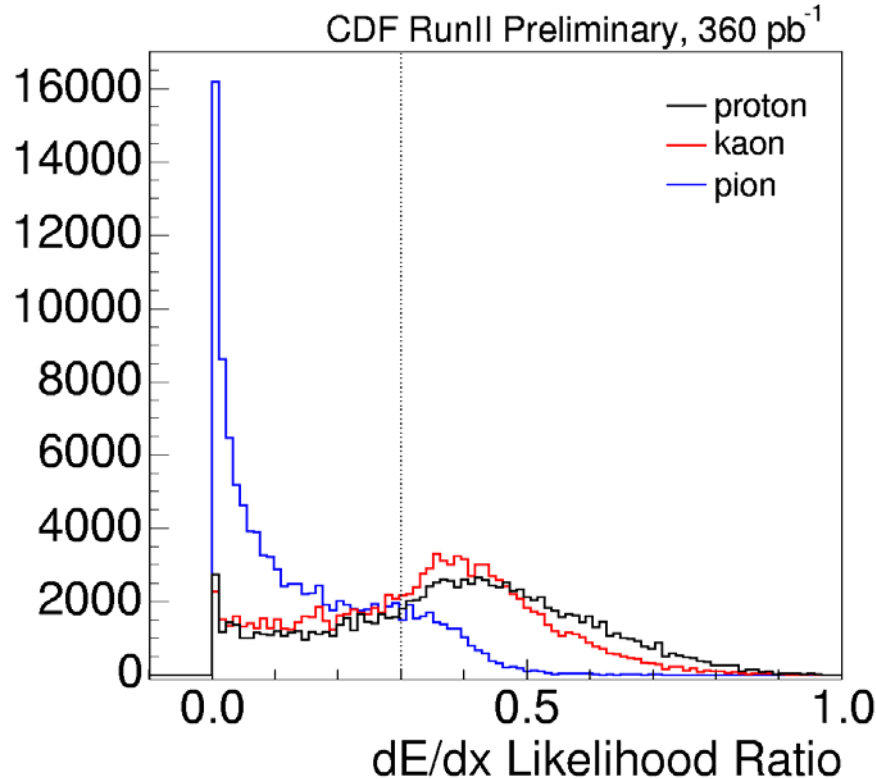
$$R_{\phi\pi} = 0.246 \pm 0.016$$

CDF RunII Monte Carlo



- Measure $N_{D_s} = 13.4 \pm 0.8$ % relative to D^+ yield in $m \in [1.78, 1.95]$

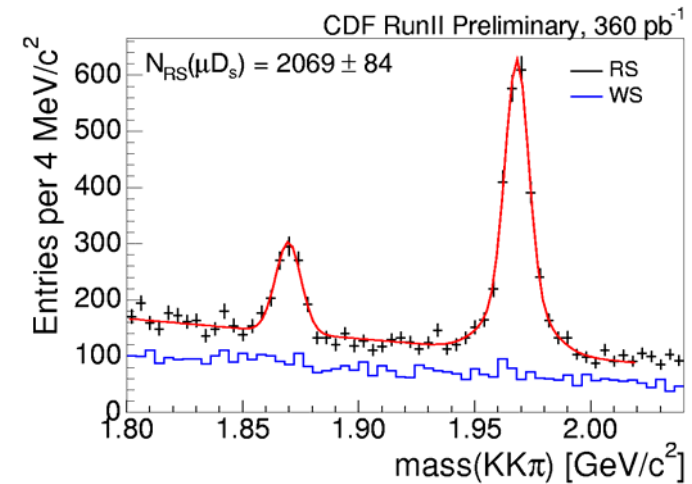
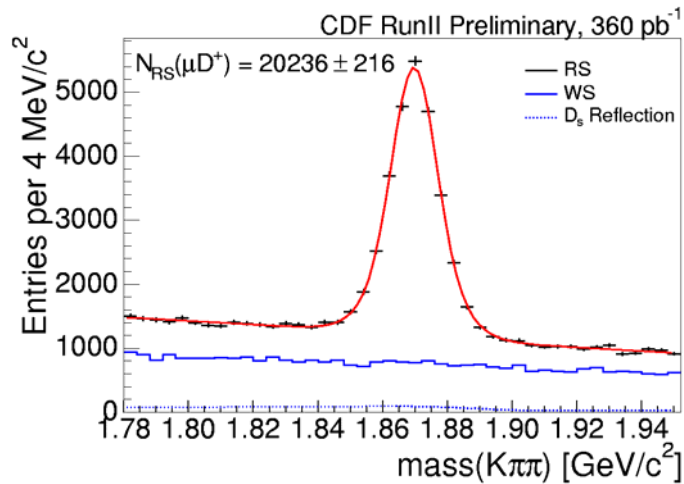
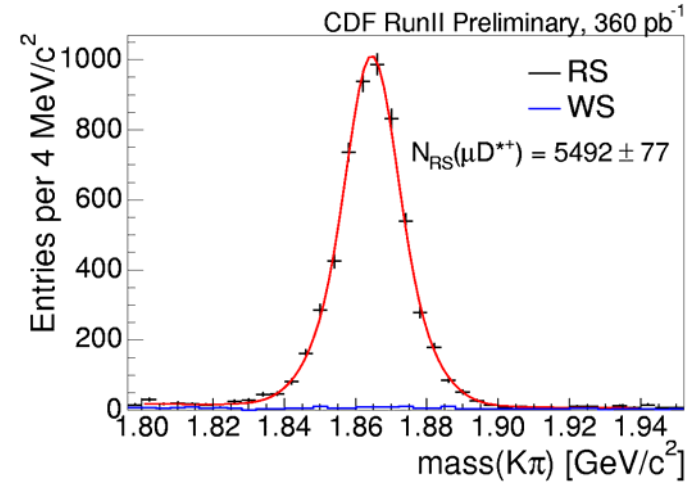
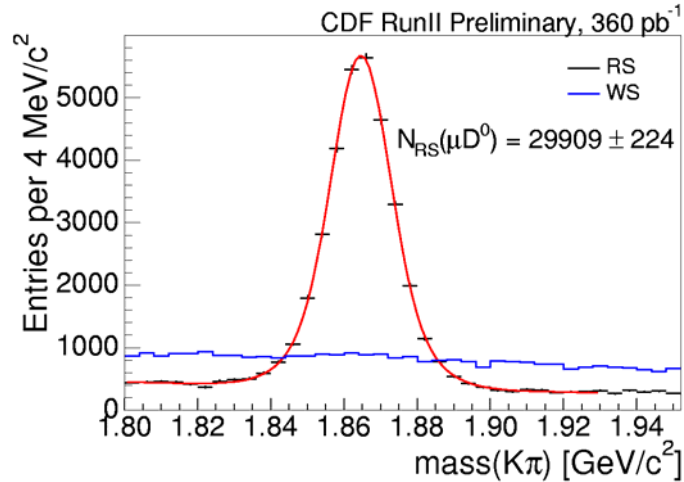
dE/dx Likelihood Cut



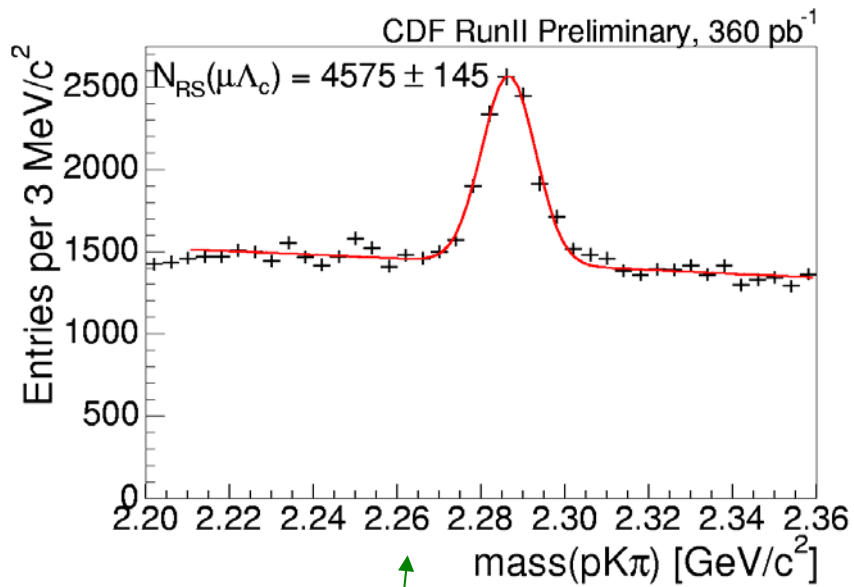
□ $\mathcal{LR} \equiv \mathcal{L}(p) / [\mathcal{L}(p) + \mathcal{L}(K) + \mathcal{L}(\pi) + \mathcal{L}(e) + \mathcal{L}(\mu)]$

■ $\mathcal{L}(i)$ constructed from $Z = \text{Log}[(dE/dx)_{\text{meas}} / (dE/dx)_{\text{pred}}]$

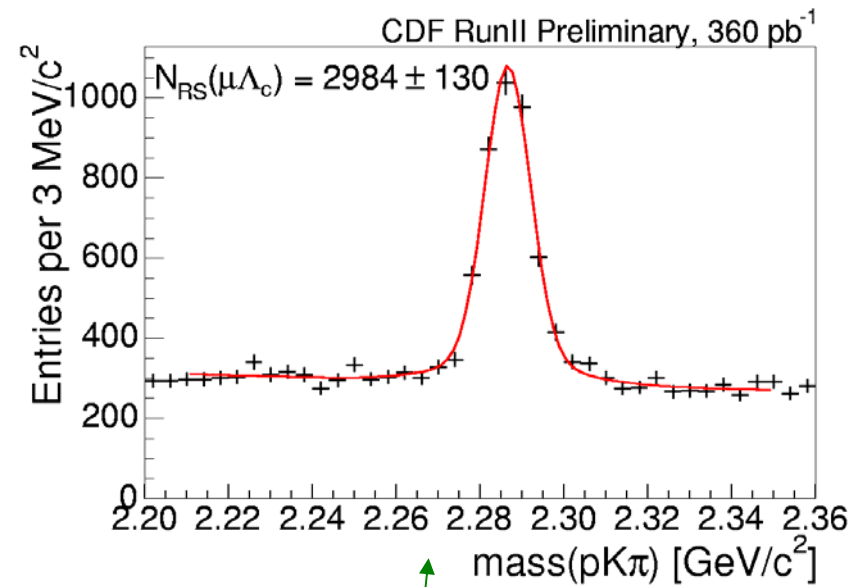
μ +Charm Meson Signals



$\mu + \Lambda_c$ Signal



No dE/dx cut



With dE/dx cut on proton

Semileptonic B Yields

Signature	Yield	
$\ell^- D^0$	$46,848 \pm 275$	} 360 pb^{-1}
$\ell^- D^{*+}$	$8,490 \pm 95$	
$\ell^- D^+$	$31,015 \pm 262$	
$\ell^- D_s^+$	$3,081 \pm 95$	
$\ell^- \Lambda_c^+$	$4,739 \pm 168$	

□ Run I yields used in fragmentation fraction measurement

■ $N(e^- D_s^+) = 59 \pm 10$

■ $N(e^- \Lambda_c^+) = 79 \pm 17$

More than 50 times the yield in Run II compared to Run I!

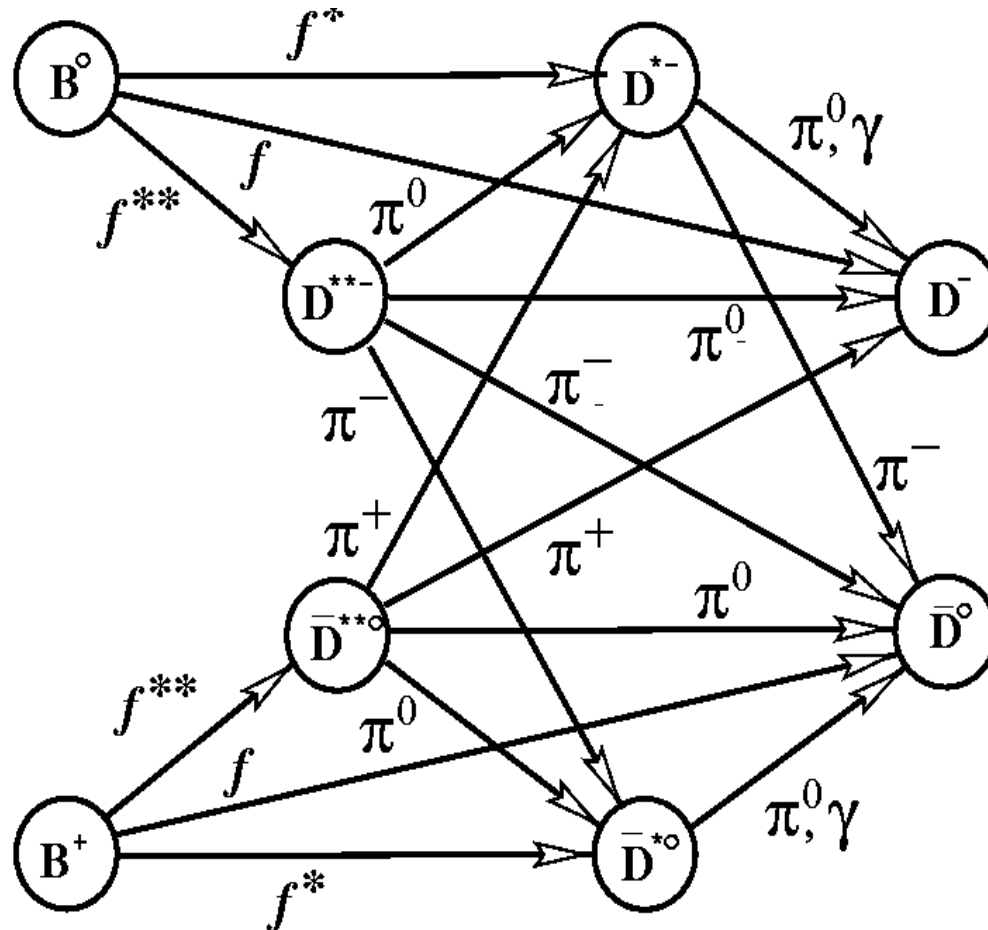
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Sample Composition

- ❑ Need to disentangle parent B hadrons from lepton-charm signals
 - Missing neutrino prevents fully reconstructing decay at CDF
 - Allows excited charm states to contribute to reconstructed charm signals
- ❑ Cross-talk between signals
 - $\bar{B}^0, B^-, \bar{B}_s^0$ contribute to $\ell^- D^+, \ell^- D^0, \ell^- D^{*+}, \ell^- D_s^+$
 - Λ_b^0 contributes to $\ell^- \Lambda_c^+$
 - ❑ Meson \leftrightarrow baryon cross talk small

Simple Sample Composition



- Simple parameterization of semileptonic B^0 , B^+ decays into \bar{D}^0 and D^-

Full Sample Composition

Consider all significant decays to semileptonic charm signals, including sequential semileptonic decays.

\bar{B}^0	B^-	\bar{B}_s^0	Λ_b^0
$\ell\nu D^+$	$\ell\nu D^0$	$\ell\nu D_s^+$	$\ell\nu\Lambda_c^+$
$\ell\nu D^{*+}$ $\rightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D^{*0}$ $\rightarrow D^0\pi^0/\gamma$	$\ell\nu D_s^{*+}$ $\rightarrow D_s^+\gamma$	$\ell\nu\Lambda_c(2593)^+$ $\rightarrow \Sigma_c(2455)^{++}\pi^-$ $\hookrightarrow \Lambda_c^+\pi^+$ $\rightarrow \Sigma_c(2455)^0\pi^+$ $\hookrightarrow \Lambda_c^+\pi^-$
$\ell\nu D_1^+$ $\rightarrow D^{*0}\pi^+$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^0$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D_1^0$ $\rightarrow D^{*0}\pi^0$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^-$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D_{s1}^+(2460)$ $\rightarrow D_{s0}^{*+}\pi^0$ $\hookrightarrow D_s^+\pi^0$ $\rightarrow D_s^+\gamma$	$\rightarrow \Sigma_c(2455)^+\pi^0$ $\hookrightarrow \Lambda_c^+\pi^0$ $\rightarrow \Lambda_c^+\pi^+\pi^-$ $\rightarrow \Lambda_c^+\pi^0\pi^0$ $\rightarrow \Lambda_c^+\gamma$
$\ell\nu D_0^{*+}$ $\rightarrow D^0\pi^+$ $D^+\pi^0$	$\ell\nu D_0^{*0}$ $\rightarrow D^0\pi^0$ $D^+\pi^-$	$\ell\nu D_{s0}^{*+}(2317)$ $\rightarrow D_s^+\pi^0$	$\ell\nu\Lambda_c(2625)^+$ $\rightarrow \Lambda_c^+\pi^+\pi^-$ $\rightarrow \Lambda_c^+\pi^0\pi^0$ $\rightarrow \Lambda_c^+\gamma$
$\ell\nu D_1^{\prime+}$ $\rightarrow D^{*0}\pi^+$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^0$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D_1^{\prime0}$ $\rightarrow D^{*0}\pi^0$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^-$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D_{s1}^{\prime+}(2535)$ $\rightarrow D^{*+}K^0$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$ $\rightarrow D^{*0}K^+$ $\hookrightarrow D^0\pi^0/\gamma$	$\ell\nu\Sigma_c(2455)^{++}\pi^-$ $\rightarrow \Lambda_c^+\pi^+$ $\ell\nu\Sigma_c(2455)^0\pi^+$ $\rightarrow \Lambda_c^+\pi^-$
$\ell\nu D_2^{*+}$ $\rightarrow D^{*0}\pi^+$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^0$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$ $\rightarrow D^0\pi^0$ $\rightarrow D^+\pi^-$	$\ell\nu D_2^{*0}$ $\rightarrow D^{*0}\pi^0$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^{*+}\pi^-$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$ $\rightarrow D^0\pi^0$ $\rightarrow D^+\pi^-$	$\ell\nu D_{s2}^{\prime+}(2573)$ $\rightarrow D^{*+}K^0$ $\hookrightarrow D^0\pi^+$ $D^+\pi^0/\gamma$ $\rightarrow D^{*0}K^+$ $\hookrightarrow D^0\pi^0/\gamma$ $\rightarrow D^+K^0$ $\rightarrow D^0K^+$	$\ell\nu\Sigma_c(2455)^+\pi^0$ $\rightarrow \Lambda_c^+\pi^0$ $\ell\nu\Lambda_c^+f_0$ $\ell\nu\Lambda_c^+\pi^+\pi^-$ (NR) $\ell\nu\Lambda_c^+\pi^0\pi^0$ (NR)
$\ell\nu D^{*+}\pi^0$ (NR) $\rightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D^{*+}\pi^-$ (NR) $\rightarrow D^0\pi^+$ $D^+\pi^0/\gamma$	$\ell\nu D_s^{*+}\pi^0$ (NR) $\rightarrow D_s^+\gamma$	
$\ell\nu D^{*0}\pi^+$ (NR) $\rightarrow D^0\pi^0/\gamma$	$\ell\nu D^{*0}\pi^0$ (NR) $\rightarrow D^0\pi^0/\gamma$	$\ell\nu D_s^{*+}\pi^0$ (NR)	
$\ell\nu D^+\pi^0$ (NR) $\ell\nu D^0\pi^+\pi^0$ (NR)	$\ell\nu D^+\pi^-$ (NR) $\ell\nu D^0\pi^0$ (NR)		
$D^{(*)}\bar{D}^{(*)}K$ $D^{(*)+}D^{(*)-}$ $D_s^{(*)}D^{(*)}X$	$D^{(*)}\bar{D}^{(*)}K$ $D_s^{(*)}D^{(*)}X$	$D^{(*)}\bar{D}^{(*)}K$ $D_s^{(*)}D^{(*)}X$ $D_s^{(*)}D_s^{(*)}X$	$\tau^-\nu\Lambda_c^+$ $\tau^-\nu\Lambda_c(2593)^+$ $\tau^-\nu\Lambda_c(2625)^+$
$\tau^-\nu D^{+(*)},(**)$	$\tau^-\nu D^{0(*)},(**)$	$\tau^-\nu D_s^{+(*)},(**)$	

“Physics backgrounds”
e.g. $B^0 \rightarrow D^+(\rightarrow K^-\pi^+\pi^+)D^-(\rightarrow \ell^-X)$

Parameterization

□ Simple example w/only ground state

$$N(\ell^+ D^-)$$

$$= N(B^0) \times \mathcal{B}(B^0 \rightarrow \ell^+ \nu D^-) \times \mathcal{B}(D^- \rightarrow K^+ \pi^- \pi^-) \\ \times \varepsilon(B^0 \rightarrow \ell^+ \nu D^-, D^- \rightarrow K^+ \pi^- \pi^-)$$

$$= N(b) \times f_d \times \tau(B^0) \times \Gamma(B^0 \rightarrow \ell^+ \nu D^-) \times \mathcal{B}(D^- \rightarrow K^+ \pi^- \pi^-) \\ \times \varepsilon(B^0 \rightarrow \ell^+ \nu D^-, D^- \rightarrow K^+ \pi^- \pi^-)$$

Number of b quarks

□ Extend this to all mesons

■ Generalize notation

$$N(\ell D_i) = \sum_{j=d,u,s} N(b) \times f_j \times \tau(B_j) \times \sum_k \Gamma_k \times \mathcal{B}_{ijk}(D_{jk} \rightarrow D_i) \times \varepsilon_{ijk}$$

$$\square D_i = D^-, D^0, D^{*-}, \text{ and } D_s$$

$$\square \Gamma_k = \Gamma, \Gamma^*, \Gamma^{**}$$

Branching Ratios

- Need model for semileptonic decays
 - $\Gamma(B \rightarrow \ell \nu D^{(*,**)}) = 1/\tau(B) \times \mathcal{B}(B \rightarrow \ell \nu D^{(*,**)})$
 - Use spectator model for meson decays
 - $\Gamma(B^0 \rightarrow \ell \nu D^-) = \Gamma(B^+ \rightarrow \ell \nu D^0) = \Gamma(B_s \rightarrow \ell \nu D_s) \equiv \Gamma$
 - $\Gamma(B^0 \rightarrow \ell \nu D^{*-}) = \Gamma(B^+ \rightarrow \ell \nu D^{*0}) = \Gamma(B_s \rightarrow \ell \nu D_s^*) \equiv \Gamma^*$
 - $\Gamma(B^0 \rightarrow \ell \nu D^{**-}) = \Gamma(B^+ \rightarrow \ell \nu D^{**0}) = \Gamma(B_s \rightarrow \ell \nu D_s^{**}) \equiv \Gamma^{**}$
 - Assume $\Gamma + \Gamma^* + \Gamma^{**} = \Gamma_{sl}(B \rightarrow \ell \nu X)$
- Use fixed sample composition for $\Lambda_b \rightarrow \ell \nu \Lambda_c X$
- Use PDG 2004 for known branching ratios
 - Use theoretical predictions and symmetry principles for unmeasured BR

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Acceptances and Efficiencies

- ❑ Need relative acceptances and efficiencies of individual ℓ +charm decays
 - Fit to relative fractions
- ❑ Use MC to determine acceptances
 - Detector geometry
 - Kinematic differences between lepton-charm signals
- ❑ Use data to determine remaining efficiencies which are different between charm channels

Monte Carlo

- Monte Carlo is good for most kinematic differences between lepton-charm signals
 - $ct(D)$, $p_T(\text{tracks})$, etc...
- Generate single B hadron directly
 - Decay with EvtGen package
 - Use input p_T spectrum measured from data
 - Inclusive $p_T(b \rightarrow J/\psi X)$ spectrum
 - Separate set of Monte Carlo generated for each decay in sample composition
 - Separate sets of Monte Carlo for e , μ
- Validate with inclusive Monte Carlo samples by comparing data and Monte Carlo
 - *e.g.* $B \rightarrow \ell \nu DX$

Baryon Decays

□ Need to implement physical baryon decay model

□ $T = (G_F/\sqrt{2})V_{Qq}\bar{u}_\ell\gamma_\mu(1-\gamma_5)v_\nu\langle\Lambda_q|J^\mu|\Lambda_Q\rangle$

□ V-A current

■ $1/2^+ \rightarrow 1/2^+ \quad (\Lambda_b^0 \rightarrow \Lambda_c^+)$

□ $\langle\Lambda_c^+|V^\mu|\Lambda_b^0\rangle = \bar{u}(p',s')[F_1(q^2)\gamma^\mu + F_2(q^2)p^\mu/m_{\Lambda_b} + F_3(q^2)p'^\mu/m_{\Lambda_c}]u(p,s)$

□ $\langle\Lambda_c^+|A^\mu|\Lambda_b^0\rangle = \bar{u}(p',s')[G_1(q^2)\gamma^\mu + G_2(q^2)p^\mu/m_{\Lambda_b} + G_3(q^2)p'^\mu/m_{\Lambda_c}]\gamma^5u(p,s)$

■ $1/2^+ \rightarrow 3/2^- \quad (\Lambda_b^0 \rightarrow \Lambda_c^+(2625))$

□ $\langle\Lambda_c^+(2625)|V^\mu|\Lambda_b^0\rangle = \bar{u}_\alpha(p',s')[p^\alpha/m_{\Lambda_b}(F_1\gamma^\mu + F_2p^\mu/m_{\Lambda_b} + F_3p'^\mu/m_{\Lambda_c}) + F_4g^{\alpha\mu}]u(p,s)$

□ $\langle\Lambda_c^+(2625)|A^\mu|\Lambda_b^0\rangle = \bar{u}_\alpha(p',s')[p^\alpha/m_{\Lambda_b}(G_1\gamma^\mu + G_2p^\mu/m_{\Lambda_b} + G_3p'^\mu/m_{\Lambda_c}) + G_4g^{\alpha\mu}]\gamma^5u(p,s)$

□ $u_\alpha(p',s') = u(p',s')\varepsilon_\alpha$

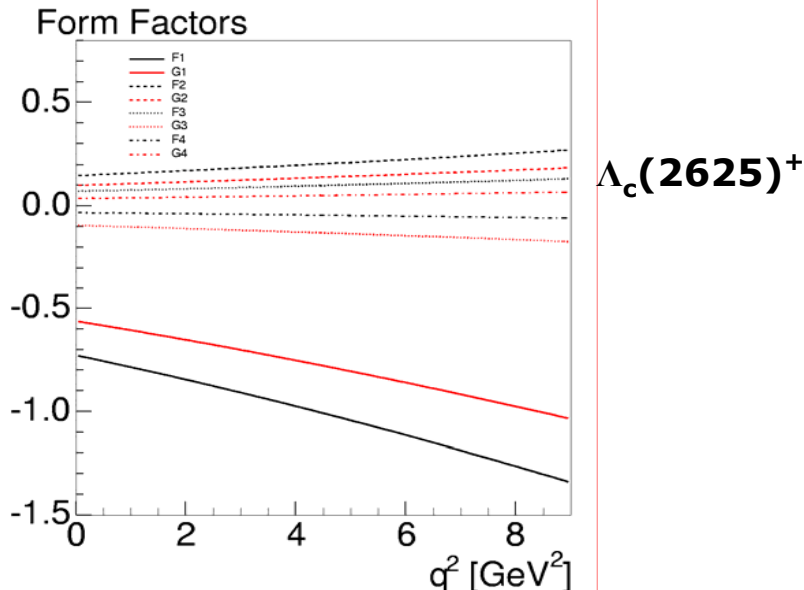
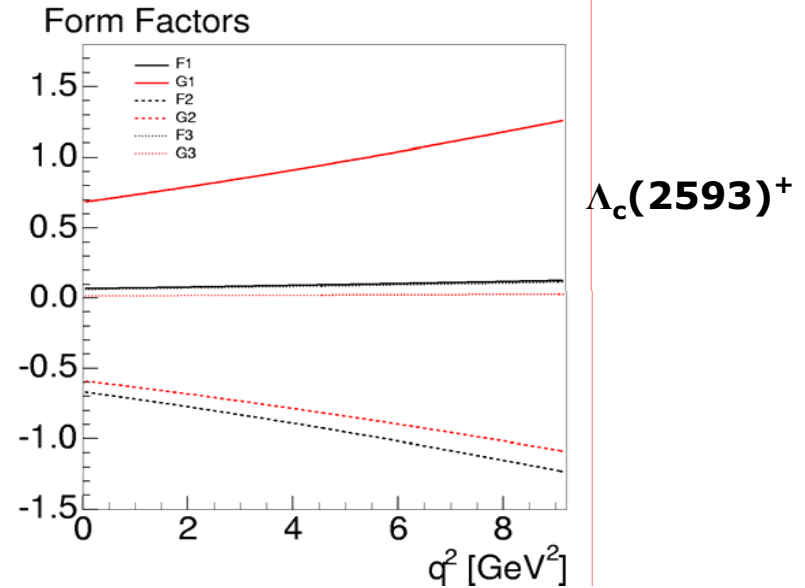
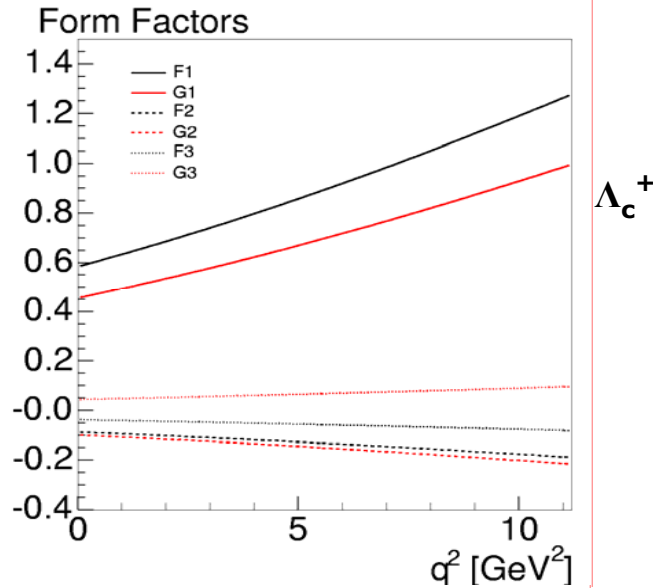
▪ $u_\alpha(p',s')p'^\alpha = u(p',s')\varepsilon_\alpha p'^\alpha = 0$

▪ $\varepsilon_\alpha(0, \underline{e}(M))$ in rest frame (of $\Lambda_c(2625)$)

▪ $\underline{e}(\pm 1) = 1/\sqrt{2}(-/+1, -i, 0)$

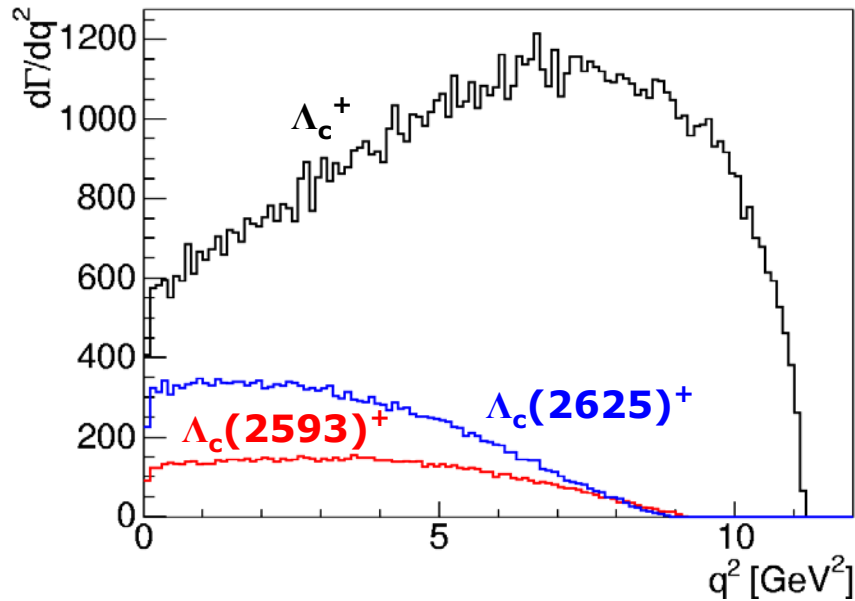
▪ $\underline{e}(0) = (0, 0, 1)$

$\Lambda_b \rightarrow \Lambda_c$ Form Factors



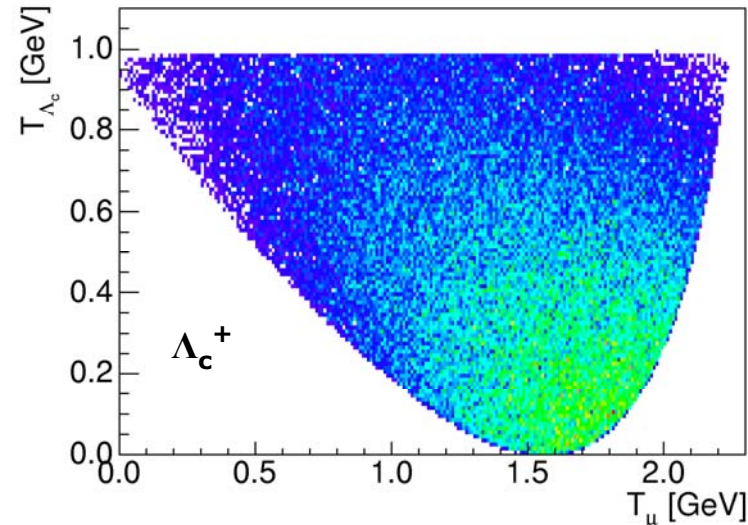
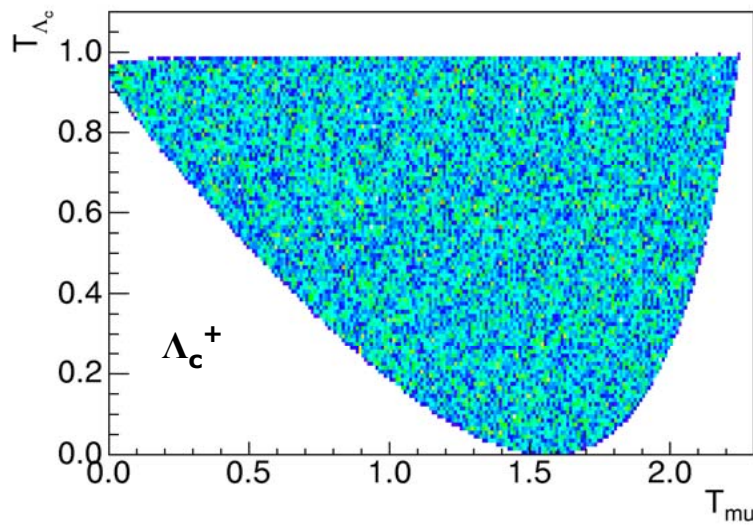
Form factor predictions from Pervin, Capstick, and Roberts et al. only made for $\ell\nu\Lambda_c^{(*,**)}$ final states

New Baryon Decay Model



□ New baryon decay model implemented according to predictions by Pervin, Capstick, and Roberts

- Constituent quark model
- Phys. Rev. C72,035201 (2005)



Reconstruction Efficiencies

- Measure some efficiencies from data
 - Single track efficiency
 - $D^0 \rightarrow K^- \pi^+$ vs. $D^+ \rightarrow K^- \pi^+ \pi^+$
 - XFT trigger efficiencies for p, K, π
 - dE/dx efficiency for cut on proton
 - $\Lambda_c^+ \rightarrow p K^- \pi^+$
- Use to re-weight Monte Carlo for total efficiency

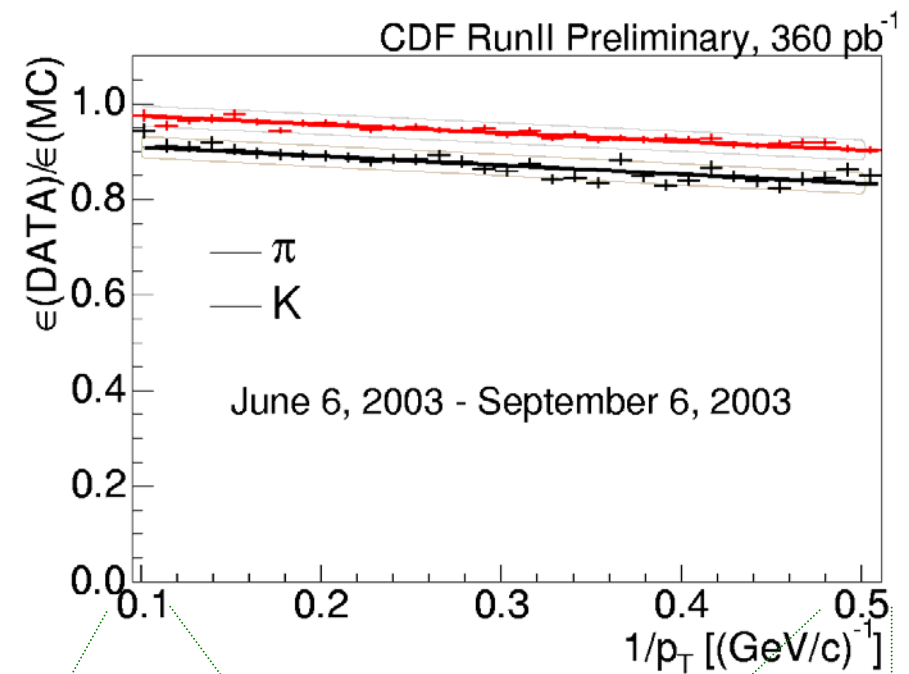
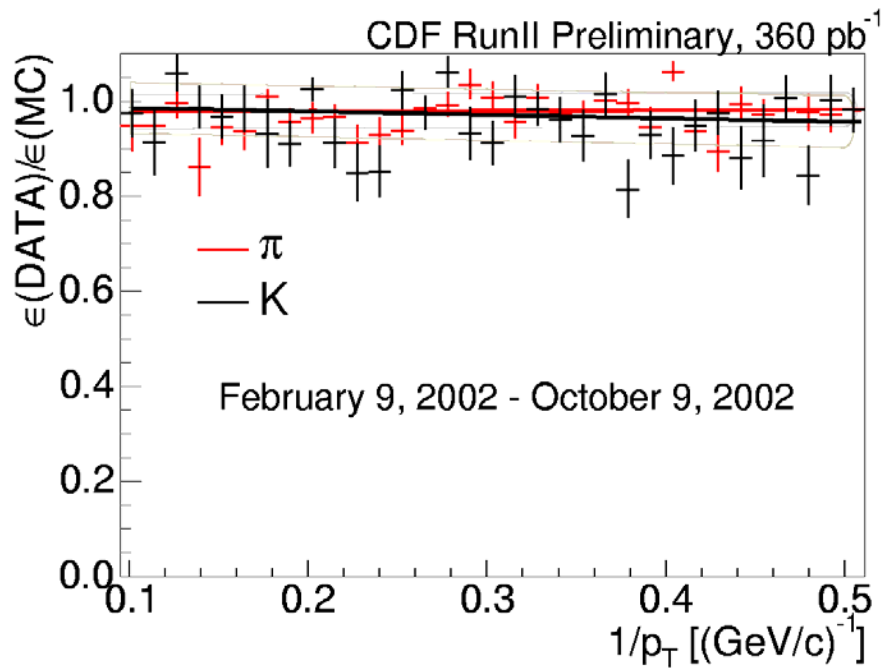
Single Track Efficiency

- Efficiency to add an additional track depends on environment in detector
 - Monte Carlo only generates B hadron
- Reconstruct $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
 - Measure efficiency relative to $D^0 \rightarrow K^- \pi^+$ in data and Monte Carlo
 - Efficiency to add two additional tracks
- Measure
 - $\varepsilon_{\text{trk}} = 87.8^{+2.1}_{-1.2}$ (stat.+sys.)%

XFT Efficiencies

- ❑ Differences in tracking p , K , π in drift chamber
 - Differences in efficiencies between reconstructed charm states
 - Only applies to SVT trigger track
 - Varying drift chamber performance not optimally described by Monte Carlo
 - Again measure from data
 - ❑ Re-weight Monte Carlo
 - ❑ Measure in separate run ranges

XFT Efficiencies

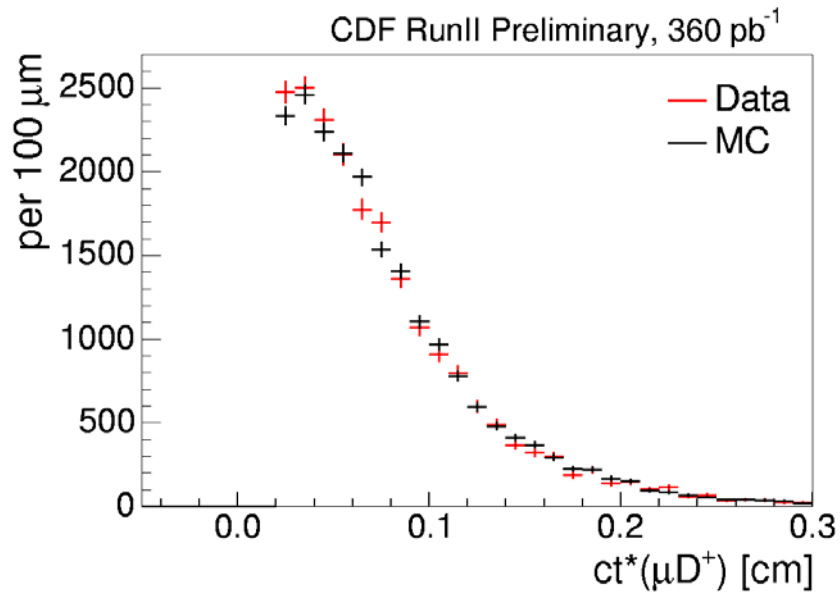


10 [GeV/c]

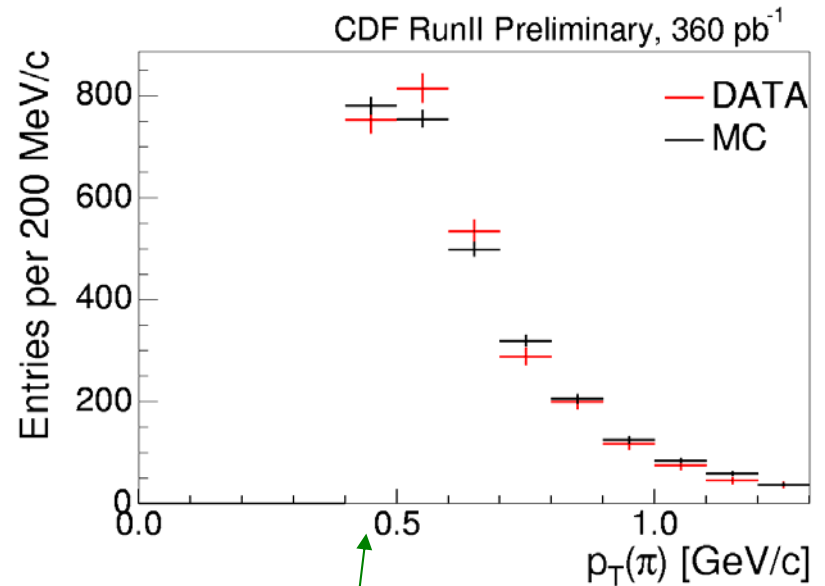
2 [GeV/c]

Comparison of Data and MC

$\chi^2/\text{NDF}=24.3/27.0$

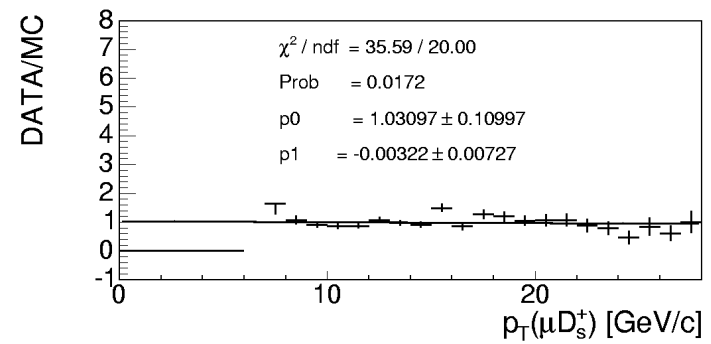
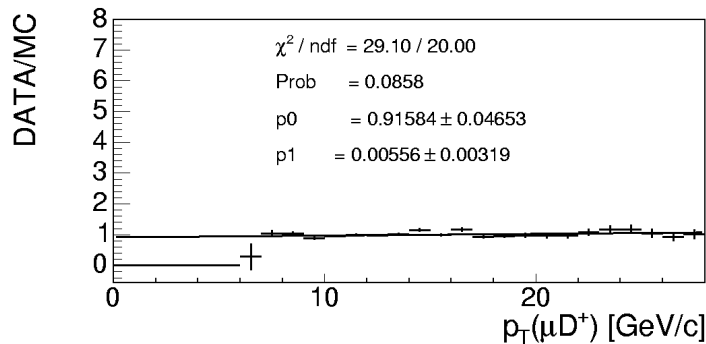
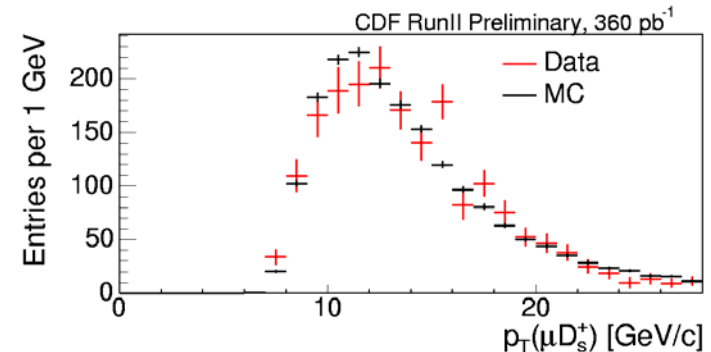
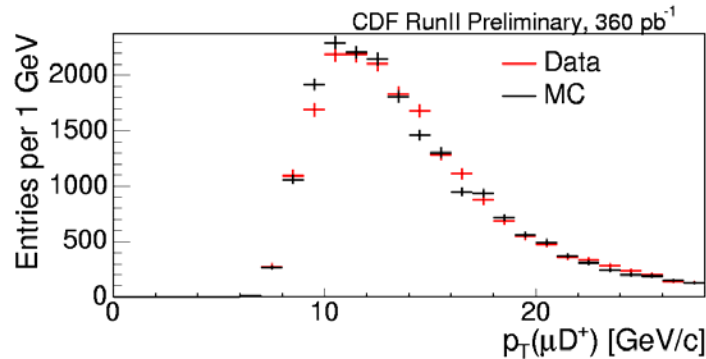


$\chi^2/\text{NDF}=11.9/8.0$



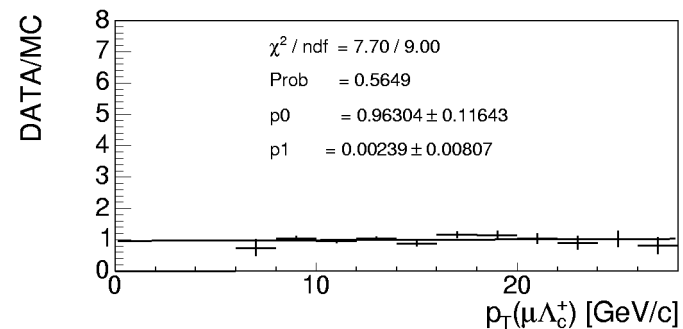
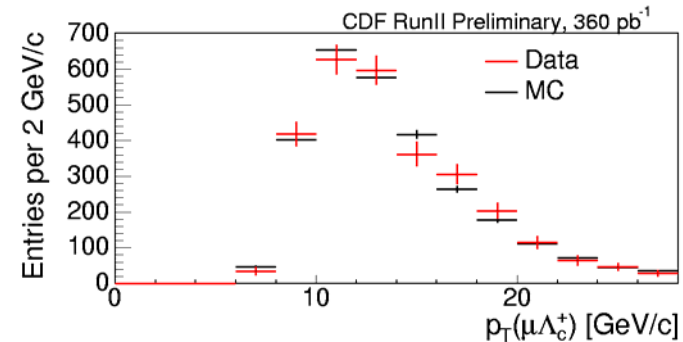
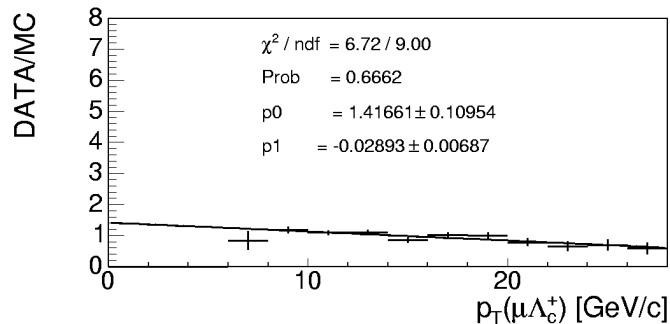
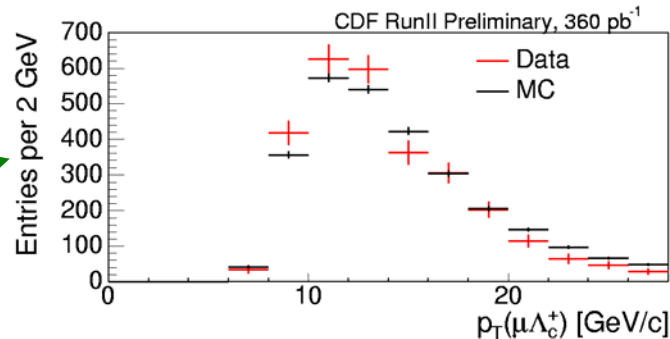
π^* from $e\text{D}^*$

B Meson p_T Spectra



- Choice of p_T spectrum used is important for determination of efficiencies
- Use inclusive $p_T(b \rightarrow J/\psi X)$ spectrum measured in Run II for meson signals
 - Good agreement with data

Λ_b p_T Spectra



- ❑ Inclusive $p_T(b \rightarrow J/\psi X)$ spectrum does not describe the $\ell\Lambda_c$ data
 - Observe softer spectrum in data than the MC
- ❑ Tune the $\ell\Lambda_c$ Monte Carlo spectrum to match the $\ell\Lambda_c$ data

Outline

- B fragmentation overview
- Semileptonic signal reconstruction
- Semileptonic sample composition
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General Idea of Fit

- Express each term of sample composition in terms of B^0

- Fit for relative production

$$N_{\text{pred}}(\ell D_i) = N(B^0) \sum_{j=d,u,s} f_j/f_d \times \tau(B_j) \\ \times \sum_k \Gamma_k \times \mathcal{B}_{ijk}(D_{jk} \rightarrow D_i) \times \varepsilon_{ijk}$$

$$N_{\text{pred}}(\ell \Lambda_c) = N(B^0) \times [f_{\Lambda_b}/(f_u + f_d)](1 + f_u/f_d) \\ \times [(\sum_k \mathcal{B}_k(\Lambda_b \rightarrow \ell \nu \Lambda_{c,k} \rightarrow \Lambda_c)) \times \varepsilon_k]$$

- χ^2 fit to 5 lepton charm channels

- $f_u/f_d, f_s/(f_u + f_d), f_{\Lambda_b}/(f_u + f_d)$

- $f_s/f_d = [f_s/(f_u + f_d)] \times (1 + f_u/f_d)$

- $N(B^0)$

- Parameter for fit, not physical number of B^0 's

Implementation of Fit

□ Fit looks like

$$\begin{aligned}\chi^2 = \sum_{i=1..5} & (N_{\text{pred}}(\ell D_i) - N_{\text{meas}}(\ell D_i))^2 / \sigma_{\text{meas},i}^2 \\ & + (\Gamma - \Gamma_{\text{PDG}})^2 / \sigma_{\Gamma_{\text{PDG}}}^2 \\ & + (\Gamma^* - \Gamma_{\text{PDG}}^*)^2 / \sigma_{\Gamma_{\text{PDG}}^*}^2 \\ & + (\Gamma^{**} - \Gamma_{\text{PDG}}^{**})^2 / \sigma_{\Gamma_{\text{PDG}}^{**}}^2\end{aligned}$$

- Gaussian constraints for Γ , Γ^* , Γ^{**}
- Test with high statistics toy Monte Carlo

Fit Results

Fit Parameter	$e+SVT$	$\mu+SVT$
f_u/f_d	1.044 ± 0.028	1.062 ± 0.024
$f_s/(f_u + f_d)$	0.162 ± 0.008	0.158 ± 0.006
$f_{\Lambda_b}/(f_u + f_d)$	0.292 ± 0.020	0.275 ± 0.015
Γ [ps ⁻¹]	0.0157 ± 0.0007	0.0154 ± 0.0007
Γ^* [ps ⁻¹]	0.0327 ± 0.0014	0.0331 ± 0.0013
Γ^{**} [ps ⁻¹]	0.0145 ± 0.0010	0.0146 ± 0.0010
$N(\bar{B}^0)$ (10^9)	2.02 ± 0.07	2.93 ± 0.10

2004 PDG

w/o $\bar{\chi}$ constraint:

$$f_s/(f_u + f_d) = 0.109 \pm 0.026$$

$$f_{\Lambda_b}/(f_u + f_d) = 0.133 \pm 0.023$$

with all constraints:

$$f_s/(f_u + f_d) = 0.134 \pm 0.014$$

$$f_{\Lambda_b}/(f_u + f_d) = 0.125 \pm 0.021$$

f_{Λ_b} higher than previously measured!

□ Statistical errors ONLY

□ Fit $e+SVT$ and $\mu+SVT$ separately

■ Cancel lepton ID efficiencies

■ Statistically independent samples

□ Results are consistent- very nice!

■ Results are consistent if f_u/f_d fixed to unity

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Systematic Uncertainties

- ❑ Measurement is dominated by systematic uncertainties
 - Largest come from knowledge of branching ratios
 - ❑ Particularly ground state charm BRs!!!
 - Other source of systematic uncertainty arise from determination of efficiencies, counting yields, and false lepton backgrounds
 - ❑ Knowledge of the B_s^0 and Λ_b^0 p_T spectrum
 - ❑ Residual false lepton contamination

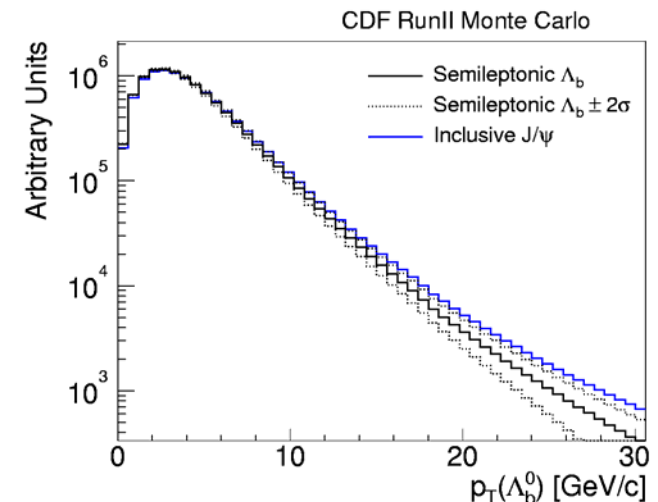
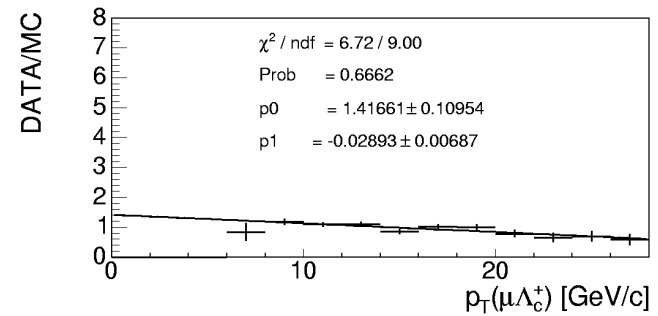
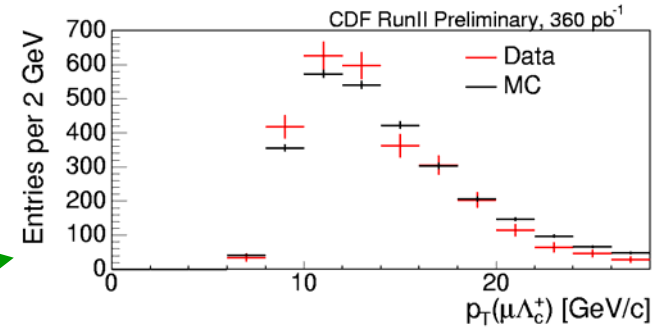
Λ_b p_T Spectrum Uncertainty

□ Vary tuned $\ell\Lambda_c$ spectrum to match inclusive J/ψ spectrum

■ Produces large uncertainty:
 ± 0.049

■ Estimate conservatively

□ True Λ_b^0 spectrum isn't known



Systematic Uncertainties

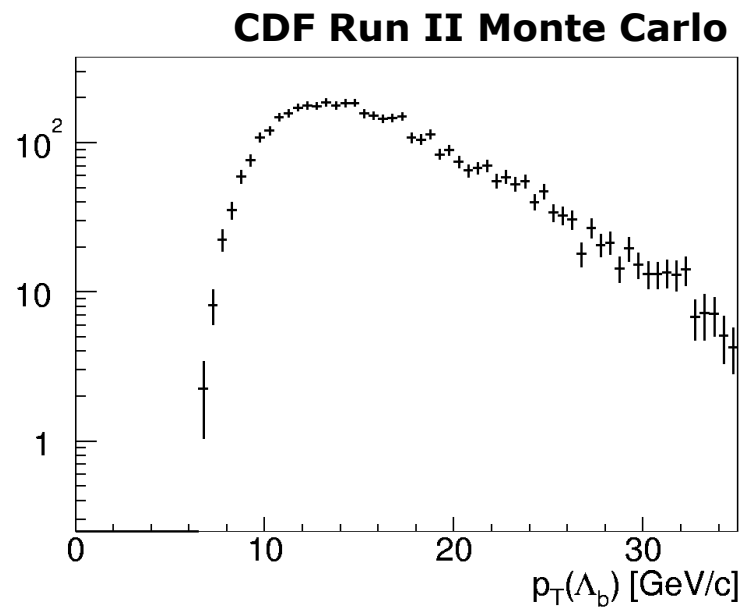
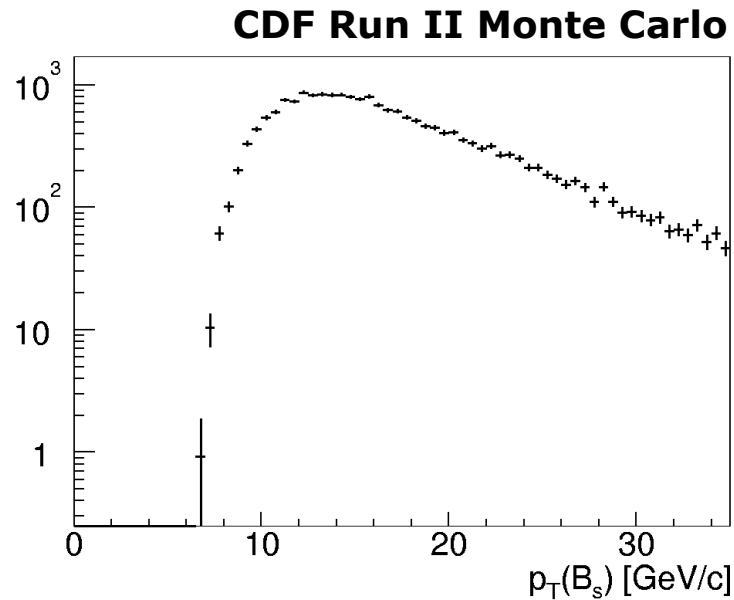
Systematic	f_u/f_d	$f_s/(f_u + f_d)$	$f_{\Lambda_b}/(f_u + f_d)$
Fake Leptons	-0.039	-0.001	+0.018
Variation of cuts	± 0.011	± 0.0003	± 0.019
D_s reflection	+0.001	+0.00002	+0.0001
XFT eff.	± 0.003	± 0.0004	± 0.006
Single track	$^{+0.013}_{-0.014}$	± 0.002	± 0.002
Sample comp. lifetimes	$^{+0.018}_{-0.014}$	± 0.006	± 0.002
MC lifetimes	-	$^{+0.005}_{-0.001}$	$^{+0.0077}_{-0.0136}$
MC statistics	± 0.005	± 0.0007	± 0.0006
p_T spectra	-	± 0.008	± 0.049
dE/dx eff.	-	-	± 0.012
Λ_b^0 polarization	-	-	± 0.007
Total (eff)	$^{+0.025}_{-0.045}$	$^{+0.011}_{-0.010}$	$^{+0.058}_{-0.056}$
$\mathcal{BR}(\Lambda_b^0 \rightarrow \ell^- \nu \Lambda_c^+ X)$	-	-	$^{+0.076}_{-0.048}$
Λ_b^0 sample composition	-	-	± 0.045
$\mathcal{BR}(D^{**})$	± 0.010	± 0.004	± 0.011
“physics bkg”	± 0.001	± 0.002	± 0.001
$\mathcal{BR}(D^+ \rightarrow K^- \pi^+ \pi^+)$	± 0.054	± 0.003	± 0.010
$\mathcal{BR}(D^0 \rightarrow K^- \pi^+)$	± 0.020	± 0.003	± 0.003
$\mathcal{BR}(D_s^+ \rightarrow \phi \pi^+)$	± 0.0006	$^{+0.057}_{-0.034}$	± 0.001
$\mathcal{BR}(\Lambda_c^+ \rightarrow p K^- \pi^+)$	-	-	$^{+0.091}_{-0.053}$
Total (BR)	± 0.058	$^{+0.057}_{-0.034}$	$^{+0.128}_{-0.086}$
Total	$^{+0.062}_{-0.074}$	$^{+0.058}_{-0.035}$	$^{+0.141}_{-0.103}$

+0.062 -0.074

+0.058 -0.035

+0.141 -0.103

p_T Threshold for Measurement



- Choose to quote p_T threshold for all fragmentation fractions
 - $p_T(B) > 7$ GeV/c determined from Monte Carlo

Final Results

$$\frac{f_u}{f_d} = 1.054 \pm 0.018(stat)_{-0.045}^{+0.025}(sys) \pm 0.058(BR)$$

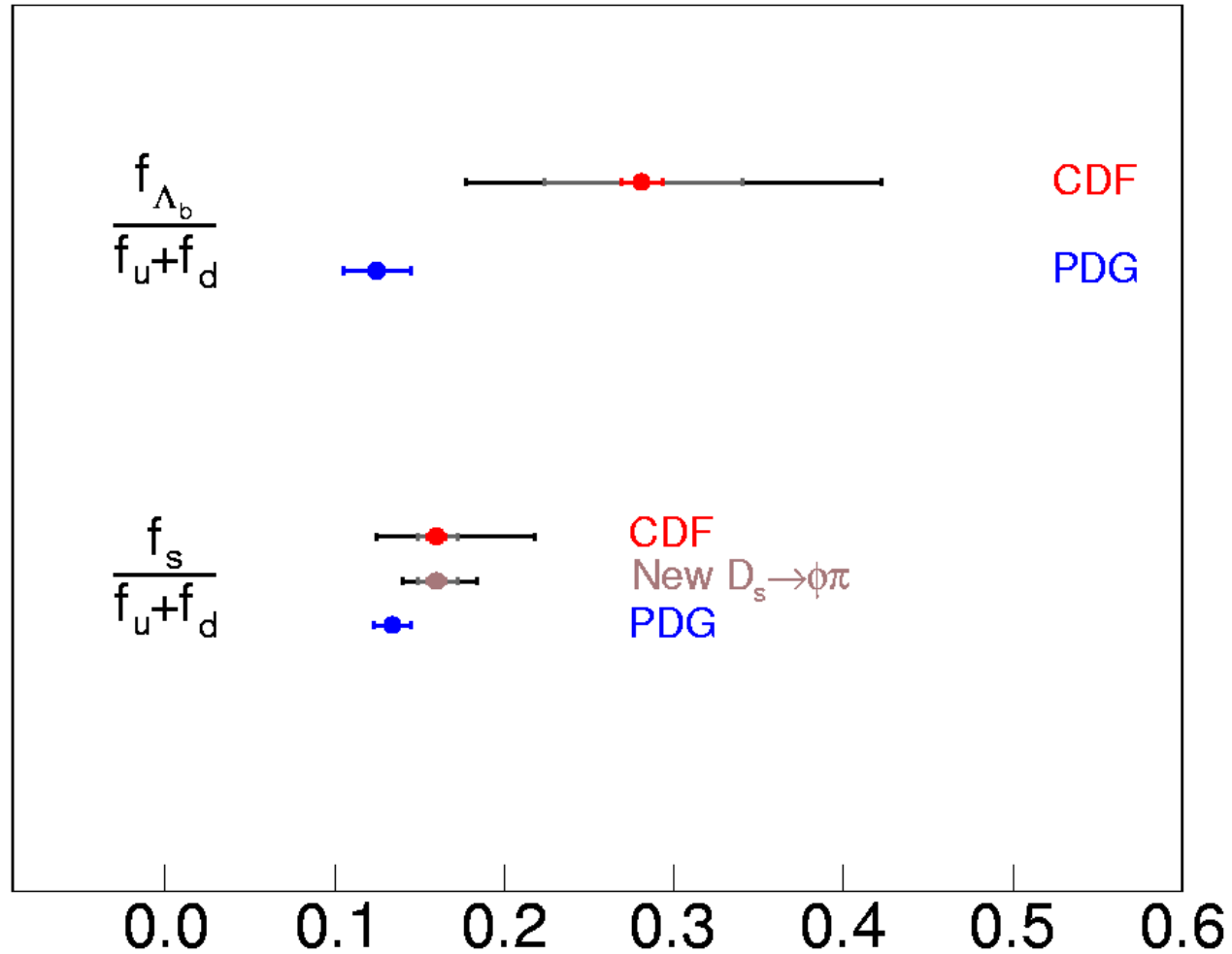
$$\frac{f_s}{f_u + f_d} = 0.160 \pm 0.005(stat)_{-0.010}^{+0.011}(sys)_{-0.034}^{+0.057}(BR)$$

$$\frac{f_{\Lambda_b}}{f_u + f_d} = 0.281 \pm 0.012(stat)_{-0.056}^{+0.058}(sys)_{-0.086}^{+0.128}(BR).$$

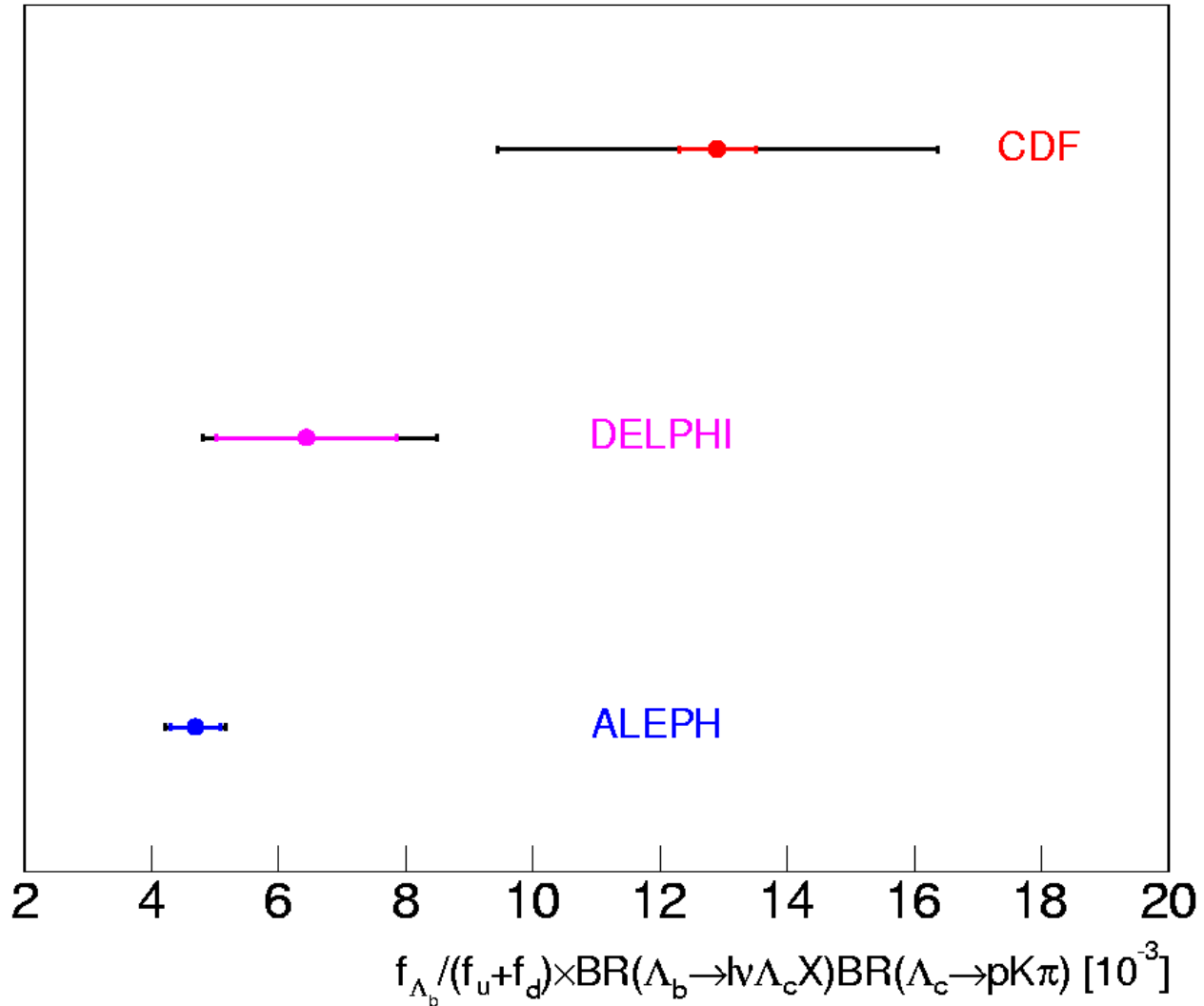
□ Weighted average between e+SVT and μ +SVT samples

- Statistical error is very small!
- Error on $f_s/(f_u+f_d)$ is dominated by PDG 2004
 - $\mathcal{B}(D_s^+ \rightarrow \phi\pi^+) = (3.6 \pm 0.9)\%$
- Sheldon Stone's estimate of CLEO-c measurement (FPCP06)
 - $\mathcal{B}(D_s^+ \rightarrow \phi\pi^+) = (3.73 \pm 0.42)\%$

Comparison with PDG



Comparisons with Other Results



Outline

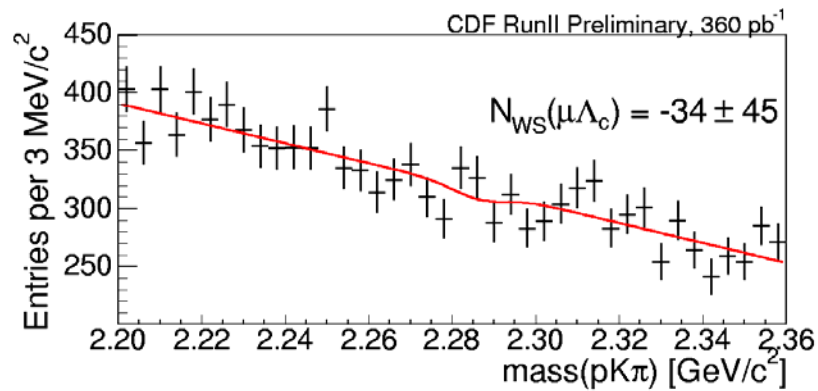
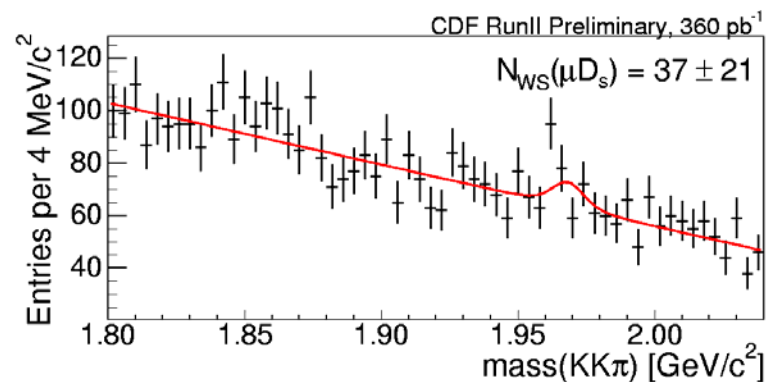
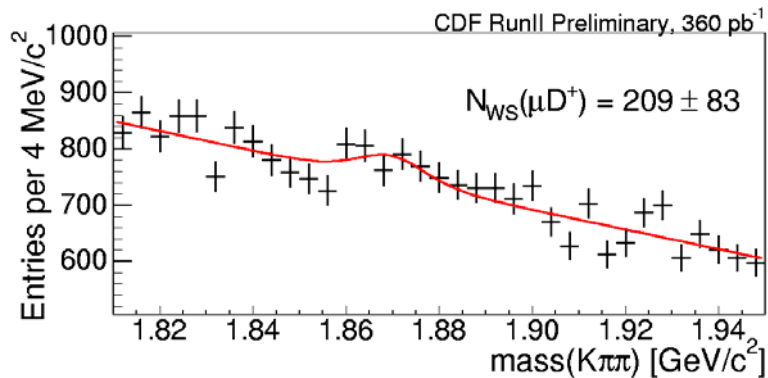
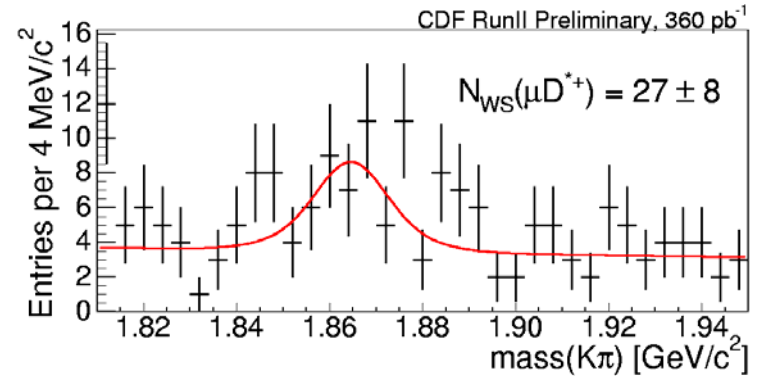
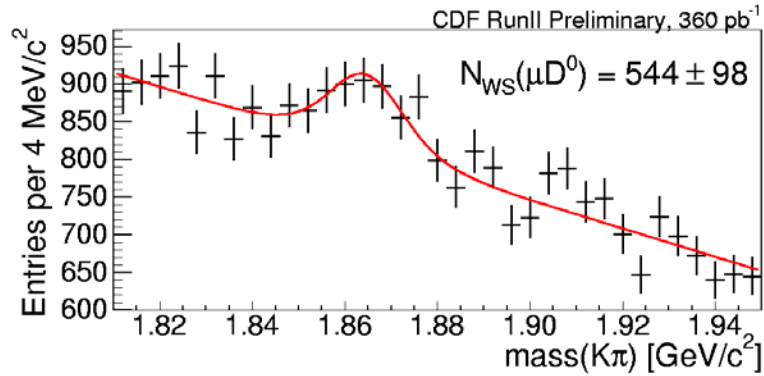
- B fragmentation overview
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Prospects

- ❑ New fragmentation fraction measurement at CDF will be improved with better measurement of charm branching ratios
- ❑ Measurements of B p_T spectra at CDF in fully reconstructed modes limit uncertainty on efficiencies
- ❑ Improved statistics are always helpful!!

Backup Slides

Wrong Sign Lepton-Charm



Fit Results with $f_u = f_d$

Fit Parameter	$e+SVT$	$\mu+SVT$
f_u/f_d	1.0	1.0
$f_s/(f_u + f_d)$	0.163 ± 0.008	0.158 ± 0.006
$f_{\Lambda_b}/(f_u + f_d)$	0.294 ± 0.020	0.277 ± 0.015
Γ [ps ⁻¹]	0.0156 ± 0.0007	0.0153 ± 0.0007
Γ^* [ps ⁻¹]	0.0330 ± 0.0014	0.0335 ± 0.0013
Γ^{**} [ps ⁻¹]	0.0144 ± 0.0010	0.0143 ± 0.0010
$N(\bar{B}^0)$ (10^9)	2.05 ± 0.07	3.00 ± 0.10

2004 PDG

w/o $\bar{\chi}$ constraint:

$$f_s/(f_u + f_d) = 0.109 \pm 0.026$$

$$f_{\Lambda_b}/(f_u + f_d) = 0.133 \pm 0.023$$

with all constraints:

$$f_s/(f_u + f_d) = 0.134 \pm 0.014$$

$$f_{\Lambda_b}/(f_u + f_d) = 0.125 \pm 0.021$$

□ Statistical errors ONLY

□ Fix $f_u/f_d = 1.0$

□ Results are consistent with default result

■ Also very nice...

Relaxed Spectator Model

Fit Parameter	$e+SVT$	$\mu+SVT$
f_u/f_d	1.006 ± 0.006	1.029 ± 0.006
$f_s/(f_u + f_d)$	0.159 ± 0.010	0.155 ± 0.009
$f_{\Lambda_b}/(f_u + f_d)$	0.297 ± 0.020	0.279 ± 0.014
Γ_{B^0} [ps ⁻¹]	0.0158 ± 0.0007	0.0156 ± 0.0007
Γ_{B^+} [ps ⁻¹]	0.0133 ± 0.0009	0.0133 ± 0.0008
Γ_{B_s} [ps ⁻¹]	0.0134 ± 0.0009	0.0134 ± 0.0009
$\Gamma_{B^0}^*$ [ps ⁻¹]	0.0328 ± 0.0014	0.0333 ± 0.0014
$\Gamma_{B^+}^*$ [ps ⁻¹]	0.0370 ± 0.0017	0.0368 ± 0.0015
$\Gamma_{B_s}^*$ [ps ⁻¹]	0.0371 ± 0.0017	0.0372 ± 0.0017
$\Gamma_{B^0}^{**}$ [ps ⁻¹]	0.0142 ± 0.0010	0.0142 ± 0.0009
$\Gamma_{B^+}^{**}$ [ps ⁻¹]	0.0144 ± 0.0010	0.0145 ± 0.0010
$\Gamma_{B_s}^{**}$ [ps ⁻¹]	0.0141 ± 0.0010	0.0141 ± 0.0010
$N(\bar{B}^0)$ (10^9)	2.03 ± 0.08	3.00 ± 0.10

2004 PDG

w/o $\bar{\chi}$ constraint:

$$f_s/(f_u+f_d) = 0.109 \pm 0.026$$

$$f_{\Lambda_b}/(f_u+f_d) = 0.133 \pm 0.023$$

with all constraints:

$$f_s/(f_u+f_d) = 0.134 \pm 0.014$$

$$f_{\Lambda_b}/(f_u+f_d) = 0.125 \pm 0.021$$

□ Allow spectator model constraints to differ between B species

- Total $\Gamma + \Gamma^* + \Gamma^{**} = \Gamma_{sl}$ and $(\Gamma^{(*,**)} - \Gamma_{PDG}^{(*,**)})/\sigma_{\Gamma_{PDG}}$ constraints applied to each B meson separately

Fit Parameter Correlations

	f_u/f_d	$f_s/(f_u+f_d)$	$f_{\Lambda_b}/(f_u+f_d)$	Γ	Γ^*	Γ^{**}	$N(B^0)$
f_u/f_d		-0.021	-0.053	-0.011	-0.135	0.162	-0.249
$f_s/(f_u+f_d)$			0.077	-0.015	-0.058	0.150	-0.116
$f_{\Lambda_b}/(f_u+f_d)$				0.425	0.563	0.239	-0.575
Γ					0.657	-0.122	-0.674
Γ^*						0.134	-0.853
Γ^{**}							-0.436
$N(B^0)$							